

Fuzzy Bayesian estimation and consequence modeling of the domino effects of methanol storage tanks

Mostafa Pouyakian^a, Fereydoon Laal^{b*}, Mohammad Javad Jafari^c, Farshad Nourai^d, Sohag Kabir^e

^a *Department of Occupational Health and Safety Engineering, School of Public Health and Safety, Shahid Beheshti University of Medical Sciences, Tehran, Iran*

^b *Social Determinants of Health Research Center, Department of Occupational Health Engineering, Birjand University of Medical Sciences, Birjand, Iran*

^c *Safety Promotion and Injury Prevention Research Center, Shahid Beheshti University of Medical Sciences, Tehran, Iran*

^d *Principal Risk Analyst, proNEXO Engineering Consultancy, Tehran, Iran*

^e *Department of Computer Science, University of Bradford, Bradford, BD7 1DP, UK*

*Corresponding author. Ghaffari Blvd, School of Public Health, Birjand University of Medical Sciences, Birjand, Iran. Tel: +985632381651, Email: fereydoonlaal@gmail.com

Abstract

In this study, a Fuzzy Bayesian network (FBN) approach was proposed to analyze the domino effects of pool fire in storage tanks. Failure probabilities were calculated using triangular fuzzy numbers, the combined Center of area (CoA)/Sum-Product method, and the BN approach. Consequence modeling, probit equations, and Leaky-Noisy OR (L-NOR) gates were used to analyze the domino effects, and modify conditional probability tables (CPTs). Methanol storage tanks were selected to confirm the practical feasibility of the suggested method. Then the domino probability using bow-tie analysis (BTA), and FBN in the first and second levels was compared, and the Ratio of Variation (RoV) was used for sensitivity analysis. The probability of the domino effect in the first and second levels (FBN) was 0.0071472631 and 0.0090630640, respectively. The results confirm that this method is a suitable tool for analyzing the domino effects and using FBN and L-NOR gate is a good way for assessing the reliability of tanks.

Keywords: Fuzzy Bayesian network, Domino effect, Atmospheric storage tanks, L-NOR, Methanol, Pool fire

1. Introduction

Large quantities of hazardous and flammable materials are stored in storage tanks in process facilities such as the petrochemical industry. Storing liquid fuels in multiple tanks has also created challenges such as fire, explosion, and the release of toxic substances that fire is the most common. Accidents can lead to heavy financial losses, long delays in production, legal complaints, and devaluation of industrial stocks. Despite the publication of standards and guidelines for the safe design, and construction of storage tanks by companies and business organizations and engineering communities such as API, ASME, and NFPA in recent years, accidents still occur in tanks. One of the important issues due to the complexity of process industries is that the occurrence of accidents in these industries is influenced by domino effects.

39 **1.1. Domino effect, accident propagation, and escalation probability**

40 Although significant progress has been made in recent years in the safety and risk analysis of
41 accident scenarios in single units, domino accidents have received more attention in the field of
42 quantitative risk assessment (QRA) due to lower probability, and more complexity and severity .
43 However, catastrophic domino events have occurred in recent years, such as the Texas refinery
44 accident in which vapor cloud explosions (VCE) caused several fires and other explosions .
45 Domino effect analysis has also been investigated to ensure an adequate internal safe distance in
46 high-risk units, because a large accident may cause secondary events in adjacent units as a result
47 of the domino effects .

48 The occurrence of many process accidents in Iran such as Bou Ali Sina Mahshahr Petrochemical
49 and Kharg Island accidents has also been a domino accident. Therefore, in risk analysis and
50 assessment, it is not only important to deal with the accidents of one equipment or unit, but also
51 the effects of unit or equipment accidents on other units must also be considered, and this is
52 possible by examining the domino effects of accidents . The domino effect occurs when the
53 initial accident in one unit causes other accidents in adjacent units by escalation vectors. These
54 vectors are the same physical effects as heat radiation, overpressure, or projectile fragments by
55 an explosion. Escalation vectors depend on a variety of factors, including the type of initial
56 accident and the distance between the accident center and adjacent units. There are several
57 methods for calculating the escalation vectors, including analytical, integral, and mean models,
58 which are a combination of both analytical and integral models .

59 Probit methods have been used more widely to estimate the probability of escalation According
60 to the methods presented in previous research , which is due to the simplicity, flexibility, and
61 usability of these methods in a wide range of equipment . To prevent dominoes, the occurrence
62 of fire in a tank or dyke wall and the amount of heat radiation received to adjacent tanks should
63 be analyzed. Therefore, according to the main study scenario (pool fire), the present study
64 intends to evaluate the most probable domino scenario.

65 **1.2. Pool fire in atmospheric floating roof storage tanks and its causes**

66 Pool fire is one of the most common process accidents. When a flammable liquid is spilled on
67 the ground, a pool fire occurs . This type of fire is an asymmetric diffuse flame that is created by
68 the combustion of evaporated materials from the liquid surface . Pool fire plays a very effective
69 role in the occurrence of domino events. Especially in an area of oil tanks, a pool fire can destroy
70 the entire complex. According to statistics, the main cause of 80% of a chain accident with fire
71 origin, was pool fire. A well-known example of chain fire is the Buncefield accident in England
72 in 2005 .

73 Based on the records of past accidents and research, there is a possibility of various types of fires
74 in storage tanks, but the possibility of pool fire is higher . In a study using databases such as
75 MHIDAS, MARS, ARIA, and research on 225 accidents that occurred since 1960, Darbra et al.
76 (2010) concluded that storage processes have been a major cause of domino events. , and as
77 reported in the study of Romina et al. (2015), fire and explosion were the main types of accidents
78 . In the study of Taveau (2011), 206 accidents occurred in floating roof tanks, of which 145
79 accidents were fire-type and 61 accidents were explosion-type . The results of the study of Kletz
80 et al., which was conducted to investigate accidents in these tanks, showed that lightning,

81 maintenance operations, and operational errors were the most important causes of these accidents
82 . This study was examined a combination of process, human, organizational, and management
83 factors.

84 **1.3. Fuzzy Bayesian approach**

85 Dynamic risk assessment (DRA) is one of the combined approaches to risk assessment which
86 uses conventional QRA and uncertainty reduction methods . DRA methods use specific data and
87 update mechanisms to review the likelihood of failure of initial public data at the system design
88 stage. New data provided by inspection of the process equipment at regular intervals usually
89 replaces general data to update failure rates using physics-based, structural, mechanical, or
90 condition-based models . Therefore, paying attention to DRA methods will be able to eliminate
91 the shortcomings in QRA methods. According to the above, most risk assessment methods such
92 as fault tree analysis (FTA) and bow tie analysis (BTA) have two important problems, including
93 uncertainty and static structure . There are various methods to reduce these limitations, including
94 sensitivity analysis, probability theory, Dempster-Schafer theory, game theory, possibility
95 theory, and fuzzy sets . In this study, fuzzy logic and Bayesian networks (BNs) were used to
96 reduce uncertainty and make structures more dynamic. Fuzzy theory is used when there is
97 ambiguity and uncertainty and promotes multi-valued, instead of double-valued, logic.
98 Therefore, it is a suitable topic for risk management that deals with qualitative variables and
99 uncertainty . Markowski and Siuta developed a new methodology to improve the identification
100 of representative accident scenarios (RASs), and the results showed the degree of accuracy of the
101 RAS selection process using fuzzy logic . In another study, they used the fuzzy logic approach to
102 the calculation of thermal hazard distances in the process industry .

103 The BN is a non-circular directional graph for uncertainty conditions consisting of nodes and
104 arcs. Nodes in the BN represent random variables and are connected by directional arcs. Arcs
105 show the usual dependencies and relationships between connected nodes. Conditional probability
106 tables (CPTs) also determine the type and severity of such dependencies. In a BN , the nodes
107 from which the arcs come out and the nodes to which the arcs reach are called the parent and
108 child nodes, respectively. Thus a node can be the child of one node and the parent of another
109 node at the same time. Nodes that have no parents are called "root nodes" and nodes that have no
110 children are called "leaf or central nodes". The other nodes are "intermediate nodes" . Fig 1
111 shows a typical BN consisting of 4 nodes in which: X1 root node; X2 is an intermediate node;
112 And X3 and X4 are leaf nodes. In addition, node X2 is both the child of X1 and the parent of X3
113 and X4. Therefore, we assume that this BN is used for failure analysis in a sprinkler system and
114 includes a smoke sensor (flame) (X1), actuator (X2), alarm (X3), and a sprinkler (X4). When a
115 fire is lit, the smoke sensor can activate the actuator ($X1 \rightarrow X2$) and sound the alarm ($X1 \rightarrow$
116 $X3$), and then the actuator activates the sprinkler ($X2 \rightarrow X4$). To increase system reliability, the
117 actuator can also use the alarm ($X2 \rightarrow X3$).

118 The field of safety risk analysis should be expanded by considering the accident precursors and
119 changes in process parameters (such as level, pressure, flow, etc.). The probabilities of failures
120 and accidents will be predictable with this approach and can be continuously updated in real-
121 time processes. One of the most important techniques for modeling the accident scenario and risk
122 assessment is BTA, which is a combination of FTA and Event Tree Analysis (ETA). These

123 methods are not suitable for analyzing large and complex systems, especially if those systems
124 contain additional components or show dynamic behavior or time-varying parameters .

125 Numerous studies have shown that events such as the BP Texas City refinery accident in 2005,
126 could have been prevented by combining a dynamic risk approach with a management
127 framework . However, implementing a DRA approach can be a complex process and requires a
128 variety of resources. Therefore, continuous improvement in any process industry requires the
129 integration of risk assessment methods with management systems .

130 Although BN has several advantages, the difficulty of determining CPTs is one of its
131 disadvantages . In this study, L-NOR (Leaky-Noisy OR) gates were used to analyze the domino
132 effects of pool fire to reduce the number and complexity of CPTs.

133 QRA methods often use OR and AND gates, which is a kind of absolute analysis of these logical
134 gates . In various studies, they used L-NOR gates to achieve smaller CPTs. The use of this type
135 of gate has higher diagnostic accuracy than common logic gates . If Noisy-OR gates are used, the
136 size of CPT decreases with the number of parent variables , and using these structures, fewer
137 parameters are required to define CPT .

138 Therefore, this study intends to provide an approach to analyze the domino effects of pool fire in
139 floating roof atmospheric storage tanks using fuzzy bayesian network (FBN) and probit models,
140 and modify the structure of CPTs in domino analysis using L-NOR gates. In this study, we have
141 performed an analytical comparison of the domino effect in the first and second levels using
142 BTA and FBN techniques in addition to the analysis of human, organizational and process
143 factors.

144 **2. Method**

145 **2.1. Specifications of the studied tanks**

146 The present study was performed on methanol tanks of a petrochemical company (three tanks
147 including TK A / B / C). Tanks are quite similar in terms of mechanical structure and stored
148 material. In these tanks, pure methanol is stored and transported to the relevant export port.
149 Methanol is a highly flammable liquid with moderate respiratory and gastrointestinal toxicity.
150 Methanol tanks are atmospheric type and have a floating roof, and each tank has a volume of
151 64,700 cubic meters of methanol and an internal diameter of 63 meters. Also, the distance
152 between tank 1 and the other two tanks is 37 and 118 meters, respectively.

153 Fig 2 shows the arrangement of tanks and their location in the petrochemical plant. Methanol is
154 transported to the jetty through pipes to load the tanker using 3 pumps. These tanks have
155 numerous instrumentation equipment including Level Switch (LS), Level Alarm (LT), Pressure
156 Transmitter (PT), Pressure Indicator (PI), Pressure Control Valve (PCV), and, Breather Valve
157 (BV) which has provided to improve safety. PCV provides the necessary nitrogen pressure above
158 the floating roof. The Low Low (LL) and High High (HH) alarms are in the range of -5 to 20
159 mbar for manual and automatic opening and closing of the nitrogen tank, respectively. BV opens
160 if PCV does not operate and nitrogen pressure is high.

161 **2.2. Research flowchart**

162 This section provides an overview of the current study approach (Fig 3). Determining the
 163 probability of failure of tanks and pool fire as well as analyzing the domino effect and
 164 calculating the joint probability distribution are two basic steps in this approach.

165 2.2.1. Determining the probability of failure of tanks and pool fire with FFT and FBN

166 At this stage, the method of determining the probability of failure of tanks and the occurrence of
 167 pool fires are briefly presented. First, hazard identification and risk analysis of selected scenarios
 168 were performed using piping and instrumentation diagram (P&ID), process flow diagram (PFD),
 169 interviews with experts of different process units, review of past accidents and near-misses of
 170 tanks, and hazard and operability study (HAZOP) results in a relevant petrochemical plant. To
 171 determine the probability of occurrence of the basic event, expert judgment, and fuzzy theory
 172 were performed using linguistic terms. For this purpose, four experts were selected
 173 heterogeneously from the relevant petrochemicals who had sufficient information about the
 174 system and familiarity with the fault tree structure. Due to the differences of experts in terms of
 175 their experiences, knowledge, and different perceptions, a weight factor (WF) was used using
 176 Lavasani and Renjith methods to Fuzzification and perception/opinion evaluation of experts was
 177 done using triangular fuzzy numbers (TFNs) ($\tilde{A} = a_1, a_2, a_3$), and 7 linguistic terms (very low
 178 (VL), low (L), relatively low (RL), medium (M), relatively high (RH), high (H) and very high
 179 (VH)). These fuzzy numbers, under some weak assumptions, directly fulfill the good
 180 optimization criteria and the popularity and simplicity of TFNs have made them more widely
 181 used.

182 Then, the Center of area (CoA)/Sum-product approach was used to evaluate aggregated fuzzy
 183 failure possibility (AFFP) (Eq 1) and for defuzzification (CFP: Crisp Failure Possibility) (Eq 2).
 184 The AFFP values obtained from the consensus stage were converted to a crisp value using the
 185 CoA method. In the Yazdi and Zarei study, which aimed to investigate uncertainties in safety
 186 risk analysis and compare different approaches, the combined CoA/Sum-product approach was
 187 mentioned to be better than other methods in terms of computational complexity, reliability, and
 188 time spent on calculation.

$$189 \quad Z_i = g_x = \sum_{j=1}^n w_j f_{ij}, \quad i=1,2,\dots,n \quad j=1,2,\dots,m \quad (1)$$

190 Here Z_i is the consensus fuzzy number for base events, w_j represents the weight of expert j,
 191 f_{ij} also represents the fuzzy numbers of the base event i with respect to expert j.

$$192 \quad CFP = \frac{\int_{a_1}^{a_2} \frac{x-a}{a_2-a_1} x dx + \int_{a_2}^{a_3} \frac{a_3-x}{a_3-a_2} x dx}{\int_{a_1}^{a_2} \frac{x-a_1}{a_2-a_1} dx + \int_{a_2}^{a_3} \frac{a_3-x}{a_3-a_2} dx} = \frac{1}{3} (a_1 + a_2 + a_3), \quad (2)$$

193 Here x is the output variable.

194 The probability of occurrence of intermediate and top events (TEs) was also calculated from the
 195 gate-by-gate method for AND and OR gates.

196 $P_i = 1 - \prod_{i=1}^n (1 - P_i), \quad (3)$

197 $P_i = \prod_{i=1}^n P_i, \quad (4)$

198 $P_{TE} = \prod_{j \in M} (1 - \prod_{BE_{i,j}} (1 - P_i)), \quad (5)$

199 Where P_i is the basic event probability (BE_i) and Q_j is a basic event or group of basic events
200 in the fault tree structure ($\forall j \in M$). P_{TE} is also the probability of the TE.

201 Finally, the Onisawa relation was used to convert CFP to failure probability (FP) using eq (6).
202 Using this relationship, the CoA output becomes probabilistic. K in this equation is an
203 intermediate variable that depends only on CFP.

204
$$FP = \begin{cases} \frac{1}{10^K} CFP \neq 0 \\ 0 CFP = 0 \end{cases} K = \left[\frac{1 - CFP}{CFP} \right]^3 \times 2.301, \quad (6)$$

205 Then the probability of occurrence of a pool fire with respect to the probability of an immediate
206 ignition was obtained from Equation (7).

207
$$P_r | Consequence | = P_r | TE | \times \prod_{j=1}^n P_r | E |, \quad (7)$$

208 Here, $P_r | Consequence |$ is the probability of each outcome, $P_r | TE |$ is the probability of the
209 main event, and $P_r | E |$ is the probability of failure or success of the protective layers.

210 According to Bevi's instructions, the probability of immediate and delayed ignition for
211 flammable and volatile liquids with a flashpoint less than 21 C is 0.065 and 0.935, respectively .
212 In the present study, basic, intermediate, and TEs, immediate, and delayed ignition barriers and
213 consequences, were entered into the GeNIe software version 2.3 as root, intermediate, central
214 (leaf), barrier, and consequences nodes, respectively, based on the study of Khakzad et al. (see
215 Fig 3) and after creating CPTs for different nodes, probability updates were obtained.

216 2.2. Analyzing the domino effect and calculate the joint probability distribution

217 In this study, their effects in the studied units were investigated using the Bayesian network and
218 probit methods. In probit methods, both the type of equipment and escalation vector are
219 considered to calculate the amount of probit (Y). In general, Y can be obtained using Eq (8).

220 $Y = a + b \ln(V), \quad (8)$

221 In this equation, a and b are probit coefficients, which are determined using experimental data
222 and regression methods, and V is the escalation vector or relevant parameters (for example, in
223 the case of radiation flux, the failure time of the vulnerable equipment is considered as time to
224 failure, TTF (s)). After determining Y, the probability of escalation ($P_{Escalation}$) can be calculated
225 using the following equation:

226 $P_{Escalation} = \Phi | Y - 5 |, \quad (9)$

227 In this study, to obtain probit values for radiation flux, the probit methods proposed by Cozzani
 228 et al. were used . The procedure can be summarized as follows in 9 steps.

229 **Step 1.** Select study nodes (three tanks) and identify the domino effect primary unit (Primary
 230 Event) using the safety and accident reports, and the results of the existing risk assessment (tank
 231 T1).

232 **Step 2.** Calculate the resonance vector based on the type of possible scenario using the amount
 233 of heat radiation calculated from PHAST software version 7.2 (consequence modeling).

234 **Credible Event Scenario Consequence Modelling (CESCM)**

235 In this study, to estimate the severity of the outcome of the accident scenario and heat radiation,
 236 a valid and specific method of process systems called CESCM modeling was used using
 237 PHAST software version 7.2. Therefore, methanol leakage from the connection of the tank to the
 238 side pipes and pool fire was selected as a scenario and possible outcome. The credible scenario
 239 was selected according to the Total standard (GS EP SAF 253) and the diameter of the outlet
 240 pipe, for a leakage size of 150 mm (large leakage) . The determined leakage is equal to 20% of
 241 the diameter of the outlet pipe according to the Total standard . Table 1 shows the physical and
 242 operational characteristics of the studied tanks for modeling.

243 **Table 1. Consequence modeling information**

Parameter	The amount or type	Parameter	The amount or type
Nominal capacity (m ³)	64700	relative humidity (%)	62.5
Inner diameter × Cylindrical height (mm)	24100×63000	Temperature (°C)	40
Material stored	Methanol	Leak diameter (mm)	150
Operating temperature (°C)	40	Leak Direction	Horizontal
Operating pressure (bar)	0.0013	Dominant wind speed (m/s)	5.2
Flash Point (°C)	14	Atmospheric stability class	E
IGBS	Nitrogen	Surface roughness (m)	1
Largest Nozzle Diameter (in.)	30	Dominant wind direction	North West
Nozzle height (m)	1		
Roof Type	Cone with an internal floating roof		

244 Note: IGBS = Inert gas blanketing system

245 **Step 3.** Determine the potential secondary unit by comparing the resonance vector with the
 246 threshold value (TV). TV is an important criterion for identifying the occurrence of fire
 247 dominoes, and dominoes will not occur if the physical effects or escalation vectors are less than
 248 this value. Cozzani et al. determined 15 kW/m² as the threshold value for atmospheric storage
 249 tanks . To determine which units are affected, the initial vectors applicable to adjacent units as a
 250 result of the initial event should be compared with the predetermined threshold values. If the
 251 escalation vectors are significantly higher than the corresponding threshold, they have sufficient
 252 power to damage adjacent units, which leads to a loss of safety or physical integrity. Therefore,
 253 primary screening of adjacent units was performed with this comparison, and potential secondary
 254 targets are identified .

255 **Step 4.** Calculate the amount of probit for pool fire.

256 $Y = 12.54 - 1.847 \ln(TTF), \quad (10)$

257 $\ln(TTF) = -1.128 \ln Q - 2.667 \times 10^{-5} V + 9.877, \quad (11)$

258 Here Y is the amount of probit, TTF is time to failure (in seconds), Q is heat radiant, and V is the
259 unit volume.

260 **Step 5.** Calculate the escalation probability for potential secondary units using the amount of
261 probit considering the initial event and conditional probabilities.

262 $P_d = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{Y-5} e^{-x^2/2} dx, \quad (12)$

263 **Step 6.** Identify the secondary units with the highest escalation probability and draw the arcs.

264 **Step 7.** Identify potential accident scenarios and their probability of occurrence for secondary
265 units: we determine the potential accident scenarios and their probability of occurrence for these
266 units by assuming that the secondary units are damaged.

267 **Step 8.** Consider the secondary units as the primary unit and repeat the previous steps to
268 determine the next potential units. After creating a probabilistic propagation pattern for the
269 domino effect in the BN and calculating the probability of the initial event and the conditional
270 probabilities of other events, the combined probability distribution for the events involved in the
271 domino effect can be calculated with GeNIe software. A noteworthy point in this study as an
272 innovation is the use of L-NOR gates to determine domino effects. Because there is a possibility
273 of failure of any of the tanks without considering the domino effects.

274 Therefore, in this study, L-NOR gates were used to modify the CPTs. When a child node is
275 affected by the parent nodes, the overall effect of the parent nodes can be calculated using
276 equations (13) and (14). If we consider the initial probability X (P_{Leak} or leak probability) as an
277 independent parent, then we use equation (14) to calculate the probability X (considering its
278 parents and initial probability).

279 $P(X|Pa(X)) = 1 - \prod_{i \in Pa(X)} (1 - P_i), \quad (13)$

280 $P(X|Pa(X)) = 1 - (1 - P_{Leak}) \prod_{i \in Pa(X)} (1 - P_i), \quad (14)$

281 P_i is the probability X given that its i^{th} parent is true and the others are false.

282 Assuming that one of the variables X_i occurs and the other variables do not occur, the occurrence
283 of the child node Y or Pa (X) can be expressed as follows:

284 $P_j = P(Y = 1 | X_1, X_2, \dots, X_j, \overline{X_{j+1}}, \overline{X_n}), \quad (15)$

285 **Step 9.** Perform a sensitivity analysis by Ratio of Variation (RoV) method: Sensitivity analysis is
286 also used to identify the most important basic events that cause process failure. The RoV

287 method is calculated based on the previous probabilities ($\theta(X_i)$) and the posterior probabilities
 288 of the root nodes ($\pi(X_i)$) as follows:

$$289 \text{RoV}_{X_i} = \frac{\pi(X_i) - \theta(X_i)}{\theta(X_i)}, \quad (16)$$

290 3. Results

291 3.1. Determining the probability of tank failures

292 In this study, a bow tie model was drawn according to Fig 4. As the main scenario in this study is
 293 the pool fire, the probability of its occurrence was calculated using FFT and FBN.

294 According to Tables 2 and 3, 58 basic events and 30 intermediate events were identified, which
 295 are a combination of process, human and organizational, management factors. Then the
 296 probability of occurrence of basic events was obtained using linguistic terms and the opinions of
 297 experts and fuzzy logic. Experts included safety supervisor, Master of analyzer and
 298 instrumentation, Master of Maintenance Planning, and operation supervisor, which had weight
 299 factors of 0.274, 0.235, 0.235, and 0.254, respectively. Weight factors were calculated based on
 300 Lavasani and Renjith methods.

301 After obtaining expert opinions, the corresponding fuzzy numbers were obtained for each
 302 linguistic term. The formulation was performed in a spreadsheet and by calculating the values of
 303 AFFP, CFP, and variable K using the Eq 1 to 5, FP (FFT) was obtained, the results of which can
 304 be seen in table 2. The probabilities were also updated after the transfer of various events in BN
 305 and GeNIe software, the results of which can be seen in the last column of the table. Updated
 306 values of basic events showed that X12, X51, and X32 had the largest shares in the occurrence of
 307 TE. X4, X3, and X2 also had the lowest FP, respectively.

308 **Table 2.** Expert opinion, fuzzy and FBN probabilities of root events

event	Description	Expert opinions	FP (FFT)	FBN	event	Description	Expert opinions	FP (FFT)	FBN
X1	BV failure	M, L, L, L	0.000367	0.000367	X30	The same sound frequency related to the alarm	M, L, H, RL	0.002422	0.002422
X2	PCV failure	RL, L, L, L	0.000119	0.000119	X31	Shift work	RL, L, RH, M	0.002352	0.002352
X3	Insufficient supply of N ²	L, L, L, L	4.575E-5	4.5759E-5	X32	Incorrect job description	L, M, H, M	0.004478	0.004478
X4	Failed to send signal	L, L, L, L	4.575E-5	4.5759E-5	X33	High working pressure	L, RH, M, M	0.003468	0.003468
X5	Failure of PT ₁	L, L, M, L	0.000294	0.000294	X34	Inadequate standards audits and Procedures	VL, M, M, RL	0.001039	0.001039
X6	Failure of PT ₂	L, L, M, L	0.000294	0.000294	X35	Lack of updated instructions and Procedures	L, RH, M, RL	0.002164	0.002164
X7	No HH Alarm on PT	L, M, RL, M	0.001395	0.001395	X36	Insufficient knowledge	M, RL, M, M	0.003334	0.003334
X8	No LL Alarm on PT	L, M, RL, M	0.001395	0.001395	X37	Defects in staff training and awareness	RH, M, M, M	0.007538	0.007538
X9	Failure of PI ₁	L, RL, M, L	0.000477	0.000477	X38	Insufficient communication	RL, VL, RH, M	0.001961	0.001961
X10	Failure of PI ₂	L, RL, M, L	0.000477	0.000477	X39	Communication failure	L, L, RH, RL	0.000934	0.000934
X11	TSV failure in the downstream line of export	RL, VL, RL, M	0.000653	0.000653	X40	Inadequate monitoring	RL, M, RH, M	0.004606	0.004606
X12	Lack of permit	M, M, RH, RH	0.010298	0.010298	X41	Inadequate safety plans	RL, RH, RH, H	0.012207	0.012207
X13	Wrong permit	RH, L, VL, RL	0.000955	0.000955	X42	Poor decision making	L, L, VH, RH	0.004192	0.004192
X14	Lack of implementation	L, L, M, L	0.000494	0.000494	X43	Insufficient job knowledge	L, VL, L	0.003582	0.003582

X15	of permit Defects in the correct execution of permit	RL VL, L, L, RL	6.213E-5	6.2133E-5	X44	of managers Inefficient management behaviors	VH, RH L, RH, VH, M	0.007439	0.007439
X16	Defects in the restarting	L, VL, M, M	0.000787	0.000787	X45	Poor communication	L, L, VH, RH	0.004192	0.004192
X17	Failure of LI ₁	VL, M, M, M	0.000183	0.000183	X46	Mechanical fatigue	L, RL, RH, M	0.002246	0.00224600
X18	LTHH failure	VL, VL, RH, RL	0.000540	0.000540	X47	Thermal fatigue	L, L, L, VL	2.141E-5	0.00002141
X19	LAH failure	VL, RL, RH, RL	0.001022	0.001022	X48	Insufficient accuracy of leak detector equipment	VL, M, H, RL	0.002352	0.002352
X20	LAHH failure	VL, RL, H, RL	0.001448	0.001448	X49	Inspector detection error	L, RL, VH, RL	0.002193	0.002193
X21	Failure of LI ₂	VL, L, RH, RL	0.000704	0.000704	X50	Lack of cathodic protection	RL, RL, RH, M	0.003072	0.003072
X22	LTLL failure	VL, VL, RH, RL	0.000540	0.000540	X51	Delay in inspection	RH, RH, RH, L	0.008103	0.008103
X23	LAL failure	VL, L, RH, RL	0.000704	0.000704	X52	Poor inspection	M, RL, H, RL	0.004131	0.004131
X24	LALL failure	VL, L, RH, RL	0.000704	0.000704	X53	Insufficient and inadequate methods of corrosion detection	L, L, RL, M	0.000524	0.000524
X25	Physical disability	VL, RL, H, RL	0.001448	0.001448	X54	Lack of monitoring of welds and joints	L, M, RH, RL	0.002164	0.002164
X26	Low job motivation	L, M, H, RL	0.002877	0.002877	X55	Poor monitoring of welds and joints	L, RL, RH, M	0.002246	0.002246
X27	Insufficient skill	L, M, M, M	0.002276	0.002276	X56	Distraction and disregard for driving principles	VL, VL, M, RL	0.000248	0.000248
X28	Defects in the improvement of the operator skill system	L, M, M, RL	0.001337	0.001337	X57	Lack of necessary skills	L, L, RH, M	0.001679	0.001679
X29	Defects in human activity locking equipment	VL, VL, H, RL	0.000823	0.000823	X58	Unauthorized speed	L, L, M, RH	0.001746	0.001746

309 Note: BV = Breathing valve; FBN = Fuzzy bayesian network; FFT = Fuzzy fault tree; FP =
310 Failure probability; H = High; HH = High high; L = Low ; LAH = Level alarm high; LAHH =
311 Level alarm high high; LAL = Levl alarm low; LI = Level indicator; LL = Low low; LTHH =
312 Level transmitter high high; LTLL = Level transmitter low low; M = Medium; PCV = Pressure
313 control valve; PI = Pressure indicator; PT = Pressure transmitter; RH = Relatively high; RL =
314 Relatively low; TSV = Temprature switch valve; VH = Very high; VL = Very low.

315 The various intermediate events (IEs) are also summarized in table 3. FFT and FBN values were
316 obtained according to the type of gate between events and CPT, which are seen in the third and
317 fourth columns of table 3. The results of inductive reasoning of fault tree showed that FFT for
318 TE was equal to 0.11213960 but the FBN calculated the probability of its occurrence being
319 0.063, which is smaller than the value calculated by the fault tree method. Because the fault tree
320 method calculates the TE probability assuming it is independent, however, the BN method
321 considers the statistical dependence between events when calculating the TE probability. The
322 probability of pool fire according to the method, based on BTA and FBN was equal to 0.007289
323 and 0.0041266742, respectively.

324 **Table 3.** Fuzzy and FBN probabilities of intermediate and TEs

Events	Description	FFT	FBN
I1	Pressure control system failure	0.03408536	0.0335850 0
I2	Level control system failure	0.03407713	0.0335850 0
I3	M&OB failure	0.00065556	0.0006420 0
I4	Preventive maintenance Barrier failure	0.02705241	0.0267470 0
I5	Vehicle collisions	0.01626913	0.0161930 0

I16	Failure in IGBS and BV	0.00000000	0.00000000 0
I17	Heat source during box up conditions	0.00000823	0.0000082 1
I18	Human Error	0.00000341	0.0335850 0
I19	Failure in IGBS	0.00000000	0.0000000 0
I110	Defect in permit	0.01259613	0.0125700 0
I111	Defects in monitors and alarms	0.00000000	0.0000000 0
I112	PT Defect	0.00000000	0.0000000 0
I113	PI Defect	0.00095400	0.0009530 0
I114	Overfilling	0.00000000	0.0000000 0
I115	Excessive emptying	0.00000000	0.0000000 0
I116	LSL Failure	0.00000050	0.0000005 0
I117	Personal characteristics	0.00793800	0.0079150 0
I118	Defects in human-system interference Barrier	0.00324500	0.0032430 0
I119	Defects in the design of Boardman's job and workplace	0.02289413	0.0227050 0
I120	LSH Failure	0.00000148	0.0000014 8
I121	Insufficient skills	0.00361300	0.0036090 0
I122	Incorrect work schedules	0.02054213	0.0204010 0
I123	Organizational Barrier Failure	0.03378300	0.0333390 0
I124	Managerial Barrier Failure	0.01940500	0.0192680 0
I125	Insufficient knowledge	0.01087200	0.0108460 0
I126	Improper communication	0.00289500	0.0028930 0
I127	Fault in leak testing	0.00454500	0.0045390 0
I128	Corrosion	0.01583000	0.0157510 0
I129	Failure to monitor the destruction of welds and joints	0.00441000	0.0044050 0
I130	Failure to detect corrosion	0.01275800	0.0127180 0
	TE Methanol leakage	0.11213960	0.0630000 0

325 Note: BV = Breathing valve; FBN = Fuzzy bayesian network; FFT = Fuzzy fault tree; IGBS =
326 Inert gas blanketing system; M&OB = Managerial and organizational barrier; PI = Pressure
327 indicator; PT = Pressure transmitter; LSH = Level switch high; LSL = Level switch low

328 3.2. Analyzing the domino effect and calculating the joint probability distribution

329 **3.2.1. Consequence modeling and heat radiation**

330 Fig 5 shows the area affected by different amounts of heat radiation in terms of distance from the
 331 accident site. According to the figure, the amount of heat radiation caused by a methanol tank is
 332 constant up to a distance of 68 meters and is equal to 50 kW/m², which is the highest amount of
 333 heat radiation due to the failure of a tank. According to Fig 6, the affected spaces due to heat
 334 radiation of 37.5, 12.5, and 4 kW/m², were equal to 169.06, 116.02, and 72.048 meters,
 335 respectively.

336 **3.2.2. Analysing the domino effect**

337 The studied tanks are located on a straight line with the same distance between them and were
 338 considered as three study nodes. Based on the results of risk assessment, storage tanks have an
 339 initial FP of 0.11213960 and 0.063 based on the results of FFT and FBN. The amount of heat
 340 radiation at a distance of 107.8 meters was equal to 15.8 kW/m², which is more than the TV.
 341 Therefore, due to the distance of 37 meters between the two tanks, the fire created in tank 1 (T1)
 342 will cause a domino effect in the first level. The distance from tank T1 to tank T3 is 118 meters.

343 Tables 4 and 5 show the probabilities of exacerbating the domino effects of initiating events.
 344 Node T2 is a potential secondary node, its escalation probability is shown in Table 5. The results
 345 of the combined escalation effects of the two tanks T1 and T2 in the second level of dominoes
 346 are also given in this table.

347 **Table 4.** The probability of escalation of domino effects caused by T₁ tank failure if (
 348 $P(T_2 \vee T_3 | T_1)$)

T2					T3				
Initiator or primary event	Heat radiation (kW/m ²) & Distance (m)	Ln _{ref}	Probit value (Y)	Probability (P)	Heat radiation (kW/m ²) & Distance (m)	Ln _{ref}	Probit value (Y)	Probability (P)	
T1	50 (37)	3.738	5.635	0.737	11 (118)	5.44 6	2.481	0.0059	

349 Note: T = Tank

350 **Table 5.** The probability of escalation of domino effects caused by T₁ tank failure if (
 351 $P(T_3 | T_2) \wedge P(T_3 | T_1, T_2)$)

Initiator or primary event	T3			
	Heat radiation (kW/m ²) & Distance (m)	Ln _{ref}	Probit value (Y)	Probability (P)
T2	50 (37)	3.738	5.635	0.737
T1 & T2	61	3.514	6.049	0.852

352 Note: T = Tank

353 Therefore, according to the above, the results can be presented in the following table.

354 **Table 6.** Conditional probability of tank 3 due to fire or safety of tanks 1 and 2

Row	T1	T2	T3
1	Fire	Fire	Fire

2	Fire	Safe	Safe
---	------	------	------

355 Note: T = Tank

356 Also, it can be concluded that:

$$357 P(U) = P(T1)P(T2|T1)P(T3|T2, T1), \quad (17)$$

358 Here P (U) is the joint probability. The chronological or sequential probability sequence of
 359 events will also be T₁, T₂, and T₃. It is noteworthy that, if the domino effect does not occur, there
 360 is still a possibility of an accident in T₃, which is the initial probability of T₃. Therefore, L-NOR
 361 gates were used, the results of which can be seen in table 7. Conditional probabilities between
 362 nodes in the previous step were calculated using the probit equations and used together with the
 363 initial tank probabilities to complete the CPTs and update the probabilities. Table 7 shows the
 364 probability of a domino accident caused by a pool fire using the BTA and FBN methods at the
 365 first and second levels.

366 **Table 7.** Probability of a domino accident caused by a pool fire in the first and second level

Method	P _{leak}	First level	Second level
BTA	7.2890E-3	0.0126073650	0.0116507438
FBN	4.1266E-3	0.0071472631	0.0090630640

367 Note: BTA = Bow-Tie analysis; FBN = Fuzzy bayesian network

368 The results of the Domino effect sensitivity analysis based on the RoV method are shown in Fig
 369 7. Three nodes are in the same direction and line, but due to a better representation of the causal
 370 relationships between them were drawn with a slight change. According to the results, in case of
 371 fire in tank T₁ and co-occurrence (T₁ and T₂), RoV values for tank T₂ and T₃ were equal
 372 (101.989, 138.913) and (57.234 and 77.730), respectively.

373 4. Discussion

374 The present study provided an approach for analyzing domino effects and risk assessment using
 375 FBN. In this study, we tried to reduce uncertainty by using FBN and modifying CPTs. As
 376 mentioned earlier, there is uncertainty in the various stages of risk assessment studies.
 377 Markowski et al. (2010) discussed in a study the sources and types of uncertainty in process
 378 safety analysis (PSA) as well as methods to deal with them . Unfortunately, for some basic
 379 events, there is no failure rate or it is not highly reliable . The use of fuzzy logic and expert
 380 opinions can address this problem. BN is a reliable method in evaluating process safety analysis
 381 that has features such as graphical representation and strong reasoning , which will be discussed
 382 further below.

383 The study of domino accidents has become an interesting field for researchers due to its
 384 importance in various industries, especially process industries. There are different methods for
 385 estimating domino effects. In this study, probit methods, consequence modeling, and CPT
 386 modification with L-NOR gates were used to investigate the domino effects. Kadri et al. (2013)
 387 proposed a hybrid method that quantitatively evaluates the effects of a domino event using
 388 probabilistic models and physical equations . Kourniotis et al. (2000) examined a statistical
 389 approach to analyze the domino effect. In this approach, past events were statistically analyzed
 390 to better understand the pattern of dominoes, consequences, and materials, and the results were
 391 updated based on new information about the accident using Bayesian inference . Cozzani and

392 Salzano's approach was to analyze the domino effect of excessive blast pressure using probit
393 models . Abdolhamidzadeh et al. (2010) proposed a simulation-based method. This methodology
394 is called FREEDOM and can evaluate very complex and nonlinear systems but can not manage
395 more than a few uncertain parameters . In a study, Khakzad and Reniers (2017) estimated the
396 risk of dominoes caused by tank fires and suggested the best design and location of tanks
397 according to various factors in the study using BN and analytic hierarchy process (AHP)
398 methods .

399 In this study, the domino effects of three tanks containing methanol with similar volume and
400 characteristics that were located in the same direction and distance were investigated. The results
401 showed that in case of fire in the first tank, the first and second levels of dominoes occur and the
402 second and third tanks are involved, respectively. The amount of heat radiation exceeds the
403 threshold and escalation effects will occur.

404 Various studies have provided different values for the threshold, ranging from 9.5 to 38 kW/m² .
405 If a higher heat radiation threshold value is considered between the storage tanks, the safer
406 distances will be higher and the results will be more conservative. The study of Cozzani et al.
407 (2006) also considered the TTF in determining this threshold that this failure time is affected by
408 active and passive control barriers. Lees also considered 37 kW/m² as the TV . Irrational
409 consideration of this threshold will lead to a loss of resources and increase costs while also
410 providing higher safety. Therefore, the threshold or intensification threshold in this study, like
411 the study of Cozzani et al. (2006) for atmospheric storage tanks, was considered 15 kW/m² . If
412 the heat radiation is less than this value, a domino accident will not occur. In this study, the
413 escalation vector was greater than the TV.

414 The important point is that even if the domino effect does not occur, there is still the possibility
415 of an accident in the tanks. Therefore, P_{leak} in the studied tanks was equal to 0.00012 which was
416 obtained from the results of risk assessment. Despite the many advantages of BN, such as the
417 ability to process uncertainties over conventional methods, it also has disadvantages such as the
418 difficulty of determining CPTs . In this approach, L-NOR gates were used to modify the
419 structure of CPTs . If this type of gate was not used in studies, the size of CPTs will be much
420 larger and the calculation of probabilities will be very complicated .

421 In this study, a comparison between BTA and FBN was performed to analyze the domino
422 effects. Given the advantages of the FBN approach in reducing uncertainty and dynamism, it can
423 be said that this approach provides more realistic results in risk assessment and analysis of
424 domino effects. Considering events with common cause failures (CCFs) and conditional
425 probabilities in BN were other advantages . While FTA and BTA statically examine
426 probabilities, the FBN approach considers dynamic aspects while computing probabilities. FBN
427 results showed that defect or absence of permit and delay in inspection and incorrect job
428 description were important causes of methanol leakage. According to the human factors analysis
429 and classification system (HFACS) approach, the root of these basic events is the defect of
430 organizational and management factors .

431 5. Conclusion

432 In this study, a FBN-based approach was presented to analyze the domino effects of atmospheric
433 storage tanks. The variables affecting accident risk, and FTA and BTA approaches are dynamic

434 and static, respectively. Therefore, the use of BN, which is dynamic in nature and has unique
435 features such as considering conditional relationships between events, deductive and inductive
436 reasoning, makes the created model more realistic and reduces uncertainty. In this approach, as a
437 new topic in the study of domino effects, due to the initial probability of failure of each tank, L-
438 NOR gates were used to modify the structure of CPTs, and conditional probabilities between
439 nodes were calculated using probit equations. Thus, the BN model of the study can reduce
440 uncertainty and examine complex causal relationships and sequential dependent failures.

441 On the other hand, the lack of a database for different failures, numerous social and cultural
442 differences, and different equipment specifications, always make systems uncertain. Therefore,
443 the use of fuzzy logic in this study to calculate the failure rate helped reduce uncertainty. In this
444 approach, all factors affecting the occurrence of consequences, including organizational,
445 management, human, and process factors were examined. The results of a case study showed that
446 the use of L-NOR gates and their mapping to BN reduced the uncertainty, complexity, and size
447 of CPTs. FBN and L-NOR gate combination is an effective way to evaluate the reliability of
448 tanks.

449 The probabilities of occurrence in FFT and BTA results were greater than the FBN in DRA and
450 domino analysis. Therefore, considering the characteristics of the FBN approach, the results
451 were more realistic than the FFT and BTA results.

452 **Disclaimer:** None

453 **Declarations of interest:** None

454 **Acknowledgments**

455 This study is a part of a PhD dissertation which was approved by Shahid Beheshti University of
456 Medical Sciences and was supported by National Petrochemical Company (NPC) of Iran in one
457 of the petrochemical industries located in Assaluyeh (Bushehr).

458 **References**

459 **Fig 1.** The usual BN.

460 Note: X = Node.

461 **Fig 2.** Arrangement of tanks and their position in the studied petrochemical plant.

462 **Fig 3.** The framework of the proposed method.

463 Note: AFFP = aggregated fuzzy failure possibility; BaN = barrier node; BN = bayesian network;
464 CFP = crisp failure probability; CN = central node; FBN = fuzzy bayesian network; IE =
465 intermediate event; IN = intermediate node; L-NOR gate= leaky noisy OR gate; MN = main
466 node; Pleak = leak probability; RN = root node; RoV = ratio of variation; TE = top event; Y =
467 probit value.

468 **Fig 4.** Bow-Tie diagram for atmospheric storage tanks.

469 Note: X = basic event; I = intermediate event; The full colour version of this figure is available
470 online.

471 **Fig 5.** Heat radiation caused by pool fire according to the distance from the accident site

472 **Fig 6.** Space affected by pool fire radiation.

473 Note: The full colour version of this figure is available online.

474 **Fig 7.** Sensitivity analysis of the domino effect of the studied tanks, (a): Overview, (b, c):

475 Sensitivity analysis of T1 and T2 tanks separately and together.