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# New Approaches and Algorithms for the Analysis of Vertical Refractivity Profile below 1 km in a Subtropical Region

A. AbouAlmal, R.A. Abd-Alhameed, S.M.R. Jones and H. AlAhmad

**Abstract** — In this paper, 17 years of high resolution surface and radiosonde meteorological data from 1997-2013 for the subtropical Gulf region are analysed. Relationships between the upper air refractivity,  $N_h$ , and vertical refractivity gradient,  $\Delta N$ , in the low troposphere and the commonly available data of surface refractivity,  $N_s$  are investigated. A new approach is discussed to estimate  $N_h$  and  $\Delta N$  from the analysis of the dry and wet components of  $N_s$ , which gives better results for certain cases. Results are compared with those obtained from existing linear and exponential models in the literature. The investigation focusses on three layer heights at 65 m, 100 m and 1 km above ground level. Correlation between the components of  $N_s$  with both  $N_h$  and  $\Delta N$  are studied for each atmospheric layer. Where high correlations were found, empirical models are derived from best-fitting curves.

**Index Terms** – Standard atmosphere, radio refractive index, microwave links, refractivity gradient.

## I. INTRODUCTION

Microwave line-of-sight links are designed taking into account the curvature of rays in a stratified atmosphere over the curved earth [1, 2]. Variation of atmospheric parameters such as temperature and relative humidity dominate the vertical refractivity profile. The prevailing meteorological conditions in a specific region determine the extent of refraction. Statistical analysis of refractivity and its vertical profile are essential to the prediction of fading and anomalous propagation, such as sub- or super-refraction and ducting, as well as interference probabilities from reliable surface and upper-air meteorological data. The extent of ray-curvature is determined by the gradient of the refractive index, in N-units, versus height in km from the surface. This is known as the surface lapse rate,  $\Delta N$ . The ITU has defined a reference atmosphere in the form of a negative exponential model and proposed a reference value of -40 N/km for the vertical  $\Delta N$  over the first kilometer in temperate regions [3]. ITU has also published global contour maps for the refractive index at Earth's surface,  $N_s$ , and  $\Delta N$  at specified altitudes [2].

It has been noted that surface meteorological data are widely available and the information about  $N_s$  is more readily available than the upper air refractivity,  $N_h$  [4]. The shortage of upper air data can be attributed to the operational and maintenance cost of radiosonde ascents compared with fixed surface weather stations. Some linear and exponential models [2, 4, 5] have been proposed to predict  $N_h$  at height  $h$  and

vertical  $\Delta N$  from the available  $N_s$  data, where upper air data are not available. It has been noted that most of these relations, in particular for  $\Delta N$ , are derived from the refractivity analysis at the ground and 1 km height. Several refractivity studies are available, e.g. [6-11], while only a few are available for the Arabian Gulf region [12-16], where high incidence of anomalous propagation conditions are reported.

The vertical refractivity profile in the first few hundred meters of the atmosphere, where terrestrial communication systems operate, is important for the analysis of these anomalous phenomena. In this study, the relationships and correlation between dry, wet and net components of  $N_s$  with the corresponding components of either  $N_h$  or  $\Delta N$  are investigated at 65 m, 100 m and 1 km layers above the ground, which are common reference altitudes proposed by ITU [2]. To the best of our knowledge, the curve fitting analysis of the dry and wet components at each layer has not been reported before. Cumulative distributions and scatter diagrams are presented. New relationships are derived from the best fitting curves and compared with existing models.

Long-term radiosonde data recorded at Abu Dhabi, the capital of UAE, from two daily ascents, nominally at 00:00 and 12:00 UT, have been used for the analysis corresponding to 4:00 am and 4:00 pm local time. In certain periods, only one ascent was available per day, usually at 00:00 UT. More details about the radiosonde and the special climate of Arabian Gulf area were recently introduced in [12]. In this paper, the measured refractivity parameters,  $N_s$ ,  $N_h$  and  $\Delta N$ , refer to the values obtained from the surface and radiosonde meteorological measurements, whereas predicted values of  $N_h$  and  $\Delta N$  refer to those calculated from the measured  $N_s$  using the models in sections I.A and I.B. The measured  $\Delta N$  is derived from the measured  $N_s$  and  $N_h$  parameters using the linear model. Root mean square errors, RMSE, and correlation between the measured parameters and between measured and predicted values are presented, using the formulations as defined in MATLAB R2009a.

### A. Refractivity Models

The atmospheric radio refractivity,  $N$ , at any altitude is calculated from the meteorological measurements of total atmospheric pressure (hPa), water vapor pressure (hPa) and absolute temperature (K) using the well-known refractivity formula [2, 5]. The  $N$  parameter consists of two components,  $N_D$  and  $N_W$ , which are often referred to as the dry and wet air contributions to refractivity [5]. The dry component contributes around 60 to 80 % of the overall value [9]. The ITU provide a reference atmosphere for terrestrial paths in the form of a negative exponential model for prediction of  $N_h$  at any height  $h$  (km) above mean sea level [2]:

$$N_h = N_0 \cdot e^{\left(\frac{-h}{h_0}\right)} \quad (\text{N - units}) \quad (1)$$

where  $N_0$  is refractivity extrapolated to sea level and  $h_0$  is the height coefficient which is referred to by ITU as the scale height of the model. The ITU provides global maps of  $N_0$

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(derived using  $h_0 = 9.5$  km) and proposes an average global profile based on  $N_0$  and  $h_0$ , values of 315 N-units and 7.35 km, respectively [2, 5]. It has been noted [2] that  $h_0$  may vary from one region to another.

Other relationships have also been proposed to predict  $N_h$  from the surface data [4, 5]. The following exponential model is further generalized to predict  $N_h$  from  $N_s$  considering “bulk” refractive index structure as opposed to short period random disturbances resulting from a variety of stochastic atmospheric processes [5]:

$$N_h = N_s \cdot e^{\left[-\frac{(h-h_s)}{h_0}\right]} \quad (\text{N - units}) \quad (2)$$

### B. Refractivity Gradient Models

The variation of  $\Delta N$  is a function of climate, season, transient weather conditions across the day, clutter and terrain over the communication path. In the standard atmosphere,  $N_h$  decreases with altitude since the total pressure decreases more rapidly than temperature with height [17]. The vertical  $\Delta N$  usually has a negative value causing the rays to bend towards the earth and to propagate beyond the geometric horizon.  $\Delta N$  can be obtained from two refractivity values,  $N_s$  at the surface,  $h_s$ , and  $N_h$  at an altitude  $h$ , using the linear model, by dividing the refractivity difference ( $N_s - N_h$ ) over  $(h_s - h)$  [5, 12, 18].

A close correlation has been observed between  $N_s$  and  $\Delta N$  “near the ground”, i.e. over the first few kilometers [5]. Several empirical equations have been derived to predict long-term mean values of  $\Delta N$  for the first kilometer layer of atmosphere above the ground from measured  $N_s$  parameter, which are only applicable to average negative gradients close to the surface [4, 5]. If  $N_h$  is not readily available, the refractivity gradient near the Earth’s surface can be predicted either by differentiating (2), [5] or by applying the linear model for the measured  $N_s$  and the predicted  $N_h$ . Other models are also studied to predict the vertical  $\Delta N$  near the ground from the measurements of electromagnetic wave strength and diffraction losses [19, 20]. For higher altitudes, different functions may be fitted as proposed by the three-part reference atmosphere model in Bean and Thayer’s 1959 paper [5], which gives different expressions for the refractivity in the first kilometer, between 1 and 9 km and above 9 km. This has a drawback of introducing discontinuities in the  $\Delta N$  profile. An exponential equation can also be used to directly relate  $\Delta N$  with  $N_s$  as follows [4, 5]:

$$\Delta N = -a \cdot e^{(k \cdot N_s)} \quad (\text{N/km}) \quad (3)$$

where  $a$  and  $k$  are the model coefficients. Another exponential decaying relationship, obtained from curve fitting analysis between  $N_s$  and  $\Delta N$ , was proposed for the first kilometer,  $\Delta N_{1\text{km}}$ , [5, 15] as follows:

$$\Delta N_{1\text{km}} = a \cdot (1 - e^{-bN_s})^c \quad (\text{N/km}) \quad (4)$$

where  $a$ ,  $b$ , and  $c$  are the model coefficients, which are found to be -477.45, 0.00736, and 22.297, respectively, in this study. In general, the values of coefficients of all the models are found to vary from one climate to another. Analyzing data for long periods may also provide more accurate values of the coefficients. In order to extend these relations to other regions around the world, the correlation between long-term measured and predicted refractivity parameters need to be evaluated as well.

## II. ANALYSIS AND RESULTS

Seventeen years of high resolution meteorological data from 1997 till end of October 2013 have been analyzed in this study. Due to low quality or incomplete ascents, data for June 1998, April 2000, November 2005, June 2006 to November 2006 and January 2010 to May 2010 are not available. From December 2006 to December 2008, the data of only one ascent, mostly at 00:00 UT, is available on daily basis. In addition, a small number of abnormal values have been excluded owing to faulty readings from the instrument.

Two approaches, direct and indirect, have been used to predict  $N_h$  and  $\Delta N$  from the measured  $N_s$  values. In the direct approach,  $N_h$  and  $\Delta N$  are directly predicted from measured  $N_s$  using the linear or exponential models. A new indirect approach is proposed by analyzing the dry and wet components of the refractivity parameters using various prediction models. In this indirect approach, the dry and wet components of  $N_h$  or  $\Delta N$  are first estimated from corresponding components of measured  $N_s$  based on the correlations observed between different components. Then, the net values of the predicted parameters,  $\Delta N_{(D+W)}$  and  $N_{h,(D+W)}$ , are computed by summing both dry and wet terms.

### A. $\Delta N$ Analysis at 65 m, 100 m and 1 km Layers

The measured refractivity,  $N$ , has been evaluated from the radiosonde measurements at the ground and at the three specified altitudes. Then, the measured  $\Delta N$  is obtained from the measured  $N_s$  and  $N_h$  for each layer using the linear model. In Figs. 1 and 2, the average seasonal and yearly variations of  $\Delta N$  over the whole period of study are shown for each of the three layers. The mean monthly variations are significant for all the layers, as shown in Fig. 1. The gradient values at the 1 km layer,  $\Delta N_{1\text{km}}$ , vary between -51 and -99 N/km, whereas the gradients span from -68 to -158 N/km and from -68 to -156 N/km, in case of the 100 m layer,  $\Delta N_{0.1\text{km}}$ , and the 65 m layer,  $\Delta N_{0.065\text{km}}$ , respectively. The range of variation is found to be approximately 45 units for  $\Delta N_{1\text{km}}$ , 90 units for  $\Delta N_{0.1\text{km}}$  and 88 units for  $\Delta N_{0.065\text{km}}$ .

Gradient values are lower (i.e. higher in magnitude, but negative) during summer months, May and June, than in winter months, January and December. This can be attributed to the decreasing vapor content and pressure with height and the observed temperature inversions (temperature increasing with height) during the night, particularly in summer. Such  $\Delta N$  trends may explain the frequent interference cases even across national borders, which are commonly experienced by

terrestrial communication systems operating in the Gulf region during the summer months [12]. Occurrence of  $\Delta N$  exceeding  $-100$  N/km is related to the incidence of anomalous propagation [2, 6, 9, 12]. For  $\Delta N_{1\text{km}}$ , no monthly mean is below  $-100$  N/km, whereas  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  fall below this value for most months. In May, the monthly means of  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  even fall below the limit at which ducting phenomenon occurs,  $-157$  N/km. The two peaks of  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  in October, where both monthly mean values of  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  are found to be higher than  $\Delta N_{1\text{km}}$ , can be attributed to a bias in the data due to having only early-morning radiosonde data for this month. In 2007 and 2008, the data for October are only available for at 00:00 UT (4 am local time). In the morning, it is observed that the temperature and the water vapor pressure,  $e$ , often increase with altitude in many cases, in particular within the 65 m and 100 m layers, while  $e$  decreases considerably at 1 km height. The early morning/early evening effect on the gradient is clearly seen in the CDFs shown in Fig. 3. Consequently, the wet components of  $N$  and  $\Delta N$  increase with altitude and  $\Delta N$  attains large positive gradients in both 65 m and 100 m layers, which relates to the incidence of sub-refraction phenomenon [1, 6, 12]. The linear  $\Delta N$  model has the drawback, particularly for the altitudes 100 m and below, that a small difference between the two refractivity values may result in large disagreement in  $\Delta N$  due to the low decimal number in the equation's denominator. Also, the data for October 2006 were not available, which may also affect the overall result.

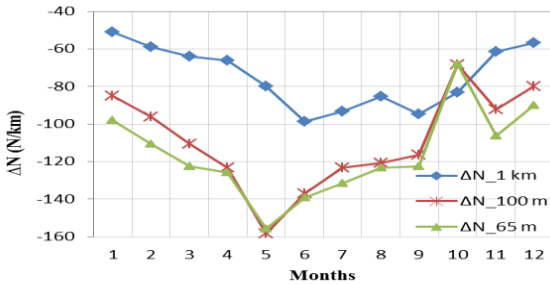


Fig. 1. Mean monthly variations of  $\Delta N$  (1997 to Oct. 2013)

Year to year variation of the mean  $\Delta N$  at 1 km, 100 m and 65 m, with spans of 32, 209 and 298 N-units, respectively, are given in Fig. 2.  $\Delta N_{1\text{km}}$  shows no significant fluctuations, while the values of  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  fluctuate from  $-1.5$  to  $-210$  N/km, and from 31 to  $-267$  N/km, respectively. It can be observed that the mean  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  values decreased for the four years 2002, 2003, 2004 and 2005, with some exceptional values in the years 2003 and 2004. One reason for such trend is the considerable decrement of the water vapor content and pressure with higher altitudes that were observed over the course of these years. This yearly increment could be part of some short-term climate cycle, although a cyclical pattern cannot be reliably inferred from the currently available measurements. By contrast, the mean  $\Delta N$  over each of the three layers showed almost the highest values during 2010, which could be due to the missing five

months data, in particular the months of April and May, which contribute to lower gradient values as shown above in Fig. 1.

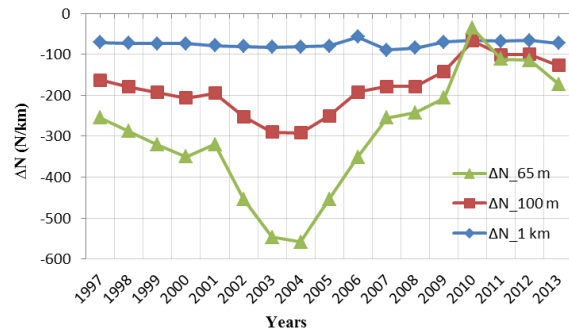


Fig. 2. Mean yearly variations of  $\Delta N$  (1997 to Oct. 2013)

Cumulative distributions of  $\Delta N_{1\text{km}}$ ,  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  for different times of day over the whole period are shown in Fig. 3. The range of  $\Delta N_{0.065\text{km}}$  varies between approximately  $-1947$  and  $1629$  N/km, however only values between  $-1500$  and  $1500$  N/km are displayed for clarity. The long-term mean values of  $\Delta N_{1\text{km}}$ ,  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  are  $-74.8$ ,  $-109.6$  and  $-116.4$  N/km, respectively (well below the  $-40$  of the ITU-R standard atmosphere), whereas the mean values at 00:00 and 12:00 UT are found to be  $-87.9$  and  $-58.8$  N/km for  $\Delta N_{1\text{km}}$ ,  $-138.7$  and  $-74$  N/km for  $\Delta N_{0.1\text{km}}$ , in addition to  $-134.9$  and  $-93.7$  N/km for  $\Delta N_{0.065\text{km}}$ .

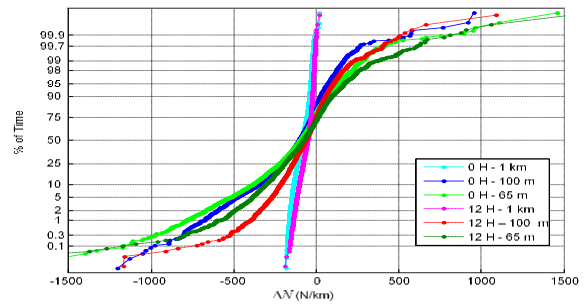


Fig. 3. Hourly Cumulative distributions of  $\Delta N$  (1997 to Oct. 2013)

By comparing the 0 H and 12 H curves for each layer, it can be observed that the gradient values are lower during the morning. Meteorological phenomena following sunset, could be responsible for such a trend [9], where vapor content considerably decreases with height, particularly during the summer season, while in Winter the moisture content may increase with altitude leading to higher positive values of  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065\text{km}}$  than 12:00 UT. Similar results were also reported in a previous study [12], however over a shorter period of years.

### B. Correlation of Refractivity Components

The models introduced in sections I (Parts A and B) for predicting  $N_h$  and  $\Delta N$  parameters from measured  $N_s$ , are examined and the predicted results are compared in terms of RMSE and correlation with the measured  $N_h$  and  $\Delta N$  parameters. Table 1 summarizes the results of RMSE and

correlation coefficients obtained for  $N_h$  and  $\Delta N$  parameters using the exponential models (2) and (4), respectively, which give the best results in most cases, compared with other models. The  $h_o$  value is found to be 3.9 km, 3 km and 2.8 km for 1 km, 100 m and 65 m layers, respectively, for which minimum RMSE values can be obtained in each scenario. The exponential model (4) provides the best correlation and RMSE results for  $\Delta N_{1\text{km}}$ , whereas (2) gives the best results of  $N_h$  at the 65 m and 100 m layers.

TABLE 1: CORRELATION AND RMSE VALUES OF EXISTING PREDICTION MODELS FOR  $N_h$  AND  $\Delta N$  FROM  $N_s$

Layer	$N_h$ & $\Delta N$	Correlation	RMSE
1 km	$N_h$	0.001	30.82
	$\Delta N_{1\text{km}}$	0.86	18.77
100 m	$N_h$	0.87	15.18
	$\Delta N_{0.1\text{km}}$	0.29	151.7
65 m	$N_h$	0.91	12.59
	$\Delta N_{0.065\text{km}}$	0.24	196.2

No correlation has been found between  $N_h$  and  $N_s$  for the 1 km layer, while strong correlation is observed for the other two layers, 100 m and 65 m. On the other hand, the correlation between  $\Delta N_{1\text{km}}$  and  $N_s$  exceeds 0.85, whereas it is found to be poor in case of the 65 m and 100 m layers. In addition, the correlation between the dry, wet and net components of measured  $N_s$  and the corresponding components of the measured  $N_h$  and  $\Delta N$  are also investigated for each of the three layers. Table 2 provides the results of correlation matrix for all the scenarios. The dry component of  $N_s$ ,  $N_{s\_D}$ , is in good correlation with the dry component of  $N_h$ ,  $N_{h\_D}$ , at all altitudes,  $N_{1\text{km\_D}}$ ,  $N_{0.1\text{km\_D}}$  and  $N_{0.065\text{km\_D}}$ , where the maximum correlation is observed within the 65 m layer. The  $N_{s\_D}$  is found to be much less correlated with the dry components of  $\Delta N$  in the three layers;  $\Delta N_{1\text{km\_D}}$ ,  $\Delta N_{0.1\text{km\_D}}$  and  $\Delta N_{0.065\text{km\_D}}$ . The wet component of  $N_s$ ,  $N_{s\_W}$ , is well correlated with the wet component of  $N_h$  at the 100 m and 65 m altitudes,  $N_{0.1\text{km\_W}}$  and  $N_{0.065\text{km\_W}}$ , while it is found to be only correlated with the wet component of  $\Delta N$  at the 1 km layer,  $\Delta N_{1\text{km\_W}}$ .

TABLE 2: CORRELATION MATRIX OF REFRACTIVITY COMPONENTS AT 1 km, 100 m AND 65 m LAYERS

	$N_s$	$N_{s\_D}$	$N_{s\_W}$
$N_{1\text{km}}$	0.001		
$N_{1\text{km\_D}}$		0.84	
$N_{1\text{km\_W}}$			0.15
$N_{0.1\text{km}}$	0.874		
$N_{0.1\text{km\_D}}$		0.96	
$N_{0.1\text{km\_W}}$			0.89
$N_{0.065\text{km}}$	0.91		
$N_{0.065\text{km\_D}}$		0.97	
$N_{0.065\text{km\_W}}$			0.92
$\Delta N_{1\text{km}}$	-0.85		
$\Delta N_{1\text{km\_D}}$		-0.56	
$\Delta N_{1\text{km\_W}}$			-0.86
$\Delta N_{0.1\text{km}}$	-0.30		
$\Delta N_{0.1\text{km\_D}}$		-0.55	
$\Delta N_{0.1\text{km\_W}}$			-0.29
$\Delta N_{0.065\text{km}}$	-0.26		
$\Delta N_{0.065\text{km\_D}}$		-0.54	

$\Delta N_{0.065\text{km\_W}}$			-0.25
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In general, no correlation could be obtained between either dry or wet components of  $N_s$ , and  $\Delta N$  at the 100 m and 65 m layers. It is also noted that the correlation between the net parameters follows the correlation between their wet components. These observations seem to be reasonable since the wet term of refractivity is proportional to the water vapor content that varies significantly across these layers, in particular within the layers close to the ground, and gets more stable at around 1 km height, while the dry term is proportional to the atmospheric pressure and inversely proportional to the dry temperature, which show less variation over all atmospheric layers within the first kilometer.

The slope of the vertical refractivity curve at 1 km, which refers to  $\Delta N_{1\text{km}}$ , is correlated with  $N_s$  since the variation of  $N_{1\text{km}}$  is very small compared with  $N_{0.1\text{km}}$  and  $N_{0.065\text{km}}$ , which are directly correlated with  $N_s$ . No correlation is observed between  $N_s$  and gradients at the layers close to the ground,  $\Delta N_{0.1\text{km}}$  and  $\Delta N_{0.065}$ . Fig. 4 describes this phenomenon, where at 1 km height the refractivity value does not change significantly with the variations in  $N_s$ , while  $N_{0.1\text{km}}$  and  $N_{0.065\text{km}}$  vary significantly with  $N_s$ . The slope,  $\Delta N$ , is only correlated with  $N_s$  in case of the 1 km layer,  $\Delta N_{1\text{km}}$ , since  $N_{1\text{km}}$  is assumed to have a stable value while  $N_s$  varies between the states S1 and S2.

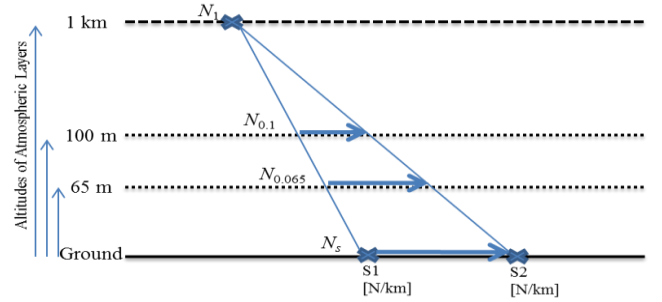


Fig. 4. Description of Correlation Between  $N_s$ ,  $N_h$  and  $\Delta N$

### C. Curve Fitting Analysis and Algorithms

The scatter diagrams of all measured refractivity parameters and components are studied. Some figures of the correlated parameters and components are provided and empirical algorithms are derived from the best fitting curves. All relationships are evaluated based on the determination coefficients, correlation of the obtained results with the measured data and RMSE values.

As presented in Table 2, the correlation between  $N_s$  and  $\Delta N_{1\text{km}}$  is dominated by the wet components of the two parameters,  $N_{s\_W}$  and  $\Delta N_{1\text{km\_W}}$ , while  $N_{s\_D}$  is found to be correlated with  $N_{1\text{km\_D}}$  rather than  $\Delta N_{1\text{km\_D}}$ .

The scatter diagram between the wet components,  $N_{s\_W}$  and  $\Delta N_{1\text{km\_W}}$ , is shown in Fig. 5. A third order polynomial relationship to predict  $\Delta N_{1\text{km\_W}}$  is obtained from the curve fitting analysis. The dry component of  $\Delta N_{1\text{km\_D}}$  is calculated

using the linear model from the predicted  $N_{1km\_D}$  and measured  $N_{s\_D}$ .  $N_{1km\_D}$  is predicted from measured  $N_{s\_D}$  using equation (2). This new indirect approach for predicting  $\Delta N_{1km(D+W)}$  has less RMSE value than the direct approach for predicting  $\Delta N_{1km}$  from measured  $N_s$  using the linear model, as shown in Table 3.

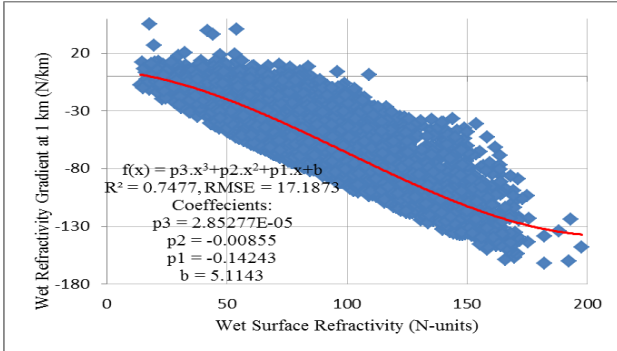


Fig. 5. Correlation between  $N_{s\_w}$  and  $\Delta N_{1km\_w}$

TABLE 3: COMPARISON OF TWO APPROACHES FOR  $\Delta N_{1km}$  PREDICTION

	Correlation	RMSE
Direct Approach: $\Delta N_{1km}$ from measured $N_s$	0.85	30.8118
Indirect Approach: $\Delta N_{1km(D+W)}$ from Dry and Wet Components Analysis	0.85	19.3338

Multiple scatter diagrams are drawn for the dry, wet and net components of the measured  $N_h$  and  $\Delta N$  against the corresponding measured  $N_s$  components at 65 m and 100 m atmospheric layers. Good correlation is observed between  $N_h$  and  $N_s$  components, while it is found to be poor between  $\Delta N$  and  $N_s$  with large RMSE values obtained regardless of the approach or the prediction model to be used. This can be attributed to the sensitivity of  $\Delta N$  to any small variation in the values of refractivity at these low altitudes.  $N_h$  has been predicted using the exponential model (2) considering both the direct and indirect approaches at the 65 m,  $N_{0.065km}$ , and 100 m,  $N_{0.1km}$ , layers. Due to the similarity of the  $N_h$  results at the 65 m and 100 m layers, the available data sets of these two layers are combined,  $N_{0.065\&0.1km}$ , to develop a single model for the atmospheric layers below 100 m altitude from the ground. The correlation and RMSE values of the measured and predicted  $N_h$ ,  $N_{h\_D}$ ,  $N_{h\_W}$  and  $N_{h\_D+W}$ , are compared for each of the three data sets at 65 m, 100 m and their combined set. For all scenarios, RMSE results for  $N_{h\_D+W}$  using the indirect approach are better than the results of  $N_h$  obtained directly from the measured  $N_s$ , while correlation results are almost the same.

The scatter diagram of  $N_h$  against  $N_s$  is given in Fig. 6. Two exponential and third order polynomial relationships are obtained from the best fitting curves, which provide marginally better results in comparison with the other models. Both models have very similar results with marginal improvement for the polynomial model. However, the result from the polynomial is highly sensitive to the precision of the coefficients. The RMSE and correlation results obtained for

the prediction of  $N_h$  from both direct and indirect approaches are similar. The following exponential model can be used for direct prediction of  $N_h$  below 100 m above the ground, where the values of the coefficients  $a$  and  $b$  are found to be 135.8 and 0.002609, respectively, for the area under study:

$$N_{0.065\&0.1km} = a \cdot e^{(b \cdot N_s)} \quad (N - \text{units}) \quad (5)$$

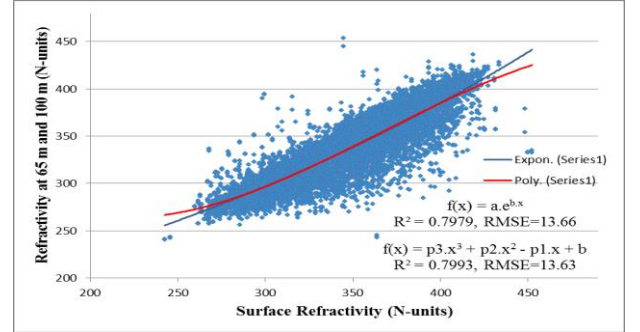


Fig. 6. Correlation between  $N_s$  and  $N_{0.065\&0.1km}$

### III. CONCLUSIONS

17 years of local radiosonde data from UAE were analysed to obtain the vertical refractivity profile for three critical atmospheric layers within the first kilometer above the ground. The correlation between  $N_s$  and either  $N_h$  or  $\Delta N$  was found to depend predominantly on the wet components of these parameters.

For estimating  $\Delta N$  at the three atmospheric layers, it was observed that the linear model resulted in somewhat lower RMSE values than the exponential one.

Based on the reduced RMSE, it is recommended to use the indirect approach to estimate  $N_h$  and  $\Delta N$  from the analysis of dry and wet refractivity components, in particular at the 1 km layer. Marginal improvement was achieved for the 65 m and 100 m layers when  $N_h$  was predicted using the exponential model (2) based on the indirect approach. Such multi-steps analysis may lead to slightly lower correlation, when compared with the measured data, than using the direct relations.

Although the use of more than one model to predict the refractivity at different atmospheric layers may introduce some discontinuities in its vertical profile, the RMSE values of the predicted  $N_h$  or  $\Delta N$  were found to be reduced while the correlation between the measured and predicted values was marginally improved for certain parameters.

Third- and fourth-order polynomial models showed marginal improvements in terms of RMSE and correlation values for the prediction of  $N_h$  and  $\Delta N$  parameters over the other models. However, it was noted that the results were very sensitive to the precision of the high order coefficients.

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