

# **The Kihara Potential Function Parameters of Methane, Ethane, Propane, and i-Butane: The Effects on Clathrate Hydrate Structure Determination**

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## ABSTRACT

Gas hydrates, or clathrate hydrates, are solid crystalline compounds, which are mixtures of water and gas. Prediction of hydrate dissociation conditions of natural gases is important in separation processes, gas storage industries, and in preventing blockage of gas transmission pipelines. In this study, initially, the different sets of the Kihara Potential Function Parameters, KPFP, reported in the literature were used to predict the equilibrium dissociation conditions of available experimental data for methane, ethane, propane and i-butane hydrates and mixtures of these four compounds. In most cases, however, based on these sets of KPFP, the hydrate structure cannot be predicted correctly. Consequently due to incorrect estimation of the hydrate structure, especially for natural gas mixture, the predicted equilibrium conditions are incorrect. For overcoming this fault and using a genetic algorithm, a new set of KPFP were optimized based on the new definition of the objective function and considering of structurea . The results show good compatibility with experimental data, both in the prediction of hydrate dissociation conditions and hydrate structures.

**Keywords:** Gas hydrate; Clathrate hydrate; Kihara Potential Function Parameters; Genetic algorithm; Model; Optimization.

## 1. INTRODUCTION

Natural gas hydrate, or Clathrate hydrate, is a solid crystalline compound that consists of water and gas. Water molecules trap the guest molecules (gas) in the cavities generated by the hydrogen bonds between the host water molecules. Guest molecules are kept in the cavities due to the van der Waals forces, meaning that there are no chemical bonds. Guest molecules are usually small hydrocarbons such as methane, ethane, etc. Gas hydrates may cause some plugging problems in pipelines, vessels, valves and in general devices, especially at high pressure and low temperatures. This plugging may cause irreversible damages, such as an explosion in oil and gas industries. There is a thought that the cause of the Deepwater Horizon oil spill in the Gulf of Mexico in 2010 was the formation of hydrate.

For the first time, Muller and Stackleberg[1] studied the properties of the hydrate structures using X-ray. According to Muller and Stackelberg's experiments, two types of hydrate crystalline structures were identified known as structure I, sI, and structure II, sII hydrates. In 1987, Ripmeester et al.[2] found out that the structure H of gas hydrates were able to encage larger molecules. Light hydrocarbons and natural gas mixtures, usually, form Structure I or II.

The first step in the estimation of hydrate formation temperatures, especially for natural gas hydrates, is to determine which structure is formed. In the absence of the experimental data on the structure, commonly, the hydrate formation conditions for two structures are determined and the stable gas hydrate structure is the one in which its formation temperature (and/or pressure) is higher (and/or lower). Based on these criteria, some case , however, the predicted *hydrate structure* is not in accordance with experimental data and consequently, the predicted formation conditions are not in agreement with experimental values. Therefore, it is required to find a way which is able to predict the gas hydrate structure correctly.

Different thermodynamic models were proposed to predict the hydrate equilibrium conditions. At first, van der Waals and Platteeuw[3] (vdW-P) presented a statistical model for estimation of water chemical potential in the hydrate phase and using the Lenard-Jones potential function to calculate the Langmuir constant. McCoy and Sinanoğlu[4] suggested using the KPFP for larger and non-spherical molecules instead of the Lenard-Jones potential function. Parrish and Prausnitz[5] extended the vdW-P solid solution theory for gas mixtures and also the component fugacity was used instead of partial pressure of the components. They also proposed a relation for estimation of water chemical potential in the liquid phase to predict the hydrate equilibrium conditions. They also estimated KPFP for 15 different gases. Holder and Hand[6] in 1982, reported hydrate dissociation pressure for methane, ethane, propane, and their mixtures. They also optimized KPFP using experimental dissociation pressure. They reported that mixtures of these gases can form either sI or sII hydrates under different thermodynamic conditions. Barkan and Sheinin[7] determined the KPFP for several gases using the data of the second-order virial coefficient and transport properties such as viscosity. Avlonitis[8] presented a method for deriving KPFP using second-order virial coefficients compared with the experimental data for nearly perfect gases, i.e., xenon, krypton, methane, ethane, propane, butane, nitrogen, carbon dioxide and hydrogen sulfide. Tohidi[9] using two different methods, reported the KPFP for eight different gases. In the first method, based on the cage occupancy, hydration number of xenon, and dissociation pressure experimental data the KPFP for xenon was found. Then, the xenon was selected as the key component and the KPFP of C1, C2 and C3 were calculated using experimental data on their binary mixtures with xenon. In the second method, the KPFP were derived from the intersections of the plot of  $\sigma$  as a function of  $\varepsilon/k$  for different structures[9]. Hendriks et al.[10] found that when ethane is present in binary gas mixtures, for example, methane + ethane, a structure transition may be seen especially when the other hydrate former can occupy the smaller cages. Sloan[11]

optimized KPFP for several gases using experimental data. Subramanian et al.[12, 13] reported that there would be a structural transition from sI to sII, when mixtures of methane and ethane form hydrates at 274.2 K and 0.72 and 0.75 mol% of methane. Ballard and Sloan[14] generated the phase diagram of different binary and ternary gas mixtures at 277.6 K by optimizing the system Gibbs free energy. Later, they reported new KPFP based on experimental data and using vdW-P solid solution theory[15]. The results showed that there are multiple phase transition points as a function of temperature when methane composition is between 0.7 to 0.75 mole percent. In 2007, Sloan and Koh[16] reported KPFP for many gases.

During these years, several KPFP are reported using different methods. Applying each set of reported KPFP, different structures can be predicted for a unique gas mixture. An incorrect prediction of the structure causes an incorrect prediction of the hydrate equilibrium conditions. In this work, first, the KPFP reported in the literature are compared to predict both stable hydrate structure and also gas hydrate dissociation temperature based on this structure. Then, the results of the optimized KPFP for methane, ethane, propane, i-butane, and their mixtures are presented and found highly accurate.

## 2. THERMODYNAMIC MODEL

The equilibrium state occurs when the chemical potentials are equal in these two phases[16]:

$$\Delta\mu_w^H = \Delta\mu_w^L \quad (1)$$

where  $\Delta\mu_w$  is the difference between water chemical potential in unoccupied and occupied hydrate lattice, and superscripts  $H$  and  $L$  refer to hydrate and liquid phases, respectively.

The right hand side of Eq. (1) could be estimated by the following expression given by Holder et al.[17]

$$\frac{\Delta\mu_w^L}{RT} = \frac{\Delta\mu_w^\circ}{RT_0} - \int_{T_0}^T \frac{\Delta h_w^L}{RT^2} dT + \int_0^P \frac{\Delta v_w^L}{RT} dP + \ln a_w \quad (2)$$

where  $\Delta h_w^L$  is the difference between water enthalpy in unoccupied hydrate lattice and liquid water which is defined as follows:

$$\Delta h_w^L = \Delta h_w^\circ + \int_{T_0}^T \Delta C_{pw}^L dT \quad (3)$$

$$\Delta C_{pw}^L = E + F(T - 273.15) \quad (4)$$

where  $\Delta C_{pw}^L$  is the difference between water heat capacity in the unoccupied hydrate lattice and liquid water. The parameters  $E$  and  $F$  are reported in Table 1.  $\Delta\mu_w^\circ$ ,  $\Delta h_w^\circ$ , and  $\Delta v_w^l$  are differences between the water chemical potential and enthalpy in unoccupied hydrate lattice and liquid water at the reference temperature, and water molar volume in unoccupied hydrate lattice and a liquid water an respectively. These values are reported in Table 2. Parameters  $P$ ,  $a_w$ ,  $T_0$  and  $R$  are system pressure, water activity, the reference temperature (273.15 K), and the universal gas constant, respectively.

**Table 1**

**Table 2**

In the absence of any additive such as salts or alcohols in the aqueous phase, the water activity,  $a_w$ , can be estimated as follows:

$$a_w = 1 - \sum_{i=1}^N x_i^{guest} \quad (5)$$

where solubility of guest compounds in water phase,  $x_i^{guest}$ , is calculated using the following equation[18]:

$$x_i^{guest} = \frac{f_i^v}{H_i(T) \exp\left(\frac{Pv}{RT}\right)} \quad (6)$$

where  $f_i^v$ , is the fugacity of the guest molecules in the gas phase which is calculated using the Peng-Robinson equation of state[19] (PR EoS) in this work and the values of  $T_C$ ,  $P_C$  and  $\omega$  are reported in Table 3[20].  $H$  is the Henry constant of each guest molecule,  $v$  is the partial molar volume of each guest molecule and  $T$  is the system temperature. Henry constant of each guest molecule can be calculated using the following equation[21]:

$$-\ln\left(\frac{H_i(T)}{101325}\right) = H_i^{[1]} + \frac{H_i^{[2]}}{T} + H_i^{[3]} \ln(T) + H_i^{[4]}T \quad (7)$$

where,  $H_i^{[1]}$ ,  $H_i^{[2]}$ ,  $H_i^{[3]}$ , and  $H_i^{[4]}$  are reported in Table 4.

**Table 4**

The left hand side of Eq. (1),  $\Delta\mu_w^H$ , can be estimated using the solid solution theory of vdW-P[3]:

$$\Delta\mu_w^H = -RT \sum_{m=1}^2 v'_m \ln\left(1 - \sum_j^{nc} \theta_{mj}\right) \quad (8)$$

where  $v'_m$ , is the number of cavities type  $m$  to the number of water molecules in a hydrate unit cell,  $\theta_{mj}$  is the fraction of the type  $m$  cavities occupied by the  $j$  type guest molecules which is described in the following equation:

$$\theta_{mj} = C_{mj} f_j / \left( 1 + \sum_j^{nc} C_{mj} f_j \right) \quad (9)$$

where  $C_{mj}$  is the Langmuir constant which is calculated using the relations given by McKoy and Sinanoglu[4]:

$$C_{mj} = \frac{4\pi}{kT} \int_0^\infty \exp\left[-\frac{\omega'(r)}{kT}\right] r^2 dr \quad (10)$$

$$\omega'(r) = 2z\varepsilon \left[ \frac{\sigma^{12}}{R'^{11}r} \left( \delta^{10} + \frac{a}{R'} \delta^{11} \right) - \frac{\sigma^6}{R'^5 r} \left( \delta^4 + \frac{a}{R'} \delta^5 \right) \right] \quad (11)$$

$$\delta^N = \frac{1}{N} \left( 1 - \frac{r}{R'} - \frac{a}{R'} \right)^{-N} - \left( 1 + \frac{r}{R'} - \frac{a}{R'} \right)^{-N} \quad (12)$$

where  $k$  is the Boltzmann's constant and  $\omega'(r)$  is the cell potential. The Kihara potential parameters  $a$ ,  $\sigma$  and  $\varepsilon$  are the hard core radius, the collision diameter and the depth of energy well, respectively,  $N$  is a parameter ( $N=4, 5, 10, 11$ ),  $z$ ,  $r$  and  $R'$  are respectively the coordinate number, the radius and the mean cavity radius.

Finally, by combining Eq. (2) and (8), the following equation will be obtained which predicts the hydrate equilibrium condition,  $T$  and  $P$ :

$$\sum_{m=1}^2 v'_m \ln \left( 1 + \sum_{j=1}^{nc} C_{mj} f_j \right) = \frac{\Delta\mu_w^\circ}{RT^\circ} - \int_{T^\circ}^T \frac{\Delta h_w^l}{RT^2} dT + \int_0^P \frac{\Delta v_w^l}{RT} dP - \ln a_w \quad (13)$$

Different sets of KPFP,  $a$ ,  $\sigma$ ,  $\varepsilon$ , are reported in the literature. Table 5 shows some of the most popular sets for methane, ethane, propane and i-butane, the main constituents of natural gas.

**Table 5**



Based on Eq. (13), different sets of Kihara potential parameters may lead to different values of hydrate equilibrium conditions and consequently different structures.

It should be noted that the determination of hydrate structures, especially for gas mixtures, is based on the fact that at a given pressure, the temperatures for the two structures, I and II, are calculated and the structure corresponds to the highest temperature is considered as the stable structure. In some cases, and based on the above criteria, the predicted structure is incorrect, especially for natural gas systems. Consequently, the predicted dissociation condition is also incorrect. In other words, the predicted dissociation temperature for the more stable structure is very different from the experimental values and this shortcoming is due to the inaccuracy of the KPFP in determining the correct conditions.

To overcome these two shortcomings, in this work, the new KPFP are optimized using the genetic algorithm which is described in the following section. This set, by comparison with the literature hydrate data, predicts the hydrate phase boundary and structure precisely.

#### **a. PARAMETERS OPTIMIZATION**

Genetic algorithm (GA) was first introduced by Holland[22]. GA is a suitable method for solving problems associated with search and optimization. This algorithm works with a population of "unique members" in which each member has a defined fitness. Members with higher degrees of fitness have more opportunities for "fertility" through "blending" with other members of the population. The new members inherit some of their parent's traits. Members' traits distribute in their populations and the members change due to multiple reproduction and generation of sequential populations. If the algorithm is well-designed, the population will converge to an optimal solution to the problem. The genetic algorithm begins with the

definition of optimization parameters and ends once the convergence condition is satisfied. The adjustable parameters are determined as follows:

**a) Chromosome (Optimization parameters) and cost function**

Optimization parameters and the cost function must be defined in this algorithm. In the culture of genetics algorithm, a chromosome is a set of optimization parameters as defined in Eq. (14):

$$\text{Chromosome} = [\alpha, \sigma, \varepsilon] \quad (14)$$

$\alpha$ ,  $\sigma$ , and  $\varepsilon$  are optimization parameters that have real numeric values which are described in section 2.1.b.

In optimization problems, the aim is to minimize the cost function known as the objective function ( $OF$ ). In this work,  $OF$  is calculated using Eq. (15):

$$OF = \Delta er + \Delta er_{\text{total}} \quad (15)$$

For methane and ethane:

$$\Delta er = \sum_{i=1}^N |T_i^{\text{Exp.}} - T_i^{\text{sI}}| \quad (16)$$

For propane and isobutane:

$$\Delta er = \sum_{i=1}^N |T_i^{\text{Exp.}} - T_i^{\text{sII}}| \quad (17)$$

and

$$\Delta er_{\text{total}} = \begin{cases} \sum_{i=1}^N |T_i^{\text{Exp.}} - T_i^{\text{sI}}| & \text{if } T_{\text{sI}} > T_{\text{sII}} \\ \sum_{i=1}^N |T_i^{\text{Exp.}} - T_i^{\text{sII}}| & \text{if } T_{\text{sII}} > T_{\text{sI}} \end{cases} \quad (18)$$

$\Delta er$  is described differently for methane, ethane, propane and isobutane since they form sI and sII, respectively.  $\Delta er_{\text{total}}$  is added to the  $OF$ , to not let the optimization process go toward the prediction of the wrong structure.

### **b) Initial population**

The initial matrix is created using Eq. (19) noting the allowed range of each parameter:

$$IPOP = (hi - low) \times \text{random}\{N_{ipop}, N_{par}\} + low \quad (19)$$

$N_{ipop}$ : The number of the initial population

$N_{par}$ : The number of optimization parameters

$\text{random}\{N_{ipop}, N_{par}\}$ : A function that generates random numbers between zero and one

$hi$ : The maximum value in the allowed range of each parameter

$low$ : The minimum value in the allowed range of each parameter

### **c) Tournament Selection**

The Tournament selection[23] method is used to select parents. The choices of parents are based on an approach that even the weakest chromosomes have a luck to be selected. This approach leads the optimization to find global answers.

### **d) Mating**

Mating is the process of producing two new chromosomes from each selected parent. One of the most common methods of mating is the crossover methods[24]. One or more locations in each chromosome are selected as cutoff-points. By choosing a random point as a cutoff point in the chromosome, the parameters in further that point will be exchanged between each parent [25]. The cutoff-point will be calculated using the BLX- $\alpha$  method[26].

### **e) Mutation**

The mutation rate is calculated using an exponential function in the form of Eq. (20):

$$\mu = \mu_o e^{-Counter} \quad (20)$$

$\mu_o$  is a primary mutation rate, and *counter* is the number of repetitions performed.

The continuous genetic algorithm works well when the mutation rate is between 1 to 20 percent. If the mutation rate is of over 20 percent, a bunch of good parameters will be lost.

#### f) Termination

The optimization process will be terminated when the main loop is repeated 100 times. Finally, the chromosome with the highest fitness value will be considered as the optimum value.

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### 3. RESULT AND DISCUSSION

The literature hydrate dissociation temperatures for methane, ethane, propane and i-butane are reported in Table 6. A complete set of experimental data is obtained from the literature and 856 data points were found. Using different sets of KPFP reported in Table 5, the average absolute deviation, *AAD*, for hydrate dissociation temperatures are reported in Table 7.

As can be seen, KPFP reported by Holder and Hand[6], Barkan and Sheinin[7], and Avlonitis[8] could not predict the hydrate formation condition precisely.

#### Table 6

#### Table 7

The KPFP reported in Table 5 are also used to predict hydrate formation conditions of different mixtures of methane, ethane, propane, and i-butane. The mixtures, depend on their compositions, may form either sI or sII. The hydrate formation structure for each set of data is determined using the thermodynamic model described in section 2. The stable structure is the one with higher hydrate formation temperature and/or lower pressure. Holder and Hand[6], reported experimental hydrate formation data for mixtures of ethane and propane. They also claimed that each set of data will form different structures when thermodynamic conditions are changed. For example, a structural transition is observed for a mixture of 74% mol ethane and

26% mol propane. To justify their statement, all the reported KPFP in Table 5 are applied to that set of data and the results are depicted in Fig. 1.

### Figure 1

A closer view of Fig. 1 reveals that some of the reported KPFP could not predict the correct structure. The *AAD* of calculated hydrate formation temperature using the reported KPFP by Parish and Prausnitz[5], Holder and Hand[6], Barkan and Sheinin[7], Avlonitis[8], Tohidi[9], Sloan[11], Sloan and Koh[16], and Hydrafact<sup>1</sup> Software. were 4.69, 14.82, 9.47, 2.67, 0.18, 5.29, 8.07 and 0.15 K, respectively.

Figures 2 and 3 are also shown the equilibrium conditions for 90.4% mol methane and 9.6% mol ethane mixture, and 96.5% mol methane and 3.5% mol propane mixture, respectively.

### Figure 2

### Figure 3

As shown in the Fig.2, some of the reported KPFP predict the structure I and some the structure II as the correct structure. According to Subramanian et al.[12], the structure II of hydrate is the correct structure for this system. Hence only the KPFP reported by Tohidi[9] have predicted the correct structure, which has the *AAD* of calculated hydrate formation temperature 1.02 K.

According to Figure 3, the parameters reported by Kihara by Parish and Prausnitz[5], Tohidi[9], Sloan[11], Sloan and Koh[16],and Hydrafact Software predicted the correct structure for this gas mixture, but some of them have high *AAD*.

Reported *AADs* are high in some cases due to the prediction of wrong structures and/or low accuracy of the reported KPFP in prediction of equilibrium conditions. To overcome this

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<sup>1</sup> HydraFlash (version 3.6) supplied by Hydrafact Ltd. (UK).

challenge, in this work, new KPFP are optimized for pure gases (methane, ethane, propane and, isobutane) using GA as described in section 2.1. Experimental hydrate formation condition data of pure gases are given in Table 6. Forty percent of the reported experimental data are used in the optimization process. The new optimized KPFP are reported in Table 8.

#### **Table 8**

The new optimized KPFP are used in the thermodynamic model and then the hydrate formation condition of pure gases and some of their mixtures are calculated and depicted in Fig. 4. The *AAD* is reported in Table 7.

#### **Figure 4**

As can be seen in Table 7, the results of hydrate formation conditions of pure gases and their mixtures using the optimized KPFP showed that the new parameters are more accurate than the former reported parameters except for pure propane and mixtures of ethane and propane.

## **4. CONCLUSION**

In this paper, the van der Waals Platteeuw solid solution theory along with the Peng-Robinson equation of state using different KPFP are applied to predict the hydrate formation conditions of pure methane, ethane, propane, i-butane and also their mixtures. The *AAD* of each set of experimental data using different KPFP are reported. The reported *AADs* are high in some cases due to the prediction of wrong structures and/ or low accuracy of the reported KPFP. Therefore, new KPFP are optimized for pure methane, ethane, propane and i-butane hydrate experimental data using GA algorithm in Matlab. Then, the optimized KPFP are also used for gas mixtures. The reported results showed that KPFP are highly accurate and also are capable of predicting the correct hydrate structures.

## Nomenclature

### *Roman Characters:*

$a$	Hard core radius, Å
$a_w$	Water activity
$AAD$	Average Absolute Deviation, K
$C_{mj}$	Langmuir constant for component $j$ in cavity $m$ , kPa <sup>-1</sup>
$\Delta C'_{pw}$	Difference in heat capacity between hydrate lattice and liquid water, J/mol/K
$f_i^v$	The fugacity of the guest molecules in the gas phase
$\Delta h_w^l$	Difference in enthalpy between hydrate lattice and liquid water, J/mol
$\Delta h_w^\circ$	Difference in enthalpy between hydrate lattice and liquid water in 273.15 K, J/mol
$H_i$	Henry constant for component $i$ , Pa <sup>-1</sup>
$IPOP$	Initial population
$k$	Boltzmann's constant, J/K
$N_{ipop}$	The number of initial population
$N_{par}$	The number of optimization parameters
$P$	Pressure, kPa
$P_c$	Critical pressure, kPa
$r$	Radius cavity radius, Å
$R$	Universal gas constant, J/mol/K
$R'$	Mean cavity radius

$T$	Temperature, K
$T_c$	Critical temperature, K
$z$	Coordinate number

*Greek Characters:*

$\varepsilon$	Depth of energy well, J
$\sigma$	Collision diameter, Å
$\nu'_m$	Number of cavities type $m$ to the number of water molecules in a hydrate lattice
$\nu$	Partial molar volume of each guest molecule, cm <sup>3</sup> /mol
$\Delta \nu_w^I$	Difference in water molar volume between an empty hydrate lattice and liquid phase, cc/mol
$\Delta \mu_w^H$	Difference in Water chemical potential between an empty hydrate lattice and hydrate, J/mol
$\Delta \mu_w^L$	Difference in Water chemical potential between an empty hydrate lattice and liquid phase, J/mol
$\Delta \mu_w^\circ$	Difference in water chemical potential between hydrate lattice and liquid water at 273.15 K, J/mol
$\omega$	Acentric factor
$\omega'(r)$	Cell potential

*Superscripts and Subscripts:*

$0$	Reference state
<i>Calc.</i>	Calculated
<i>Counter</i>	Number of repetitions performed
<i>Exp.</i>	Experiment



<i>H</i>	Hydrate phase
<i>L</i>	Liquid water
<i>w</i>	Water
<i>v</i>	vapor

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**Table1.**  $E$  and  $F$  values used by other researchers to calculate the specific heat capacity by equation 4.

$E$ (J/mol/K)	$F$ (J/mol/K)	Ref.
-38.1162	0.1406	Parrish and Prausnitz[5]
-38.1162	0.1406	Holder and Hand[6]
-38.1200	0.1410	Barkan and Sheinin[7]
-37.8850	0.1770	Avlonitis[8]
-37.8850	0.1770	Tohidi[9]
-38.1200	0.1410	Sloan[11]
-38.1200	0.1410	Sloan and Koh[16]
-38.1200	0.1410	Values used in this work



**Table 2.** The thermodynamic properties used by other researchers to calculate the difference in the chemical potential of water in the aqueous phase.

Structure I			Structure II			Ref.
$\Delta v_w^l$ (cc/mol)	$\Delta h_w^\circ$ (J/mol)	$\Delta \mu_w^\circ$ (J/mol)	$\Delta v_w^l$ (cc/mol)	$\Delta h_w^\circ$ (J/mol)	$\Delta \mu_w^\circ$ (J/mol)	
4.6	-4858.0	1264.0	5	-5202.0	882.80	Parrish and Prausnitz[5]
4.6	-5627.0	1155.0	5	-6008.0	883.00	Holder and Hand[6]
4.6	-4616.0	1297.0	5	-5226.0	975.00	Barkan and Sheinin[7]
4.6	-4622.0	1297.0	5	-4986.0	937.00	Avlonitis[8]
4.6	-4622.0	1297.0	5	-4986.0	937.00	Tohidi[9]
4.6	-4622.0	1263.0	5	-4986.0	883.80	Sloan[11]
4.6	-4858.9	1263.6	5	-5202.2	882.80	Sloan and Koh[16]
4.6	-4858.9	1263.6	5	-5202.2	882.80	This work

$\Delta v_w^l$ : Difference in water molar volume between an empty hydrate lattice and liquid phase, cc/mol.  $\Delta h_w^\circ$ : Difference in water enthalpy between hydrate lattice and liquid water in 273.15 K, J/mol.  $\Delta \mu_w^\circ$ : Difference in water chemical potential between hydrate lattice and liquid water in 273.15 K, J/mol

**Table 3.**  $T_C$ ,  $P_C$  and  $\omega$  of the hydrate formers used in PR EoS [20].

Compound	$T_C$ (K)	$P_C$ (MPa)	$\omega$
C1	190.81	4.595	0.011
C2	305.3	4.872	0.099
C3	369.8	4.301	0.152
iC4	408.14	3.648	0.177

**Table 4.** Henry Law Constants in equation 7 [21].

Compound	$H_i^{[1]}$	$H_i^{[2]}$	$H_i^{[3]}$	$H_i^{[4]}$
C1	-183.7860	9112.582	25.0405	-0.00015
C2	-268.4410	13369.400	37.5561	-0.00230
C3	-316.4900	15922.700	44.3285	0.00000
iC4	96.1158	-2472.570	-17.3680	0.00000

**Table 5.** Kihara potential function parameters of gas-water interaction.

Compound	$a$ (Å)	$\sigma$ (Å)	$\frac{\epsilon}{k}$ (K)	Ref.
C <sub>1</sub>	0.3000	3.2398	153.170	Parrish and Prausnitz[5]
C <sub>2</sub>	0.4000	3.3180	174.970	
C <sub>3</sub>	0.6800	3.3030	200.940	
iC <sub>4</sub>	0.8000	3.1244	220.52	
C <sub>1</sub>	0.3330	3.1880	150.730	Holder and Hand[6]
C <sub>2</sub>	0.5580	3.1550	174.770	
C <sub>3</sub>	0.6460	3.3200	209.020	
iC <sub>4</sub>	-	-	-	
C <sub>1</sub>	0.3690	3.2078	150.180	Barkan and Sheinin[7]
C <sub>2</sub>	0.6760	3.1383	190.800	
C <sub>3</sub>	0.8340	3.1440	194.550	
iC <sub>4</sub>	0.9590	3.3057	177.290	
C <sub>1</sub>	0.3930	3.2500	153.800	Avlonitis[8]
C <sub>2</sub>	0.4980	3.4300	184.100	
C <sub>3</sub>	0.7640	3.2590	203.300	
iC <sub>4</sub>	0.7980	3.0770	231.600	
C <sub>1</sub>	0.2950	3.2512	153.690	Tohidi[9]
C <sub>2</sub>	0.4880	3.4315	183.320	
C <sub>3</sub>	0.7300	3.4900	189.270	
iC <sub>4</sub>	0.7980	3.6000	209.580	
C <sub>1</sub>	0.3834	3.1439	155.593	Sloan[11]
C <sub>2</sub>	0.5651	3.2469	188.181	
C <sub>3</sub>	0.6502	3.3093	203.310	
iC <sub>4</sub>	0.8706	3.0822	225.160	
C <sub>1</sub>	0.3834	3.1439	155.593	Sloan and Koh[16]
C <sub>2</sub>	0.5651	3.2469	188.181	
C <sub>3</sub>	0.6502	3.4167	192.855	
iC <sub>4</sub>	0.8706	3.41691	198.333	

$a$  : Hard core radius, Å.  $\sigma$ : Collision diameter, Å.  $\epsilon$ : Depth of energy well, J.

$k$ : Boltzmann's constant, J/K.

**Table 6.** The experimental data used for pure and mixed gases.

Comp.	No. of data points	Pres. range (MPa)	Ref.
C <sub>1</sub>	261	2 – 250	Deaton et al.[27]; Kobayashi et al.[28]; McLeod et al.[29]; Marshall et al.[30]; Jhaveri and Robinson[31]; Galloway et al.[32]; Verma[33]; Falabella et al.[34]; De Roo et al.[35]; Thakore and Holder[36]; Song et al.[37]; Adisasmito et al.[38]; Deng et al.[39]; Dickens et al.[40]; Makogon et al.[41]; Hutz et al.[42]; Mei et al.[43]; Komai et al.[44, 45]; Nixdorf and Oellrich[46]; smelik et al.[47]; Nakano et al.[48]; Clarke et al.[49]; Jager[50]; Yang et al.[51]; Kharrat et al. (2003); Nakamura et al.[52]; Mohammadi et al.[53]; Gayeta et al.[54];
C <sub>2</sub>	158	0.40 – 120	Roberts et al.[55]; Deaton et al.[27]; Reamer et al.[56]; Galloway et al.[32]; Falabella et al.[34]; Holder et al.[57]; Holder and Hand[6]; Ng and Robinson[58]; Avlonitis[59]; Englezos et al.[60]; Nixdorf and Oellrich[46]; Nakano et al.[61]; Clarke et al.[62]; Morita et al.[63]; Larionov et al.[64];
C <sub>3</sub>	89	0.17 – 10	Wilcox et al. [65]; Miller and Strong [66]; Deaton and Frost [27]; Reamer et al. [56]; Robinson and Metha[67]; Verma [33]; Kubota et al. [68]; Thakore and Holder [36]; Patil [69]; Mooijer-van den Heuvel et al.[70]
iC <sub>4</sub>	31	0.10 - 0.17	Sloan and Koh[16], Rouher and Barduhn[71], Thakore and Holder[36].
C <sub>1</sub> + C <sub>2</sub>	55	0.94 – 68	Deaton and Frost[27], Holder and Grigoriou[57], McLeod and Campbell[29], Holder and Hand[6]
C <sub>1</sub> + C <sub>3</sub>	69	0.26 – 69	Deaton and Frost[27], Holder and Hand[6], McLeod and Campbell[29], Verma[33], Song and Kobayashi[37], Nixdorf and Oellrich[46]
C <sub>1</sub> + iC <sub>4</sub>	100	0.30 – 63	Deaton and Frost[27], McLeod and Campbell[29], Wu et al.[72], Ng and Robinson[58]
C <sub>2</sub> + C <sub>3</sub>	67	0.44 – 2	Holder and Hand[6], Nixdorf and Oellrich[46]
C <sub>1</sub> + C <sub>2</sub> + C <sub>3</sub>	18	0.92 – 24	Zerpa et al.[73], Nixdorf and Oellrich[46]
C <sub>1</sub> +C <sub>2</sub> + C <sub>3</sub> +iC <sub>4</sub>	8	0.92 – 3	Mei et al.[74]

**Table 7.** The Average Absolute Deviation between the experimental and predicted hydrate dissociation conditions for the different Kihara potential function parameters reported by other researchers.

Compound	$AAD^*$ (K)										$AAD_{total}$ (K)
	$C_1$	$C_2$	$C_3$	$iC_4$	$C_1 + C_2$	$C_1 + C_3$	$C_1 + iC_4$	$C_2 + C_3$	$C_1 + C_2 + C_3$	$C_1 + C_2 + C_3 + iC_4$	
Parrish and Prausnitz[5]	0.38	2.83	0.35	0.08	1.22	1.01	1.11	4.21	2.41	2.98	1.38
Holder and Hand[6]	3.38	3.22	2.70	-	3.78	7.36	-	8.50	4.95	-	3.51
Barkan and Sheinin[7]	2.99	9.60	5.03	5.67	2.29	1.57	3.67	13.36	4.15	8.72	5.33
Avlonitis[8]	1.66	0.69	1.91	1.59	1.00	4.16	6.86	2.56	1.80	6.86	2.39
Tohidi[9]	0.78	0.53	0.35	0.12	0.60	7.37	2.99	0.26	0.90	0.52	1.40
Sloan[11]	0.46	0.75	0.85	2.36	1.13	1.93	3.56	4.86	2.78	2.41	1.56
Sloan and Koh[16]	0.33	8.25	0.21	3.23	4.56	0.76	1.23	6.80	5.75	0.33	2.92
Hydract Software	0.30	0.43	0.20	0.11	0.52	0.55	2.73	0.20	0.32	2.34	0.64
This work	0.31	0.43	0.34	0.07	0.39	0.75	1.01	0.32	0.32	0.33	0.45

$$* AAD = \frac{1}{N} \sum_{i=1}^N |T_{i,Calc.} - T_{i,Exp.}|$$

**Table 8.** The values of KPFP optimized in this work..

Hydrate former	$a$ (Å)	$\sigma$ (Å)	$\frac{\varepsilon}{k}$ (K)
C <sub>1</sub>	0.3830	3.14360	155.800
C <sub>2</sub>	0.5900	3.29980	178.709
C <sub>3</sub>	0.6470	3.41900	191.855
iC <sub>4</sub>	0.8921	3.20691	198.332

## Figures Captions:

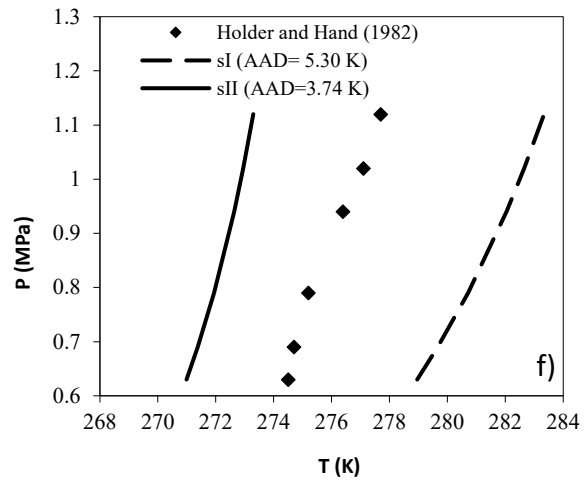
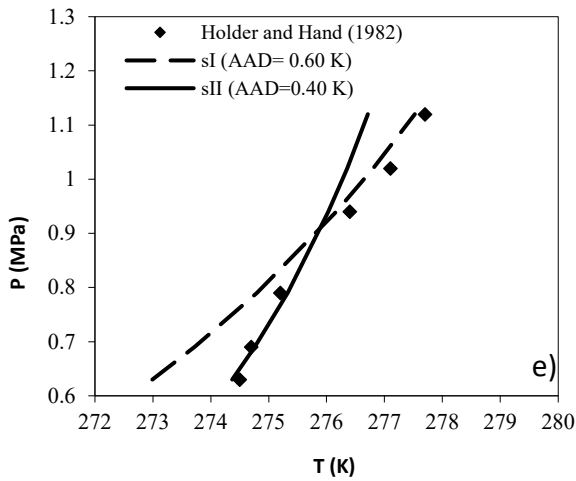
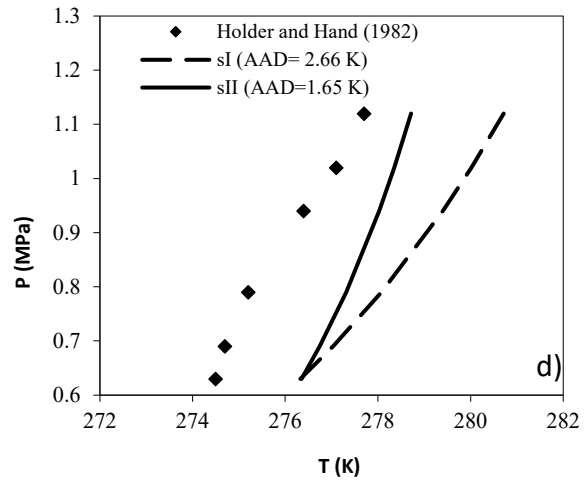
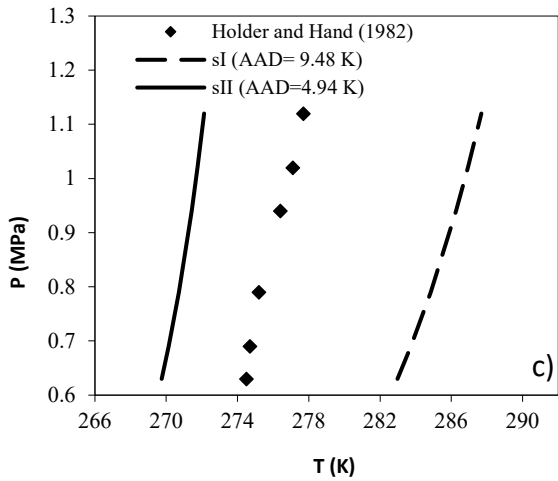
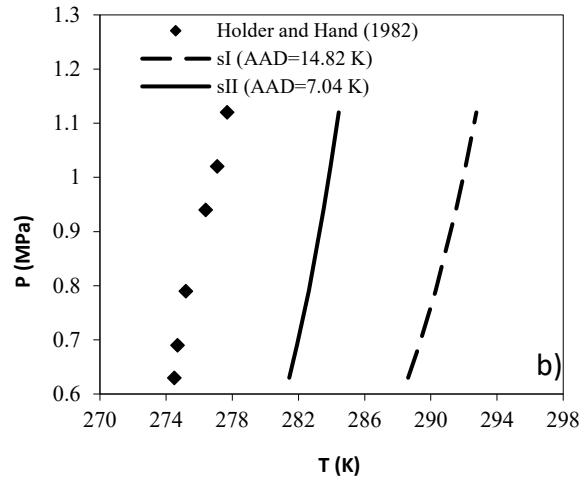
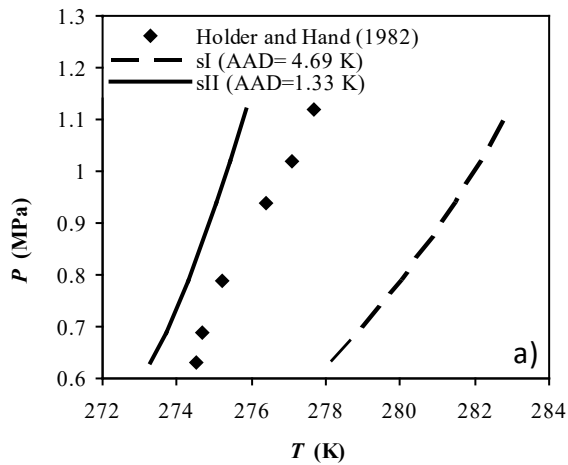
**Figures 1.** Hydrate dissociation conditions of 74 mole % C<sub>2</sub> + 26 mole % C<sub>3</sub> using Kihara Potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** Hydrafact Software.

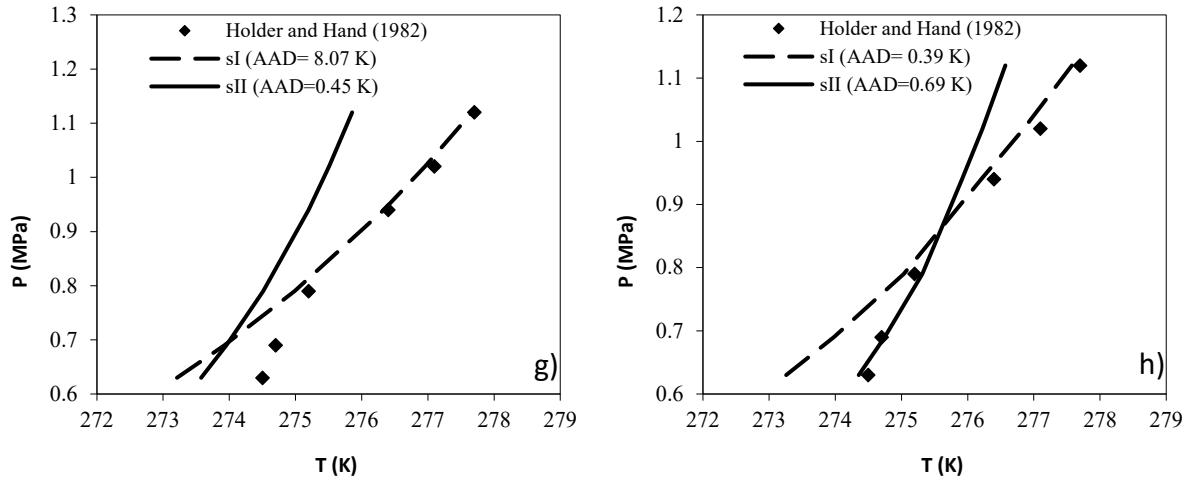
**Figures 2.** Hydrate dissociation conditions of 90.4 mole % C<sub>1</sub> + 9.6 mole % C<sub>2</sub> using Kihara Potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** Hydrafact Software.

**Figures 3.** Hydrate dissociation conditions of 96.5 mole % C<sub>1</sub> + 3.5 mole % C<sub>3</sub> using Kihara Potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** Hydrafact Software.

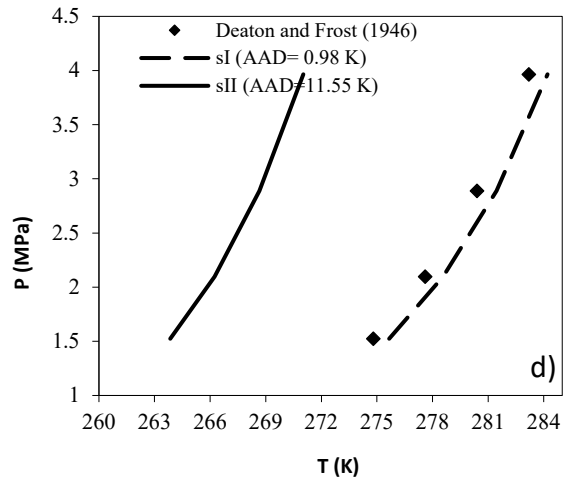
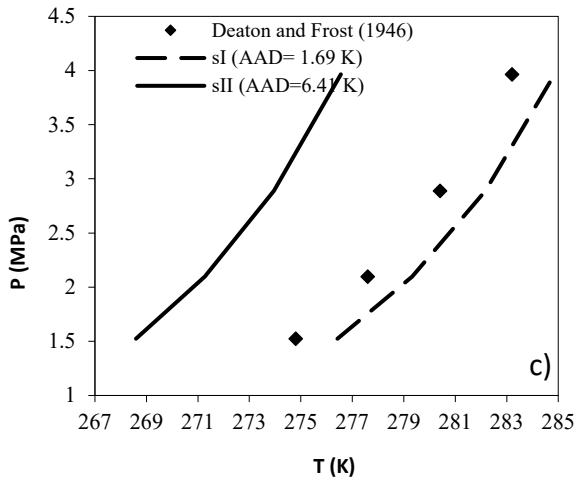
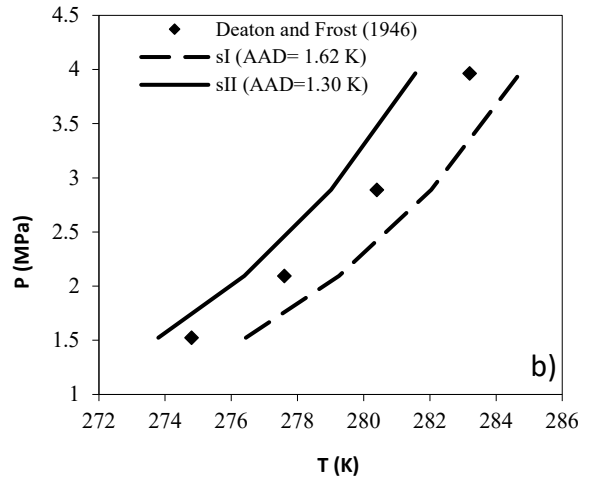
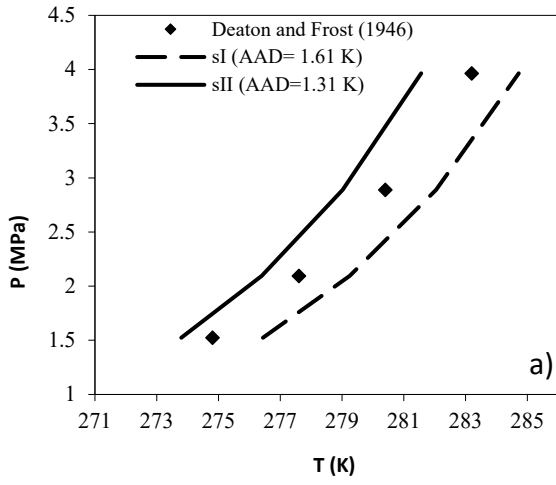
**Figure 4.** Hydrate dissociation conditions of different gas mixtures predicted using Kihara Potential function parameters optimized in this work: **a)** 97.8 mole % C<sub>1</sub> + 2.2 mole % C<sub>2</sub>, **b)** 17.7 mole % C<sub>1</sub> + 82.3 mole % C<sub>2</sub>, **c)** 74 mole % C<sub>2</sub> + 26 mole % C<sub>3</sub>, **d)** 85.15 mole % C<sub>2</sub> + 14.85 mole % C<sub>3</sub>, **e)** 96.5 mole % C<sub>1</sub> + 3.5 mole % C<sub>3</sub>, **f)** 88.13 mole % C<sub>1</sub> + 11.87 mole % C<sub>3</sub>, **g)** 8.7 mole % C<sub>1</sub> + 91.3 mole % iC<sub>4</sub>, **h)** 84.52 mole % C<sub>1</sub> + 12.55 mole % C<sub>2</sub> + 2.93 mole % C<sub>3</sub>, **i)** 70.5 mole % C<sub>2</sub> + 17.4 mole % C<sub>1</sub> + 12.1 mole % C<sub>3</sub>, **j)** 97.25 mole % C<sub>1</sub> + 1.42 mole % C<sub>2</sub> + 1.08 mole % C<sub>3</sub> + 0.25 mole % iC<sub>4</sub>.

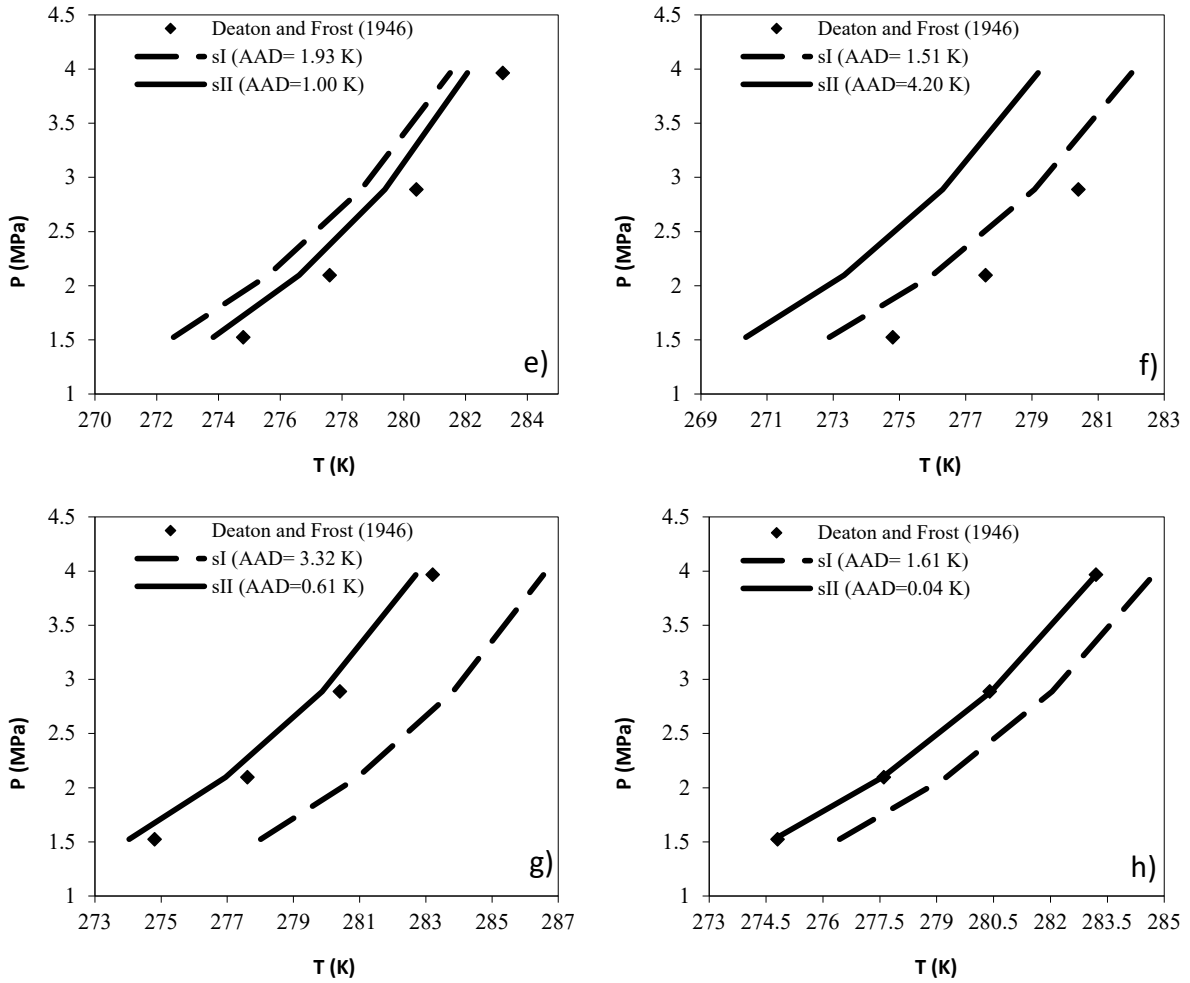




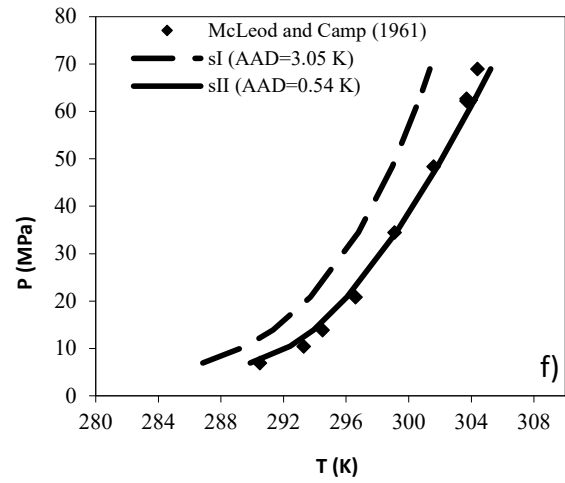
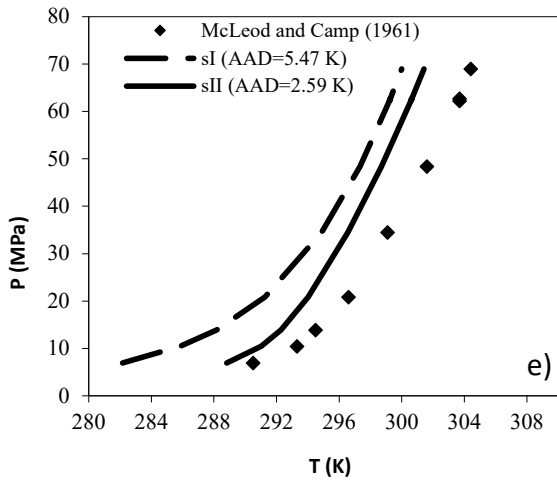
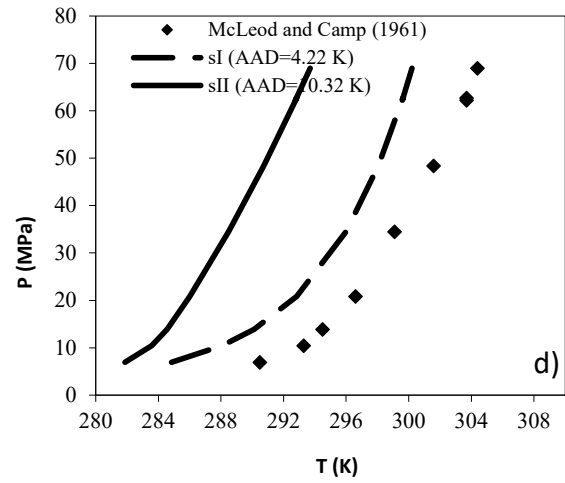
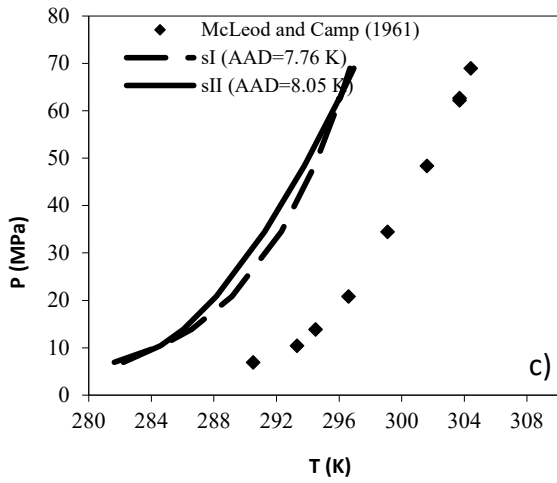
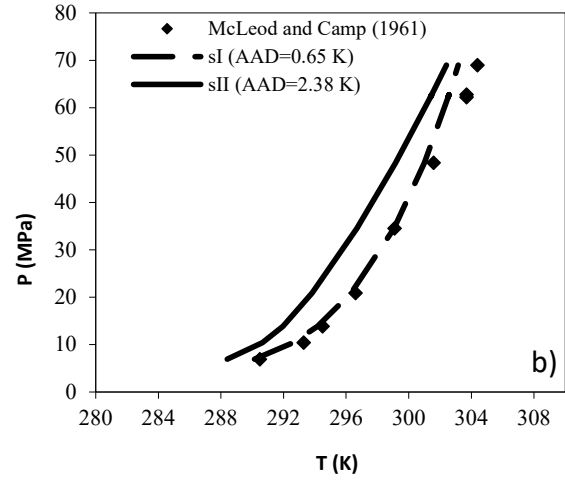
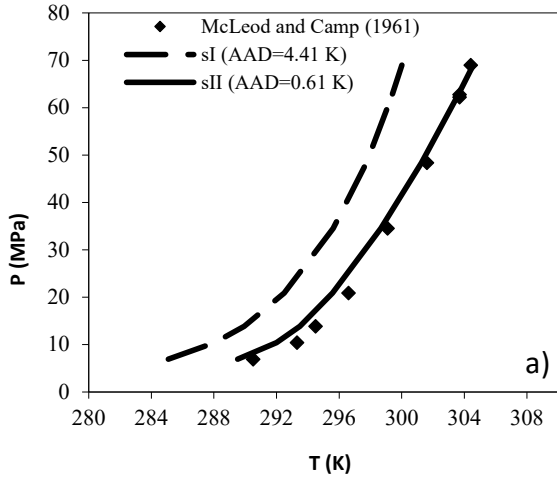


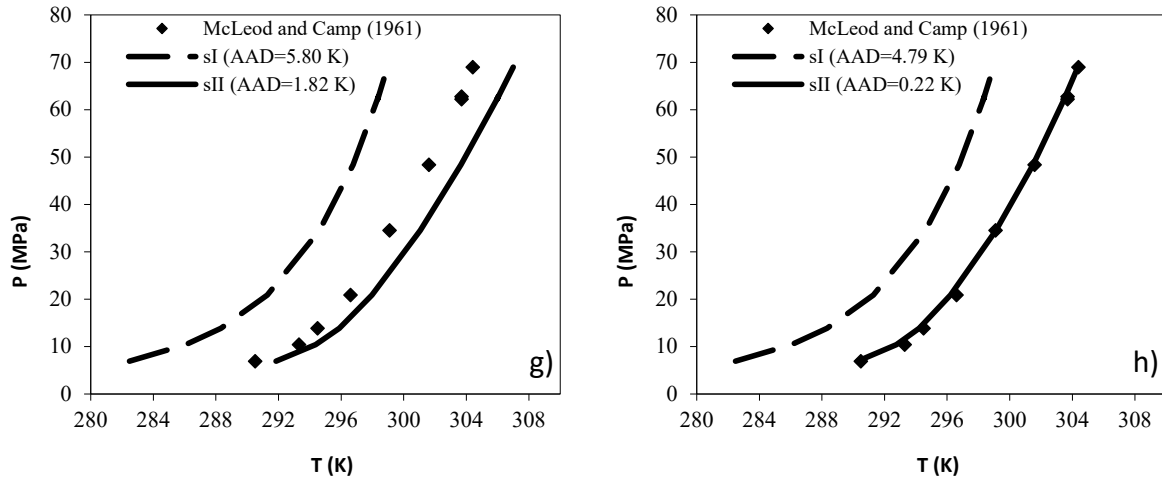
**Figure 1.** Hydrate dissociation conditions of 74 mole % C<sub>2</sub> + 26 mole % C<sub>3</sub> using Kihara potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** HydraFact Software.



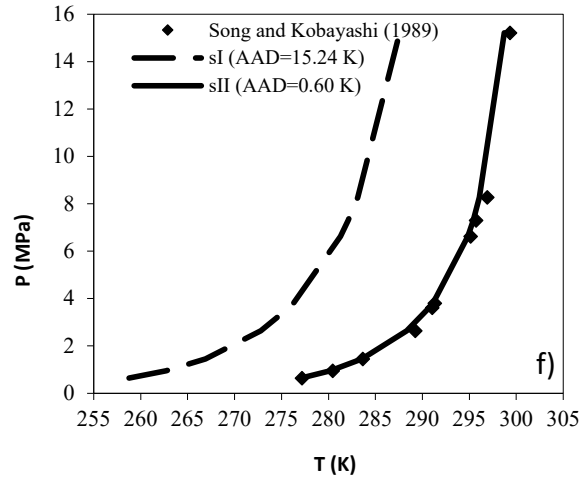
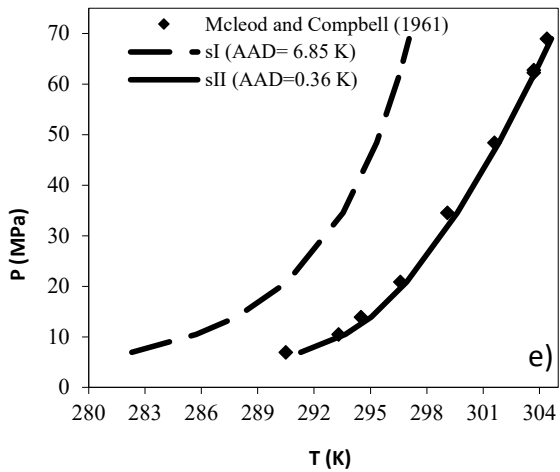
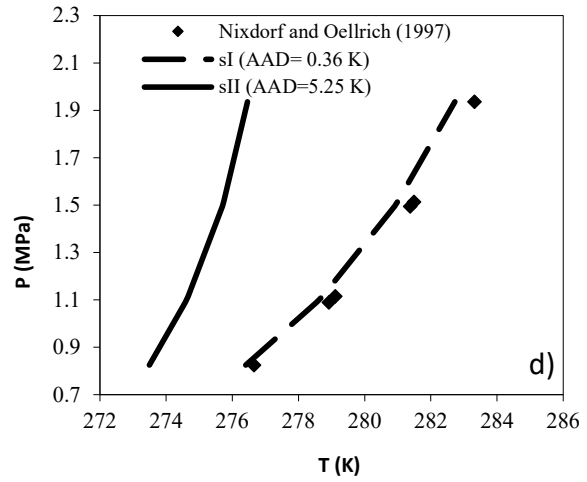
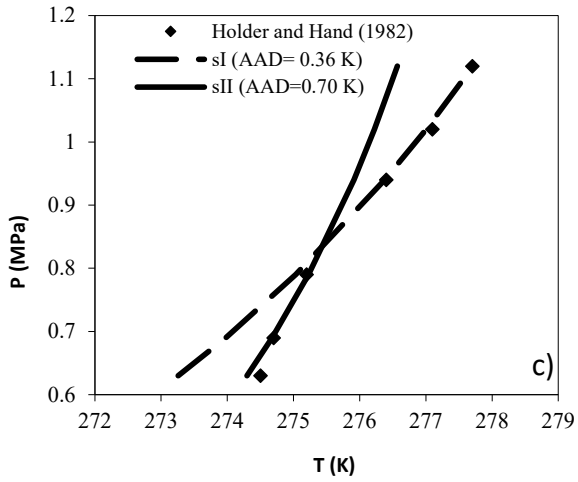
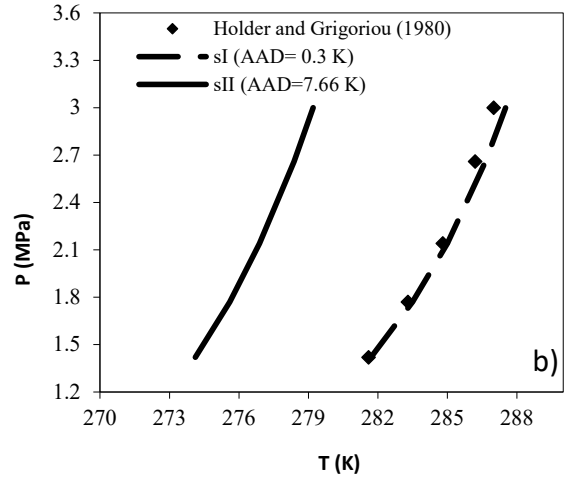
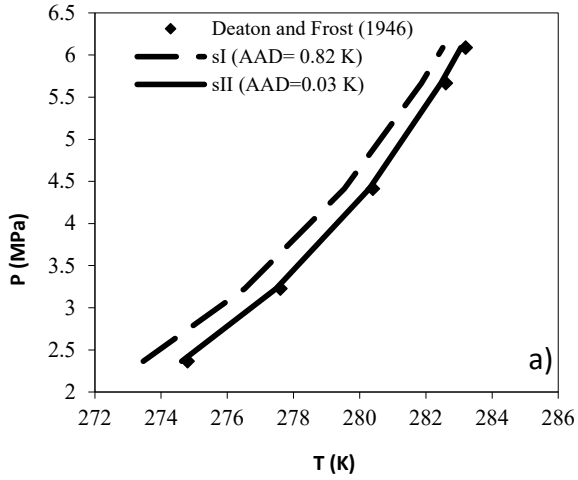


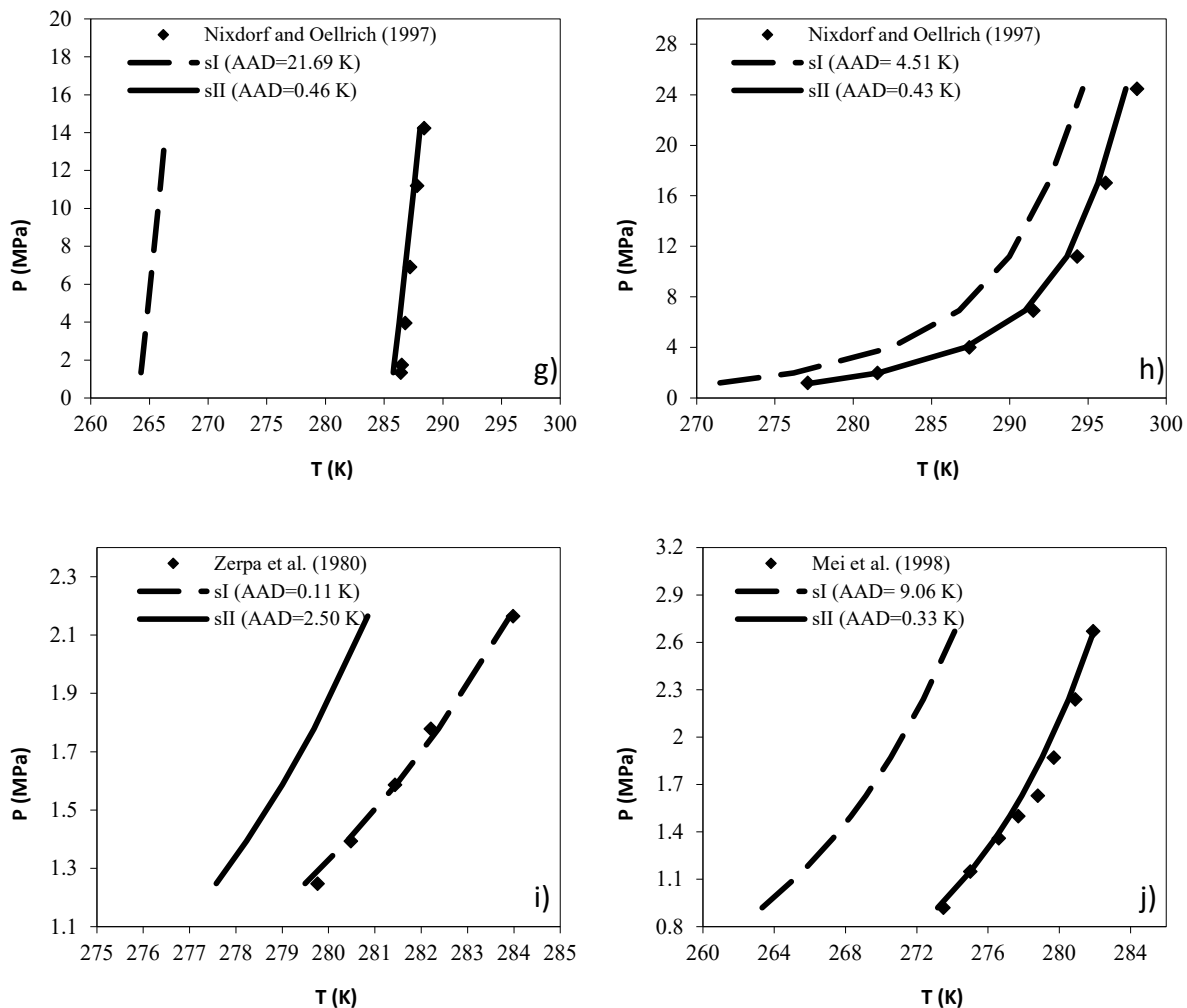
**Figure 2.** Hydrate dissociation conditions of 74 mole %  $C_2$  + 26 mole %  $C_3$  using Kihara potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** Hydract Software.





**Figure 3.** Hydrate dissociation conditions of 96.5 mole %  $C_1$  + 3.5 mole %  $C_3$  using Kihara potential function parameters reported by: **a)** Parrish and Prausnitz[5] **b)** Holder and Hand[6] **c)** Barkan and Sheinin[7] **d)** Avlonitis[8] **e)** Tohidi[9] **f)** Sloan[11] **g)** Sloan and Koh[16] **h)** Hydrafact Software.





**Figure 4.** Hydrate dissociation conditions of different gas mixtures predicted using Kihara potential function parameters optimized in this work: **a)** 97.8 mole %  $C_1$  + 2.2 mole %  $C_2$ , **b)** 17.7 mole %  $C_1$  + 82.3 mole %  $C_2$ , **c)** 74 mole %  $C_2$  + 26 mole %  $C_3$ , **d)** 85.15 mole %  $C_2$  + 14.85 mole %  $C_3$ , **e)** 96.5 mole %  $C_1$  + 3.5 mole %  $C_3$ , **f)** 88.13 mole %  $C_1$  + 11.87 mole %  $C_3$ , **g)** 8.7 mole %  $C_1$  + 91.3 mole %  $iC_4$ , **h)** 84.52 mole %  $C_1$  + 12.55 mole %  $C_2$  + 2.93 mole %  $C_3$ , **i)** 70.5 mole %  $C_2$  + 17.4 mole %  $C_1$  + 12.1 mole %  $C_3$ , **j)** 97.25 mole %  $C_1$  + 1.42 mole %  $C_2$  + 1.08 mole %  $C_3$  + 0.25 mole %  $iC_4$ .