Laboratory experimental study of ocean waves propagating over a partially buried pipeline in a trench layer

Ke Sun¹², Jisheng Zhang¹², Yuan Gao¹², Dong-sheng Jeng²³, Yakun Guo⁴ and Zuo-dong Liang³

¹ State Key Laboratory of Hydrology Water Resources and Hydraulic Engineering, Hohai University, Nanjing 210024, China
² College of Harbor, Coastal and Offshore Engineering, Hohai University, Nanjing 210024, China
³ School of Engineering and Built Environment, Griffith University Gold Coast Campus, Queensland, 4222, Australia
⁴ School of Engineering, University of Bradford, Bradford, BD7 1DP, UK

Highlights:

- Provide the first set of comprehensive experimental data for wave-induced pore pressure around a partially backfilled pipeline in a trench layer.
- Systematically investigate the effect of wave characteristics on transient pore-water response in the trench layer near the partial-buried pipeline.
- Integraisly examine the effect of trench depth and backfill thickness on oscillatory pore-water pressure around the partial-embedded pipeline.

Abstract: Seabed instability around a pipeline is one of the primary concerns in offshore pipeline projects. To date, most studies focus on investigating the wave/current-induced response within a porous seabed around either a fully buried pipeline or a thoroughly exposed one. In this study, unlike previous investigations, a series of comprehensive laboratory experiments are carried out in a wave flume to investigate the wave-induced pore pressures around a partially embedded pipeline in a trench layer. Measurements show that the presence of the partially buried pipeline can significantly affect the excess pore pressure in a partially backfilled trench layer, which deviates considerably from that predicted by the theoretical approach. The morphology of the trench layer accompanied with the backfill sediments, especially the deeper trench and thicker backfill (i.e., $b \geq 1D, e \geq 0.5D$), provides a certain degree of resistance to seabed instability. The amplitude of excess pore pressure around the trench layer roughly exhibits a left-right asymmetric distribution along the periphery of the pipeline, and decays sharply from the upper layer of the trench to the lower region. Deeper trench depth and thicker buried layer significantly weaken the pore-water pressures in the whole trench area, thus sheltering and protecting the
submarine pipeline against the transient seabed liquefaction.

Keywords: wave-seabed-pipeline interaction; soil response; trenched pipeline; partially buried
1. Introduction

Submarine pipelines, the most widely-used and reliable transportation carrier for offshore oil and gas, are installed in both offshore and nearshore environments with different layouts. They could be laid on the seabed surface, buried in the sediment or embedded in the trench with/without backfilling deposits. Under these conditions, the phenomenon of wave-induced deformation and instability of a porous seabed plays an important role in the design of submarine pipelines because it might potentially compromise the safety of underwater pipelines located either on or in the submarine sediments and result in severe consequences (Christian et al., 1974; Herbich et al., 1984; Palmer and King, 2008; Sumer, 2014a). During cyclic wave loadings, some buried pipeline may float, when the specific weight of the pipeline is smaller than that of surrounded liquefied sediments (Sumer et al., 1999, Damgaard and Palmer, 2001; Damgaard et al., 2006). On the other hand, some pipelines may sink into the seabed when the specific weight of the pipeline is larger than that of the neighboring liquefied deposits (Dunlap et al., 1979; Sumer et al., 1999). Some may even undergo horizontal and vertical displacements after continuous exposure to the wave-current combined actions (Damgaard et al., 2006). Numerous failures of submarine pipelines have been reported to be linked to wave-induced seabed instability which is vulnerable to liquefaction (de Groot and Meigers, 1992; Sumer, 2014b, c). Such failures could be catastrophic during severe storms or hurricanes. Due to its practical engineering importance, the interactions between waves/currents, a seabed and a pipeline have attracted great attentions among geotechnical and coastal engineers. A state-of-art review of recent research on the pipeline-seabed interactions exposed to waves and/or currents can be found in Fredsøe (2016).

When a submarine pipeline is involved, the problem of fluid-seabed interaction becomes more complicated, because the pipeline will disturb local flow field and sediment transport. Numerous investigations for the wave-seabed-pipeline interactions have been carried out since 1970. MacPherson (1978) and McDougal et al. (1988) proposed analytical solutions for an infinite seabed, which exhibits perturbations in the pore pressure field around a marine pipe. Monkmeyer et al.
(1983) developed an algorithm with the concept of “image pipe”, which can be applicable to a soil layer of a finite thickness. Magda (1992) extended Okusa’s (1985) model to investigate a fully buried pipeline in a seabed by solving the Laplace’s equation and consolidation equation. Compared with the previous model without consideration of a submarine pipeline (Okusa, 1985), the perturbation due to existence of a subsea pipeline was included in the model of Magda (1992).

In addition to analytical approximations, several numerical models have been proposed for the problem. Among these, Cheng and Liu (1986) applied a boundary integral equation model to solve the wave-induced soil response around a buried pipeline. In their study, the trench is surrounded by two impermeable rigid walls and u-p approximation (u represents the soil displacement, p is the pore-water pressure) is adopted. Magda (1996) considered a similar case with a wider range of the degree of saturation, but based on consolidation model (i.e., quasi-static soil behavior is considered). Jeng and his co-workers applied their two-dimensional finite element model (Jeng, 2003) to various conditions with a pipeline, including Gibson soil (Jeng and Lin, 1999), effect of a cover layer (Wang et al., 2000), internal stresses of the pipeline (Jeng, 2001; Jeng et al., 2001). The model was extended by Gao et al. (2003a) and Gao and Wu (2006) to investigate the cases with non-linear wave loading. Dunn et al. (2006), applying the poro-elastoplastic model (Chan, 1988), conducted a systematic investigation of wave-induced soil liquefaction caused by residual pore pressure around a fully embedded pipeline. Luan et al. (2008) further considered the contact effects between pipeline and soil with dynamic soil behavior. In their study, three different types of trench layers, i.e., square, rectangular and triangular, were considered. All these studies only considered a fully buried pipeline. Zhao and Jeng (2014) and Zhao et al. (2014) were the first attempt for considering a partially buried pipeline in a trench layer with a natural backfilling process. Recently, Zhao and Jeng (2016) further investigated the effects of backfill in trench layer on the seabed liquefaction and proposed a relationship between the critical backfill thickness and wave steepness and other wave and soil characteristics. In their numerical studies, residual liquefaction was considered. Lin et al. (2016) developed an integrated FEM to investigate transient liquefaction occurrence nearby the trenched pipeline with different backfill depths. This
framework was further extended to the case subject to combined wave and current loadings in two-dimension and three-dimension (Duan et al., 2017a, b). In these studies (Zhao and Jeng, 2016; Duan et al., 2017a), a simplified approximation process for the design of the critical thickness of backfill depth with given wave characteristics and soil parameters is proposed for the protection of the pipeline against soil liquefaction.

Apart from theoretical approaches and numerical modeling studies, laboratory experiment is another common methodology to reveal the physical process and its mechanism of the wave-soil-structure interactions. In general, three different experimental methods have been reported in the literature. First, one-dimensional compressive tests are conducted in a vertical cylinder (Zen and Yamazaki, 1990a; 1990b; Chowdhury et al., 2006; Liu et al., 2015; Liu and Jeng, 2016). With this experiment set-up, it is possible to install ten or more pore-water pressure transducers in the soil column, which could provide more measurable data to resolve the vertical profile of pore pressure distribution in the seabed, especially in the region near the seabed surface. However, this type of experiment can only capture the response of soil to oscillatory pore pressure in time domain, not in spatial domain, because only oscillatory dynamic pressures are applied at the top of the cylinder and no shear strain is generated in the soil column.

The second type of experimental approach is the geo-centrifugal wave tests (Sassa and Sekiguchi, 1999; 2001; Miyamoto et al., 2004). In this approach, the stress level in the soil at the experimental model under the environment of several times of gravitational acceleration is the same as that of the prototype. This approach can simulate the pore-water pressure fluctuation in both spatial and time domains, although the wave generation in the experiment may not represent the realistic ocean waves and only limited numbers of measurements can be taken. Furthermore, complicated engineering problems such as the current problem with a trench layer cannot be simulated in geo-centrifugal tests.

The third type of experimental approach is wave flume test, which have been commonly used by coastal engineering researchers. Turcotte et al. (1984) were the first to conduct experiments for
the wave-induced pore-water pressure around a buried pipeline in a wave flume. Sumer et al. (1999) carried out a series of laboratory experiments to explore the wave-induced seabed response under progressive waves, and then the sinking/floatation of marine pipelines in the liquefied soil. Sudhan et al. (2002) carried out the experimental investigation to analyze wave-induced pressure on a pipeline fully buried in a permeable seabed with different burial depths. They found that high-pressure values took place at the top and low-pressure values appeared at the bottom. Teh et al. (2003; 2006) studied the sinking/floatation of pipelines in a liquefied seabed. They demonstrated that the pipeline behavior on a mobile seabed strongly depended on specific gravity of itself and liquefied soil characteristics, but not on the wave parameters. Sumer et al. (2006) further extended their experiments to explore the liquefaction due to the buildup of pore pressure around a buried pipeline. Their research work further indicated that the accumulation of pore pressure and the residual liquefaction were influenced by the boundary condition of pipeline surface. In general, liquefaction occurs in the top layer and develops downwards with the absence of the marine pipeline, whereas under the presence of the pipeline, liquefaction occurs at the bottom of the pipeline and develops along the perimeter of the pipeline upwards. Recently, a series of wave flume tests were carried out (Gao et al., 2002; 2003b; 2007; 2011) to examine the fluid-pipeline-seabed interaction mechanism for the lateral stability of un-trenched pipelines as well as partially embedded pipelines for various loading conditions, e.g., the wave action and/or the current action. Pan et al. (2007) conducted large-scale wave flume experiments to investigate various parameters on the pore pressure around a submarine pipeline with a shallow burial depth due to regular waves, such as relative water depth, relative burial depth and scattering parameter. Zhou et al. (2011) conducted a series of physical modelling tests in wave flume on soil responses with a pipeline either half buried or resting on the seabed under regular waves or combined with currents. Recently, Yang et al. (2012a, b; 2014) conducted laboratory experiments to investigate the stability of marine pipeline due to regular and irregular wave-induced scour. They found that attaching a rigid spoiler at the top of the pipeline could greatly accelerate the scour around the pipeline as well as the so-called self-burial (Yang et al., 2012a, b). When a flexible rubber was placed under the pipeline, no scour around the pipeline would occur if the length of the rubber reaches
Besides the above experimental approaches, based on some practical projects, such as PIPESTAB Project, DHI Research Program and AGA Project, the interaction between wave-seabed around an unburied-pipeline was investigated by means of mechanical loading tests (Palmer et al., 1988; Allen et al., 1989). In this approach, wave growth process and horizontal propagation is neglected. However, the above physical modelling studies are impossible to simulate the pore pressure in the trench layer around a partially buried pipeline, which can be easily achieved through the wave-flume experiments.

In summary, to reproduce the problem of the practical wave-soil-pipeline interaction within a trench layer, wave flume tests seem to be a more appropriate approach, although it has some limitations and shortcomings.

The aforementioned studies are primarily concerned with pore-water pressures around an underwater pipeline, either directly resting on the seafloor or shallowly/fully buried in the seabed, in which the soil responses are well acknowledged. While rare attention has been paid to the wave-induced responses of trench layer nearby a partially backfilled pipeline. The complicated seafloor profile combined with the bare pipeline segment will strongly affect the local flow and consequently the sediment transport. However, in the engineering practices, the submarine pipelines are typically deployed in a trench with partially backfill soil to strengthen the stability and reduce costs simultaneously (Du and Zhao, 2015).

The first set of experimental data for wave-induced pore pressure around a partial-buried pipeline in a trench layer was reported by Zhai et al. (2018). However, in their experiments, only four measuring points were deployed around the periphery of the pipeline in total, in which the pore pressure variation in the trench layer nearby partially embedded pipeline cannot be captured. Therefore, to have a better understanding of the whole physical process and mechanism, a series of comprehensive experiments are desired for pipeline engineers and researchers, which
motivates this study. Main objectives of this paper are to examine the wave-driven pore-water pressure in trench layer around a partially buried pipeline through physical modelling, including:

(i) Providing a comprehensive experimental database for the wave-induced pore-water pressures in the vicinity of a submarine pipeline partially buried in a trench layer.

(ii) Consideration of partially buried pipeline in a trench layer, in which the pore pressure may deviate considerably from that predicted by the poro-elastic models (e.g. Liang and Jeng, 2018a, b);

(iii) Investigation of the effects of wave characteristics on trench layer, where the local flow will be definitely disturbed by the complicated seabed-pipeline configuration;

(iv) Exploration of the effects of backfill thickness and trench depth in the vicinity of the partially embedded pipeline, where the sediment mobility and soil instability would be suppressed.

2. Experimental setup

A series of wave flume tests are carried out to investigate the process of the wave-driven pore-water pressure around a trenched pipeline with partially sediment backfilling. To the authors’ best knowledge, this is the first comprehensive experimental work for such a problem in the literature, and expected to provide invaluable data for future studies in the field.

2.1 Facilities and instruments

The experiments are conducted in a wave flume having the dimension of 55 m (long) × 1.3 m (high) × 1.0 m (wide) at Hohai University. As shown in Figure 1, the wave flume is equipped with a hydraulic piston-type wave maker at the upstream end and a sponge-type wave absorber at the downstream end to dissipate the incoming wave energy and thus minimize the wave reflection effect. The wave maker is capable of generating regular waves with wave period of 0.6 sec - 2.5
sec and the maximum wave height of 0.2 m. A sediment basin located at a distance of 25 m away from the wave generator with the size of 2.0 m (length) × 1.0 m (width) × 0.58 m (depth), is manufactured for the experiments specifically. The surrounding walls and the bottom of the test sand-pit are made of rigid and impermeable concrete. As shown in Figure 1, the pit is elevated 0.25 m in height, based on the original 0.33 m depth, by introducing two artificial trapezoids (false floors) on both ends of the sediment basin. The false floors at each side comprises a 1:10 slope plywood ramp and a 7.5 m-long false floor, keeping off both the generation of reflection wave and progressive wave deformation to ensure smooth transition of waves to the utmost before propagating through the measurement section.

In the experiments, the wave-induced pore-water pressure variation and water surface elevation around a pipeline placed in a backfilled trench are measured simultaneously by using the pore pressure sensors and wave height gauges. The CY203/CY303 type miniature pressure transducers (6 mm in outer-diameter) are designed and manufactured by Chengdu Smart World Technology CO.LTD. The measurement range of the transducer is 30kPa with accuracy of ±0.1% Full Scale. Three pressure transducers are installed to record wave-driven pore-water pressures in the soil along the central line at different depths of 0.23 m, 0.27 m, and 0.40 m below the seabed surface. Another eight pressure transducers, deployed around the pipeline circumference with a fixed interval of π/4, generally record the hydrodynamic pressure when exposed to water and occasionally obtain the pore-water pressure when buried in the soil. The wave height gauges, designed by Nanjing Hydraulic Research Institute with the measurement range of 0.60 m and the measurement precision of 0.1 mm, are located along the central axis of the wave flume, containing one far-field gauge to measure the incoming wave characteristics and four near-field ones to explore the wave evolution propagating through the porous seabed. A remote computer connected to the servo system and acquisition system is employed to sample the signals of wave height gauges and pore pressure transducers synchronously, with sampling frequency of 50 Hz. The locations of the measurement device are indicated in Figure 1.
2.2 Properties of seabed sediments

The sandy sediment with mean particle size of \( d_{50}=0.173 \) mm, is used as the seabed material (for both trench-layer and backfill-layer) in the experiments, and its main physical properties are listed in Table 1. In Table 1, the submerged specific gravity of soil is defined as \( \gamma' = (1 - n)(\gamma_s - \gamma_w) \) where \( \gamma_w \) is the unit weight of pure water, \( \gamma_s \) represents the unit weight of soil grains and \( n \) is the soil porosity. The mean grain size and grading curve of sandy sediment is measured with Mastersizer 3000E, while permeability coefficient is measured by the constant head permeability test. Water is introduced into flume and left for 3 days before experiment is run to allow the subsidence of the seafloor is complete and the variation of void ratio is negligible. This is also to ensure the seabed to be almost fully saturate. As mentioned previously, because laboratory experiments can be performed in a wave flume with natural waves/currents, many liquefaction experiments are based on the small-scale wave flume experiments with 1 - g environment rather than N – g environment made by centrifuge tests. The purpose of wave flume tests is mainly to capture the residual pore pressure as well as the response of seabed to pore pressure oscillation. However, the drawback of wave-flume experiments is that the stress level cannot be simulated as the prototype stress level in the seabed. Thus, in the present tests, no scaling law for seabed sediments is adapted, because the model was regarded as a small prototype. The seabed thickness is maintained at 0.58 m for all tests.

2.3 Characteristics of submarine pipeline

A PMMA (polymethyl-methacrylate) pipeline with the external diameter of 0.1 m is used to model the submarine pipeline, as illustrated in Figure 1, laying at the seafloor perpendicularly to the direction of wave propagation. To eliminate the side effects, the pipeline length is chosen to be 0.96 m, slightly smaller than the internal width of wave flume. Therefore, the gap between the end of pipeline and the wall of the flume is too small to generate large score holes and notable flow disturbance. This would simplify the simulation of wave-seabed-structure interaction as a two-dimensional problem. Besides, the pipeline movement is thoroughly constrained through a
steel frame, including translational motion and rotation. As mentioned before, eight pore-water pressure transducers are equally spaced around the pipeline circumference at the center section, as shown in Figure 1.

The weight of the pipeline has been adjusted to model the typical submerged weight of actual pipeline. According to the gravity similarity parameter \( G = W_s / \gamma' D^2 \) proposed by Gao et al. (2003), where \( W_s \) is the submerged weight of pipe. Hence, the dimensional analysis of model and prototype can be expressed by \( \lambda G = \frac{\lambda W_s}{\lambda \gamma' \lambda_D^2} \), where \( \lambda \) represents the ratio of the parameters of model to that of prototype. As aforementioned, the model pipe is made of PMMA, with length of 0.96 m, and the outer diameter and inner diameter are 0.1 m and 0.08 m respectively. Herein, the submerged weight of the pipe is 4.985 N/m.

2.4 Conditions of incident waves and soil patterns

Due to the unpredictability and uncertainty of the storm waves, it is difficult to obtain accurate data in the field marine environment. This makes laboratory experiments of pipeline model be of particular importance. Extreme care is taken to make sure that the behavior of model simulates that of the prototype as accurately as possible.

In the wave-seabed-pipeline coupling problem, three non-dimensional numbers relative to flow characteristics can be deduced. They are: (1) the Froude Number \( \text{Fr} = \frac{U_m}{\sqrt{gD}} \), which represents the ratio of inertia force to gravitational force; (2) the Keulegan-Carpenter Number \( KC = \frac{U_m T}{D} \), which controls the generation and development of vortex around pipeline, and is related to the hydrodynamic force acting on the pipe under wave motion, and (3) the Reynolds Number \( \text{Re} = \frac{U_m D}{\nu} \), which is the ratio of inertia force to viscous force. Here \( U_m \) is the flow velocity; \( D \) is the pipe diameter; \( T \) is wave period and \( \nu \) is kinematic viscosity of water.

According to the principle of similarity from the Froude number \( \lambda_{\text{Fr}} = \frac{\lambda U_m}{\lambda g \lambda_D^{1/2}} = 1 \), where \( \lambda \)
represents the ratio of the parameters of model to that of prototype, since $\lambda_g = 1$, the following relationship should be maintained:

$$\lambda_{U_m} = \lambda_D^{1/2},$$

which could be further rendered to

$$\lambda_T = \frac{\lambda_D}{\lambda_{U_m}} = \lambda_D^{1/2}.$$

Therefore,

$$\lambda_{KC} = \frac{\lambda_{U_m} \lambda_T}{\lambda_D} = 1,$$

This indicates that Fr and KC numbers can be satisfied concurrently during the model simulation.

In the natural marine environment of ocean wave with a free surface, the effective range of viscosity force is restricted to the immediate vicinity around the particles and hardly affects the overall motion of the fluid, hence the viscosity force is negligible while the gravity and inertial force predominates the fluid motion and consequently the interactions of wave-seabed-pipeline.

Since Fr and Re numbers cannot meet the principle of similarity synchronously during the laboratory experiments, it is reasonable to yield the wave-seabed-pipeline couple problem to the scaling law of the Froude number and to make allowance for the deviation in the Reynolds number scale. Small-scale experiments have limited values because the Re is usually much higher in the prototype than in the experiments. The value of Fr and KC numbers of coastal sediments in South China Sea varies between 0-0.5 and 0-20 respectively (Gao et al., 2003), which is within the range used in the present laboratory experiments.

The experimental conditions are listed in Table 2. For a fully buried submarine pipeline (i.e., trench depth $d$=backfill depth $e$), the wave height ($H$) varies from 0.06 m to 0.14 m with an interval of 0.02 m, and the wave period ($T$) ranges from 1.2 sec to 1.8 sec where set 0.2 sec as a span. For the
284 partially buried pipeline, the incident wave is only adopted as $H=0.12 \, \text{m}$ and $T=1.6 \, \text{sec}$. The water depth is kept at 0.40 m above the sediment basin for all tests.

286 Apart from the trench depth, the side slope and bottom width will definitely affect the soil response in the trench soil layer. However, limited by submarine repose angle of model sand particle, the gradient of the trench chosen in this study is 1:2, where trench depth is the dominant factor whereas the bottom width of the trench has the minus impact according to the preliminary understanding. Therefore, this study places priorities on the trench depth as well as the backfill thickness, instead of the side slope and bottom width.

2.5 Test procedures

The procedure of test is as following:

(1) Place the facilities and instruments: Eight pore pressure transducers are installed in the drilled holed around the pipeline covered with waterproof tape, and another three are strapped at the steel frame located at the bottom of sediment basin. Four wave height gauges are deployed along the central axis of the wave flume. As the pore-pressure transducers are equipped with sand filters, they must be submerged in water for at least 24 hours to ensure air would be completely exhausted.

(2) Fulfill the sediment basin: Prior to the experiments, the large amount of sand is firstly poured into the soil-mixture tank, and water is gradually added into the tank while continuously and thoroughly stirring until it reaches the homogeneous liquid state. The mixture is then pumped into the test section where it is allowed to consolidate for at least 3 days. Finally, a soil layer of about 0.58 m in thickness is produced.

(3) Place the submarine pipeline: The trench (1:2 side slope with 0.16 m in bottom width) is dredged via iron plate as soon as the consolidating soil layer surface is leveled with the false floor. The pipeline is then placed at the central bottom of the trench.
(4) **Backfill the trench layer and fill the flume:** The trench is backfilled with prescribed backfill material to an intended thickness. The flume is then filled with clear water as slowly as possible to the designed water depth. Extreme care should be taken to ensure that the soil configuration, especially the turning point from platform to slope, is not washed away. The backfill soil under hydrostatic pressure is left to settle and consolidate for 3 days.

(5) **Switch on the wave maker.**

(6) **Sample the statistics of pore pressure and wave height:** The duration of data collection is at least 120 sec after the oscillatory soil response in sandy seabed is fully developed and reaches to equilibrium state.

(7) **Switch off the wave maker.**

(8) **Empty the wave flume and clean the sand pit.** Repeat step 2 to step 7 for the next test.

3. **Comparison with the numerical model (Liang and Jeng, 2018a, b)**

In this section, the laboratory experiment is compared with the previous numerical model for wave-soil interactions around a partially buried pipeline (Liang and Jeng, 2018a, b). In the wave model, the RANS equations are employed to simulate the progressive wave motion over a porous seabed near the trench layer; while in the seabed model, the Biot's consolidation equation is solved to investigate the distribution of pore pressure, effective stress and soil displacement of the seabed in the trench around a partially backfilled pipeline. With the consideration of one-way coupling process, the integrated numeral model is established with the OpenFOAM.

Figure 2 shows the simulated and the measured water surface elevation ($\eta$) versus time, recorded by wave height gauges $h_4$, for Test 10 and Test 49. Figure 3 shows the comparison between the simulated and the measured normalized amplitude of excess pore-water pressure ($|u_e|/p_0$) around the outer surface of submarine pipeline ($\theta$) for Test 10 and Test 49. Test 10 is the case of a fully buried pipeline (where trench depth is $d=0.15$ m and backfill thickness is $e=0.15$ m), while Test
49 is a partially buried pipeline in a trench (in which $d=0.2 \text{ m}$, $e=0.05 \text{ m}$). For both test cases presented in the figure, the simulated wave height and excess pore-water pressure overall agrees with the collected data in the experiments.

Another comparison is for the normalized amplitude of transient pore-water pressure variation ($|u_e|/p_0$) versus time at various measurement points beneath the pipeline, which are not available in the previous literature (Zhai et al., 2018). As illustrated in Figure 4, the dimensionless amplitude of excess pore pressure profile obtained from in the numerical model (Liang and Jeng, 2018) overall agrees with the experimental data.

4. Results and Discussions

In this study, 71 tests are conducted in total. Among these, Tests 1-40 are primarily performed to investigate the effects of wave parameters (defined in terms of wave height and wave period) on pore pressure in trench layer. Tests 41-71 are mainly conducted to explore the effects of seabed configurations (consisting of backfill thickness as well as trench depth on soil response around a partially backfilled pipeline in the trench. Detailed information of tests is listed in Table 2.

4.1 Effect of wave parameters

To systematically understand the influence of wave parameters on soil responses around a buried pipeline, twenty incident waves, the wave height ($H$) ranging from 0.06 m to 0.14 m with an interval of 0.02 m and the wave period ($T$) varying from 1.2 sec to 1.8 sec with 0.2 sec as a span, are tested for each pipeline-seabed configuration.

Based on the wave and soil characteristics used in the present experiments, transient mechanism dominates the seabed response rather than residual mechanism as reported in Jeng and Seymour (2007) and Jeng (2018). That is, the wave-induced excess pore pressure oscillates periodically and hardly ever accumulates in a sandy seabed. Such phenomena occurred in all experimental tests conducted, which may be ascribed to the fact that the grain size of seabed sediments used in the
The present model is too large ($d_{so}=0.173$ mm) to generate the residual excess pore-water pressure. Therefore, the excess pore pressure induced by the previous wave loading dissipates quickly and fully before the next wave arrives, thus does not accumulate in the sandy seabed.

Figure 5 shows the depth profile of amplitude of normalized excess pore-water pressure ($|u_e|/\sigma_0'$) along the normalized soil depth ($z/h$) downward from the trench surface to seabed bottom. Here, $\sigma_0' = \gamma'z(1 + 2K_0)/3$, where $K_0$ is the coefficient of lateral earth pressure at rest. Compared with the hydrostatic water pressure, the weight of the submarine pipeline is considered to be small, therefore, the effects of pipeline weight on the initial effective stress is ignored as the first approximation. In the figure, the pore-water pressure measured at pipeline bottom corresponds to the value of relative depth $z/h=0.357$ with the trench depth $d=0.2$ m and backfill depth $e=0.1$ m, and three pore pressure transducers are installed at different depths 0.03 m, 0.07 m and 0.20 m ($z/h=0.411$, 0.482 and 0.714) downward from the trench bottom respectively.

Figure 5 shows that the amplitude of excess pore-water pressure attenuates more significantly in the upper layer of the seabed than damps in the lower layer, which is primarily due to the effect of permeability and deformation properties of submarine sediments. Furthermore, a criterion reported by Zen and Yamazaki (1990a) that includes the initial stress due to pre-consolidation is used to determine the oscillatory soil liquefaction, which is well known that soil liquefaction will occur when $|u_e| = \sigma_0'$. The present results indicate that the soil is not liquefied, even with the large wave height and long wave period (e.g., $H=0.14$ m and $T=1.6$ sec, or $H=0.12$ m and $T=1.8$ sec). Such phenomenon is observed in all tests and could be attributed to the large-size and non-cohesive sediment particles.

Figure 6 presents the vertical distribution of the amplitude of wave-induced excess pore-water pressure with a certain seabed configuration of 2D-depth-trench and 1D-thickness-backfill, for various wave heights. The results reveal that the excess pore-water pressure amplitude increases as the wave height increases, and the amplitude attenuation for the excess pore-water pressure towards the seabed bottom is greater for wave with larger wave height. Besides, the amplitude
of oscillatory pore pressure component recorded at p9 (relative depth \( z/h = 0.411 \)) is slightly larger than that at p1 (relative depth \( z/h = 0.357 \)), especially for the cases with larger wave height (e.g., \( H = 0.12 \) m, 0.14 m) and longer wave periods (e.g., \( T = 1.6 \) sec, 1.8 sec). Such a phenomenon differs from the law of monotonous attenuation of pore pressure distribution as the increment of seabed depth without any presence of the pipeline. When a pipeline exists in the submarine environment, the local seepage flow scatter and consequentially the excess pore-water pressure distribution across the soil depth is perturbed. Thus, the energy of the pore pressure within sediments that transferred from wave-induced seafloor pressure, propagates in the neighborhood of the underwater pipeline via several approaches. They might transmit through the soil particles downward directly from the shallow region to the deep layer, or spread along the periphery of the pipeline until reach the pipeline bottom and subsequently downward to the seabed bottom. In the former case, the excess pore-water pressure transmitted through porous media attenuates sharply due to the friction effect and that through the outer circumference of the pipeline definitely dominates the stress distribution, following by the fact that excess pore pressure measured at p9 is smaller than p1. Nevertheless, in the latter case, especially for the wave with longer period and larger height where the damping rate of excess pore-water pressure energy inside the seabed is relatively slight. Therefore, the excess pore pressure delivered by sediment grains and that by outside surface of pipeline has the comparative magnitude. This might lead to the larger value recorded at p9 than p1. More detailed discussions will be provided in the latter section.

Variations of the non-dimensional amplitude of excess pore-water pressure \( (|u_e|/p_0) \) around the circumferential surface of pipeline under different wave heights are plotted in Figure 7. In these figures, \( p_0 \) is the amplitude of dynamic wave pressure at the surface of the mud-line, calculated by the linear wave theory \( p_0 = \frac{\gamma w H}{2 \cosh kd} \), and the points represent the excess pore pressures \( (|u_e|/p_0) \), which are measured radially from the center of the circle, with an equal interval of \( \pi/4 \), where p1 (\( \theta = 3\pi/2 \)), p3 (\( \theta = 0 \)), p5 (\( \theta = \pi/2 \)) and p7 (\( \theta = \pi \)) corresponding to the bottom, seaward, top, and shoreward edge of the pipeline, respectively (referring to Figure
1). The results presented in the figure are for the case, in which the trench depth of 1.5D and backfill thickness of 1.5D (the submarine pipeline diameter D=0.1 m). Figure 7 demonstrates that the dimensionless amplitude of excess pore-water pressure increases as the wave height increases. The effect of the wave height on excess pore-water pressure presents a positive correlation with the increasing wave height. However, the variation of the transient pore pressure amplitude is insignificant under the wave height generated in this study. In addition, the values of excess pore pressure oscillation measured at the upper half part of the pipeline (e.g., p4, p5, p6) almost have the same magnitude, possessing the largest quantity around the pipeline circumference. Nevertheless, the excess pore pressure oscillatory component recorded at the lower half part (e.g., p1, p2, p8) exhibits the minimum value. This observation is consistent with the conclusion of Pan and Wang (2007), in which the underwater pipeline is fully buried in the sediments with impermeable wall surrounded. That is, in a sandy seabed, higher pore pressure occurs at the pipeline top and the lower pore pressure appears at the bottom.

To further study the effect of wave period (T) on the soil dynamic responses around a partially buried pipeline, the case in which the trench depth kept as 2D and backfill thickness kept as 1D is taken as an example. Figure 8 displays the vertical distribution of the transient excess pore-water pressure recorded along the seabed depth straight beneath the pipeline. As illustrated in these figures, the excess pore pressure around the trenched pipeline increases with the increasing wave period, and generally decays from the surface to the bottom of the seabed. In this study, the water depth remains constant. According to the dispersion relationship of linear wave theory, when the water depth keeps unchanged, the wave with a larger period has a longer wave length. Thus, shorter wave-induced excess pore pressure attenuates faster with depth than that driven by the longer wave (see Figure 8). Moreover, the influences of wave period on the excess pore pressure response decreases as the wave period increases. Taking the case of wave height H=0.14 m, for example, the rising percentage of excess pore-water pressure measured at pipeline bottom reaches 33.5%, 20.2%, and 4.5% as the wave period increases from 1.2 sec to 1.4 sec, 1.6 sec and 1.8 sec. That is, the percentage gain of pore pressure declines with the increase of the wave length.
The normalized excess pore-water pressure variation around the pipeline circumference plotted in the form of scatter plot with the trench depth of 0.15 m and 0.20 m is represented in Figure 9, under various wave periods. Different from the effect of wave height, the amplitude of excess pore pressure increases considerably with the increase of the wave period. However, the effect of wave period on soil response decreases as wave period increases. This discrepancy is attributed to the fact that the non-dimensional parameter \( p_0 \) is calculated by the linear wave theory rather than the recorded data, which are not successfully measured in the experiments. Therefore, the normalized excess pore-water pressure amplitude seems to be insusceptible to the wave height, whereas be susceptible to the wave period. Taking Figure 9(d) as an example, as the wave period increases from 1.2 sec to 1.8 sec, the excess pore-water pressure recorded at p5 increases from 0.291 to 0.356, 0.401 and 0.424, leading to the percentage gain of 22.3%, 12.6% and 5.7%. Nevertheless, the dimensionless oscillatory amplitude of pore pressure at the top of the pipeline (recorded by p5) is approximately doubled or even trebled as great as the dimensionless quantity at the bottom (recorded by p1) similarly as Figure 7. Furthermore, under the same incident wave conditions, the magnitude of transient pore pressure measured at p3 (shoreward edge of pipeline) is slightly larger than that at p7 (seaward edge of pipeline). This can be ascribed to the sheltering effect of the submarine pipeline on the energy of wave stress propagating from upstream to downstream, causing the higher liquefaction potential at upstream side of pipeline.

### 4.2 Effect of backfill thickness

One of main objectives of this study is to explore the effects of backfill thickness and trench depth on the wave-induced pore pressures around a partially buried pipeline, which has no reliable and comprehensive experimental data currently available in the literature.

Figure 10 shows the scatter plots of the dimensionless excess pore-water pressure versus various seafloor configurations, including trench depth of (a) \( d=0.20 \) m and (b) \( d=0.15 \) m with non-backfill gradually increasing to full-backfill (set an interval for backfill thickness as a quarter of the pipeline diameter). The variation of relative buried depth \((e/D)\) has a significant impact on the variation of
excess pore-water pressure ($|u_e|/\sigma_0'$). When the submarine pipeline is entirely exposed to water
without any protection of backfill deposits, the pore pressure sensors recorded the hydrodynamic
pressure, representing almost same magnitude along the upper-periphery of the pipeline. With
the existence of overburden sediment, the obtained excess pore-water pressure experiences a
sharp decline when the pore pressure sensor is buried into the soil. This damping phenomenon of
wave-induced pore pressure oscillation is mainly due to the strong friction effect between soil
particles and pore water, which transfers energy from pore fluid to soil grains and attenuates
pressure fluctuation. The transient excess pore pressure keeps dropping off as the overburden
soil thickness continues to increase, whereas the attenuation degree of the transient excess pore
pressure declines. As aforementioned, the criterion of instantaneous liquefaction based on the
transient excess pore pressure and the initial vertical effective stress can be expressed as seabed
liquefaction will occur when $|u_e| = \sigma_0'$. In general, the seabed in the vicinity of pipeline is more
vulnerable to liquefaction as the backfill thickness decreases, as shown in Figure 10. This means
that a fully buried pipeline could be better protected against instantaneous seabed liquefaction,
compared with a partially backfilled pipeline. These results are consistent with previous research
reported by Palmer and King (2008) that compared to a pipe laid in an open trench, the pipe
embedded in a trench with sufficient thickness is more insulated from the threat of instability of
either the seabed or the pipeline due to the potential liquefaction.

In general, a trench layer with partially backfills is typically employed in engineering practice to
reduce the financial costs and accelerate the construction process compared to a fully backfilled
trench. Therefore, a critical backfill thickness for the resistance to seabed transient liquefaction is
urgently required for coastal engineering involved in the design for pipeline project. As sinking of
pipelines is a common concern in practical offshore engineering, it is assumed that the pipeline
could be completely prevented if there is no liquefaction taking place within the underlying soils.
Thus, Figure 10 (a) and (b) demonstrate that the bottom of the pipeline will be unstable and
damaged by the oscillatory liquefaction when the backfill thickness is less than 0.5D (i.e., e=0 and
e=0.25D). Whereas, this study shows that the partially buried trench will provide the pipeline the
full protection against the oscillatory liquefaction when the backfill thickness is larger than 0.5D. Figure 11 further presents the effect of relative buried depth (e/D) on the oscillatory amplitude of excess pore-water pressure (|ue|/p0), measured around the pipeline for the wave height of H=0.12 m and wave period of T=1.6 sec. The result reveals that the excess pore-water pressure undergoes a either mild or severe decline tendency with increasing relative backfill depth. The excess pore-water pressure at the pipeline bottom begins to decline for relative backfill depth increasing from 0 to 0.25. The excess pore-water pressure at p3 and p7 does not decrease until the relative backfill depth reaches 0.75, while the excess pore pressure at the top of the pipeline starts falling off after the relative backfill depth reaches 1.0. This is because, when the transducer is submerged in water without any presence of buried sediments, the measurement recorded by transducer is the value of wave pressure. However, when the sensor is covered by overburden layer, the measurement recorded by transducer is the value of pore-water pressure instead, which decays along soil depth because of the friction effect between pore water and soil particles within pore seabed. Moreover, the reduction of excess pore-water pressure caused by backfill materials is substantial until the thickness of backfill equals to 1D, while the curve representing the excess pore pressure variation becomes gradual when backfill thickness continues to grow from 1D to 2D. Here, the overburden depth of 1D (0.1 m) is considered to be optimum (minimum) backfill thickness, which is roughly consistent with the experimental results found in Zhai et al. (2018).

Figure 12, demonstrated the effect of relative buried depth (e/D) on the dimensionless excess pore pressure (|ue|/p0) along the soil depth from the pipeline bottom downward to seabed bottom, is examined for the wave condition of H=0.12 m and T=1.6 sec. Similar to the results around pipeline circumference, the dimensionless excess pore-water pressure decrease as the relative backfill depth increases. However, the decrement at upper layer is larger than that at lower layer.

Figure 13, accompanied with Figure 6 (c), illustrates the systematic depth profiles of normalized excess pore pressure (|ue|) versus backfill for the same wave characteristics. The results are for the case in which, the trench depth remains at 0.2 m, whereas the backfill thickness varies from 0
(non-backfill), 0.05 m, 0.1 m, 0.15 m to 0.2 m (full-backfill). As presented in Figure 13, $|u_e|$ measured at p1 ($z/h=0.357$) is occasionally smaller than that recorded at p9 ($z/h=0.411$), which is inconsistent with the general acknowledgement of decays of excess pore pressure along with soil depth in the absence of a submarine pipeline. These phenomena only occur in the shallow backfill layer under the high-energy wave conditions (i.e., in Figure 12 (a) and (b)). As afore-discussed, wave-induced seafloor pressure is transferred into sediment in terms of pore pressures and its energy propagates downward from the seabed surface to the internal area below the pipeline via diverse approaches, transmitting along the outer surface of the pipeline prior to subsequently downward, and/or passing through the porous bed down primarily. In the case of shallow backfill thickness, where the friction effect is comparatively small, the wave energy delivered by sediment particles and that by external periphery of the pipeline has almost the same magnitude, especially for wave loading with larger wave height or longer wave period. Herein, the larger oscillatory amplitude of the excess pore pressure may be recorded at p9 than that at p1. Nevertheless, when overburden depth is raised to a certain depth, e.g., $e=0.15$ m, 0.2 m, in which the friction effect of porous media cannot be negligible, the transient excess pore pressure transferred through soil grains sharply attenuates and that through the outside circumference of the pipeline definitely dominates the stress field. Thereby, $|u_e|$ measured at p9 is considerably smaller than that at p1, being consistent with the universal rule without the presence of the pipeline.

4.3 Effect of trench depth

Generally speaking, the trench depth has remarkable impacts on the wave-induced soil response in the trench layer around a partially buried pipeline. This is because, that a trench layer definitely perturbs the local flow and soil movement, thus further influence the excess pore pressure in the neighborhood. Duan et al. (2018) has numerically investigated that the flow velocity inside the trench is much lower than that outside the trench. In Figure 14, the excess pore-water pressure along the upper-half surface (e.g., $0^\circ < \theta < 180^\circ$) of the pipeline is not considered since the pipeline in some cases (i.e., $d=0.05$ m and $e\leq0.05$ m when $d=0.10$ m) is partially buried in the trench.
layer. Therefore, only the excess pore-water pressure along the lower-half surface (e.g., $180^\circ < \theta < 360^\circ$) of the pipeline is discussed, for $H=0.12$ m and $T=1.6$ sec. As shown in Figure 14, the lowest excess pore-water pressure ($|u_e|/\sigma_0'$) occurs at the bottom of the pipeline (measured by p1), while the highest value is located near the trench surface (recorded by p3 and p7). This implies that the upper region around the pipeline is more likely to be liquefied.

Figure 14 further illustrates that excess pore-water pressure generated by wave pressure becomes smaller for larger trench depth. This phenomenon could be ascribed to the fact that the deeper trench means the deeper location of the pipeline below the water surface, where wave-induced excess pore-water pressure will be attenuated more significantly. Therefore, the trench layer with larger depth has greater ability to suppress transient excess pore-water pressure response. As a result, the sheltering effect of the trench becomes stronger. Another observation is that the critical (the minimum) backfill thickness against transient seabed liquefaction for 1.0D-depth trench can be considered as 0.5D, as shown in Figure 14(a). However, even if the 0.5D-depth trench is fully backfilled, the value of excess pore-water pressure ($|u_e|/\sigma_0'$) is greater than 1. This indicates that the 0.5D-depth trench cannot prevent the pipeline from instability and the bottom of the pipeline could be damaged by the wave-induced transient seabed liquefaction.

5. Conclusions

In this paper, a comprehensive experimental investigation on soil responses in the trench layer around a partially backfilled pipeline to cyclic wave loading was reported. Twenty incident wave conditions (in which $H$ ranges from 0.06 m to 0.14 m and $T$ varies from 1.2 sec to 1.8 sec) are tested in the experiment. Three trench depths ($d/D=1.0, 1.5, 2.0$) and corresponding backfill thicknesses, which varies from non-backfill (where $e/D=0$) to full-backfill (where $e/D=1.0, 1.5, 2.0$ for $d/D=1.0, 1.5, 2.0$, respectively), are considered. Note that this is the first set of comprehensive experimental study for the soil response in the vicinity of a partially buried pipeline in a trench layer. Based on the experimental data, the following conclusions can be drawn.
(1) Based on the comparison between the experimental data and the numerical simulation (Liang and Jeng, 2018a,b), both overall agrees in the pore-water pressures along the pipeline periphery and beneath the pipeline for both fully buried \((e/D=0)\) and partially buried pipelines \((e/D=0.5)\). The pore pressure closely below the underwater pipeline under large progressive wave loading shows considerable deviation from that predicted by the theoretical model, especially at the lower backfill thickness. This is believed to be caused by the complex seepage flow in the trench layer.

(2) Transient excess pore-water pressure appears as a periodic response to the wave action, significantly determined by the wave characteristics. The oscillation of excess pore pressure presents a left-right circumferential asymmetric distribution, where the seaward edge of the pipeline is more vulnerable to instability caused by potential liquefaction than the shoreward edge. The crest pressure value occurs at the top of the pipeline and the trough pressure takes place at the bottom. The excess pore pressure oscillation in the trench layer attenuates along seabed depth and increase considerably with the increasing wave height and wave period.

(3) Excess pore-water pressure oscillatory amplitude decreases as the thickness of the backfill increases within the range of relative backfill depth chosen in this study. This can be ascribed to the increasing overburden effective stress. For practical engineers involved in the design of offshore pipeline projects, it is vital to determine a critical thickness of the backfill materials to suppress the wave-induced transient seabed liquefaction and meanwhile to reduce the financial budgets. In this study, the backfill thickness of \(e=0.5D\) can fully satisfy the requirement of pipeline stability, especially in the deep trench (i.e., \(d=2.0D\) and \(d=1.5D\)).

(4) Excess pore-water pressure oscillatory amplitude declines as the trench becomes deeper because of the better sheltering effect of trench. However, in the shallower trench, the ability to mitigate excess pore-water pressure becomes weaker as the flow velocity is stronger. Under the wave and soil characteristics tested in this study, the trench layer whose depth is greater than \(0.5D\) could provide a resistance to transient liquefaction occurring at the bottom.
of the pipeline.

Acknowledgements

This research was jointly supported by the National Key research and development program of China (2017YFC1404200), the research grants of Jiangsu (BK20150804), the marine renewable energy research project of State Oceanic Administration (GHME2015GC01), Open Foundation of State Key Laboratory of Hydrology-Water Resources and Hydraulic Engineering, Hohai University (Project No: 2016491011), the Royal Academy of Engineering the Distinguished Visiting Fellowship (DVF1718-8-7) and the Fundamental Research Funds for the Central Universities, Hohai University (2016B42514). Comments made by Reviewers have greatly improved the quality of the paper.

Reference:


562 pipeline on-bottom stability on liquefied noncohesive seabeds, Journal of Waterway, Port,
563 Coastal, and Ocean Engineering, ASCE, 132(4), 300-309.
564 de Groot, M. and Meijers, P. (1992), Liquefaction of trench fill around a pipeline in the seabed,
566 Du, X. J. and Zhao, J. (2015), Deep trenching protection of subsea pipeline crossing channel, Port
567 Engineering Technology, 52(6), 80-83.
568 Duan, L. L., Liao, C. C., Jeng, D.-S. and Chen, L. Y. (2017a), 2D numerical study of wave and current-
569 induced oscillatory non-cohesive soil liquefaction around a partially buried pipeline in a
570 trench, Ocean Engineering, 135, 39-51.
572 integrated model for wave and current-induced oscillatory soil liquefaction around an
574 Dunlap, W., Bryant, W., Williams, G. and Suhayda, J. (1979), Storm wave effects on deltaic
575 sediments – Results of SEASWAB I and II, Port and Ocean Engineering Under Arctic Conditions
576 (POAC79), Norwegian Institute of Technology, 2, 899-920.
577 Dunn, S. L., Vun, P. L., Chan, A. H. C. and Damgaard, J. S. (2006), Numerical modelling of wave-
578 induced liquefaction around pipelines. Journal of Waterway, Port, Coastal, and Ocean
580 Fredsøe, J. (2016), Pipeline–seabed interaction, Journal of Waterway, Port, Coastal and Ocean
581 Engineering, ASCE, 142(6), 03116002.
584 Gao, F. P., Jeng, D.-S. and Sekiguchi, H. (2003a), Numerical study on the interaction between non-
585 linear wave, buried pipeline and non-homogenous porous seabed, Computers and
586 Geotechnics, 30(6), 535-547.
588 instability, Ocean Engineering, 30(10), 1283-1304.
589 Gao, F. P. and Wu, Y. X. (2006), Non-linear wave-induced transient response of soil around a
590 trenched pipeline, Ocean Engineering, 33(3-4), 311-330.


Liang ZD and Jeng D.-S. (2018b): A three-dimensional model for the seabed response induced by waves in conjunction with currents in the vicinity of an offshore pipeline using OpenFOAM. *International Journal of Ocean and Coastal Engineering*, accepted


Sassa, S. and Sekiguchi, H. (2001), Analysis of wave-induced liquefaction of sand beds,


Zen, K. and Yamazaki, H. (1990a), Mechanism of wave-induced liquefaction and densification in


Fig 6
Figure captions:
Figure 1 Sketch of the wave flume and experimental setup.

Figure 2 Comparison of the simulated and measured water surface elevation recorded by wave height gauge \( h_4 \), for (a) Test 10 and (b) Test 49.

Figure 3 Comparison of the simulated and measured circumferential distribution of the oscillatory excess pore-water pressure amplitude \( |u_e|/p_0 \) along the periphery of the pipeline against numerical solution (Liang and Jeng, 2018): (a) Test 10 and (b) Test 49.

Figure 4 Comparison of the simulated and measured vertical distribution of the oscillatory excess pore-water pressure amplitude \( |u_e|/p_0 \) through the center of the pipeline against numerical solution (Liang and Jeng, 2018): (a) Test 10 and (b) Test 49.

Figure 5 Effect of (a) wave height and (b) wave period on the distribution of the ratio between the oscillatory excess pore-water pressure amplitude and the initial effective stress \( |u_e|/\sigma_0' \) along the vertical line below pipeline bottom versus relative depth \( z/h \) under different incident waves.

Figure 6 Distribution of oscillatory amplitude of wave-induced excess pore-water pressure \( |u_e| \) near the wave troughs along the central axis at four positions below the pipeline, \( z=0.20 \) m (p1), 0.23 m (p9), 0.27 m (p10) and, 0.40 m (p11), for various wave heights. (a) \( T=1.2 \) sec, (b) \( T=1.4 \) sec, (c) \( T=1.6 \) sec, and (d) \( T=1.8 \) sec.

Figure 7 Distribution of non-dimensional amplitude of wave-induced excess pore pressure \( |u_e|/p_0 \), around the pipeline outer-surface recorded by p1 to p8, for various wave heights. (a) \( T=1.2 \) sec, (b) \( T=1.4 \) sec, (c) \( T=1.6 \) sec, and (d) \( T=1.8 \) sec.

Figure 8 Distribution of oscillatory amplitude of wave-induced excess pore-water pressure \( |u_e| \) near the wave troughs along the central axis at four position below the pipeline, \( z=0.20 \) m (p1), 0.23 m (p9), 0.27 m (p10) and, 0.40 m (p11), for various wave periods. (a) \( H=0.08 \) m, (b) \( H=0.10 \) m, (c) \( H=0.12 \) m, and (d) \( H=0.14 \) m.
Figure 9 Distribution of non-dimensional amplitude of wave-induced excess pore pressure ($|u_e|/p_0$), around the pipeline outer-circumference recorded by p1 to p8, for various wave periods.

Figure 10 Scatter plot of normalized amplitude of excess pore pressure ($|u_e|/\sigma'_0$) around pipeline circumference, under wave height $H=0.12$ m and wave period $T=1.6$ sec, for various backfill thickness: (a) backfill depth ($d$) ranging from 0.00D to 2.00D with an interval of 0.25D, trench depth $e=2.0D$; (b) backfill depth ($d$) ranging from 0.00D to 1.50D with an interval of 0.25D, trench depth $e=1.5D$.

Figure 11 Variation of dimensionless amplitude of excess pore-water pressure ($|u_e|/p_0$) along the pipeline periphery at p1 ($\theta=\pi/2$), p3 ($\theta=0$), p5 ($\theta=\pi/2$) and p7 ($\theta=\pi$) for $H=0.12$ m and $T=1.2$ sec, under different seabed patterns: (a) $d=2.0D$, $e/D$ ranging from 0 to 2.00; (b) $d=1.5D$, $e/D$ ranging from 0 to 1.50.

Figure 12 Variation of dimensionless amplitude of excess pore-water pressure ($|u_e|/p_0$) along the central vertical line downward recorded at p1 ($z/h=0.357$), p9 ($z/h=0.411$), p10 ($z/h=0.482$), and p11 ($z/h=0.714$) for wave height $H=0.12$m and wave period $T=1.2$ s. These results are for the case in which trench depth $d=2.0D$ with various backfill depth, and the interval of backfill depth is 0.5D.

Figure 13 Distribution of normalized excess pore-water pressure versus backfill thickness

Figure 14 Scatter plot of normalized amplitude of excess pore pressure ($|u_e|/\sigma'_0$) around pipeline circumference, under wave height $H=0.12$ m and wave period $T=1.6$ sec, for various trench depth: (a) trench depth $e=1.0D$; (b) trench depth $e=0.5D$.

Table 1 Soil properties

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean grain size</td>
<td>$d_{50}$ (mm)</td>
<td>0.173</td>
</tr>
<tr>
<td>Unit weight of soil</td>
<td>$\gamma_s$ (kN/m$^3$)</td>
<td>26.5</td>
</tr>
</tbody>
</table>
Submerged unit weight of soil $\gamma'(\text{kN/m}^3)$ 19.7
Specific gravity of sediment grain $G_s = \gamma_s / \gamma_w$ 2.70
Permeability $k (\text{m/s})$ $3.56 \times 10^{-5}$

<table>
<thead>
<tr>
<th>Property</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Poisson's ratio $\mu$</td>
<td>0.32</td>
</tr>
<tr>
<td>Maximum void ratio $e_{\text{max}}$</td>
<td>0.886</td>
</tr>
<tr>
<td>Minimum void ratio $e_{\text{min}}$</td>
<td>0.420</td>
</tr>
<tr>
<td>Void ratio $e_s$</td>
<td>0.564</td>
</tr>
<tr>
<td>Porosity $n$</td>
<td>0.396</td>
</tr>
</tbody>
</table>

Relative density $D_r = \frac{e_{\text{max}} - e_s}{e_{\text{max}} - e_{\text{min}}}$ 0.624

### Table 2 Experiment conditions

<table>
<thead>
<tr>
<th>Case No.</th>
<th>Wave condition</th>
<th>Seabed condition</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Wave height $H$ (m)</td>
<td>Wave period $T$ (sec)</td>
</tr>
<tr>
<td>1</td>
<td>0.06</td>
<td>1.2</td>
</tr>
<tr>
<td>2</td>
<td>0.08</td>
<td>1.2</td>
</tr>
<tr>
<td>3</td>
<td>0.10</td>
<td>1.2</td>
</tr>
<tr>
<td>4</td>
<td>0.12</td>
<td>1.2</td>
</tr>
<tr>
<td>5</td>
<td>0.14</td>
<td>1.2</td>
</tr>
<tr>
<td>6</td>
<td>0.06</td>
<td>1.4</td>
</tr>
<tr>
<td>7</td>
<td>0.08</td>
<td>1.4</td>
</tr>
<tr>
<td>8</td>
<td>0.10</td>
<td>1.4</td>
</tr>
<tr>
<td>9</td>
<td>0.12</td>
<td>1.4</td>
</tr>
<tr>
<td>10</td>
<td>0.14</td>
<td>1.4</td>
</tr>
<tr>
<td>11</td>
<td>0.06</td>
<td>1.6</td>
</tr>
<tr>
<td>12</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>13</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>14</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>---</td>
<td>---</td>
<td>---</td>
</tr>
<tr>
<td>15</td>
<td>0.14</td>
<td>1.6</td>
</tr>
<tr>
<td>16</td>
<td>0.06</td>
<td>1.8</td>
</tr>
<tr>
<td>17</td>
<td>0.08</td>
<td>1.8</td>
</tr>
<tr>
<td>18</td>
<td>0.10</td>
<td>1.8</td>
</tr>
<tr>
<td>19</td>
<td>0.12</td>
<td>1.8</td>
</tr>
<tr>
<td>20</td>
<td>0.14</td>
<td>1.8</td>
</tr>
<tr>
<td>21</td>
<td>0.06</td>
<td>1.2</td>
</tr>
<tr>
<td>22</td>
<td>0.08</td>
<td>1.2</td>
</tr>
<tr>
<td>23</td>
<td>0.10</td>
<td>1.2</td>
</tr>
<tr>
<td>24</td>
<td>0.12</td>
<td>1.2</td>
</tr>
<tr>
<td>25</td>
<td>0.14</td>
<td>1.2</td>
</tr>
<tr>
<td>26</td>
<td>0.06</td>
<td>1.4</td>
</tr>
<tr>
<td>27</td>
<td>0.08</td>
<td>1.4</td>
</tr>
<tr>
<td>28</td>
<td>0.10</td>
<td>1.4</td>
</tr>
<tr>
<td>29</td>
<td>0.12</td>
<td>1.4</td>
</tr>
<tr>
<td>30</td>
<td>0.14</td>
<td>1.4</td>
</tr>
<tr>
<td>31</td>
<td>0.06</td>
<td>1.6</td>
</tr>
<tr>
<td>32</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>33</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>34</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>35</td>
<td>0.14</td>
<td>1.6</td>
</tr>
<tr>
<td>36</td>
<td>0.06</td>
<td>1.8</td>
</tr>
<tr>
<td>37</td>
<td>0.08</td>
<td>1.8</td>
</tr>
<tr>
<td>38</td>
<td>0.10</td>
<td>1.8</td>
</tr>
<tr>
<td>39</td>
<td>0.12</td>
<td>1.8</td>
</tr>
<tr>
<td>40</td>
<td>0.14</td>
<td>1.8</td>
</tr>
<tr>
<td>41</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>42</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td></td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>---</td>
<td>------</td>
<td>-----</td>
</tr>
<tr>
<td>44</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>45</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>46</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>47</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>48</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>49</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>50</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>51</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>52</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>53</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>54</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>55</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>56</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>57</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>58</td>
<td>0.14</td>
<td>1.6</td>
</tr>
<tr>
<td>59</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>60</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>61</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>62</td>
<td>0.14</td>
<td>1.6</td>
</tr>
<tr>
<td>63</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>64</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>65</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>66</td>
<td>0.14</td>
<td>1.6</td>
</tr>
<tr>
<td>67</td>
<td>0.08</td>
<td>1.6</td>
</tr>
<tr>
<td>68</td>
<td>0.10</td>
<td>1.6</td>
</tr>
<tr>
<td>69</td>
<td>0.12</td>
<td>1.6</td>
</tr>
<tr>
<td>70</td>
<td>0.14</td>
<td>1.6</td>
</tr>
</tbody>
</table>

- 39 -
<p>| | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>71</td>
<td>0.12</td>
<td>1.6</td>
<td>0.10</td>
<td>0.1</td>
<td></td>
</tr>
</tbody>
</table>

826
827