

# **Devise of a W Serpentine Shape Tube Heat Exchanger in a Hard Chromium Electroplating Process**

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1 Energy, Resources and Environmental Technology

## 2 **Devise of a W Serpentine Shape Tube Heat Exchanger** 3 **in a Hard Chromium Electroplating Process**

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### 9 **Abstract**

10 In a hard chromium electroplating process, a heat exchanger is employed to remove the heat  
11 produced from the high current intensity in an electroplating bath. Normally, a conventional U  
12 shape heat exchanger is installed in the bath but it provides low heat removal. Thus, this study  
13 designs a novel W serpentine shape heat exchanger with identical heat transfer area to the  
14 conventional one for increasing heat removal performance. The performance of the heat  
15 exchange is tested with various flow velocities in a cross-section in range of 1.6 to 2.4 m·s<sup>-1</sup>.  
16 Mathematical models of this process have been formulated in order to simulate and evaluate the  
17 heat exchanger performance. The results show that the developed models give a good prediction  
18 of the plating solution and cooling water temperature and the novel heat exchanger provides  
19 better results at any flow velocity. In addition, the W serpentine shape heat exchanger has been  
20 implemented in a real hard chromium electroplating plant. Actual data collected have shown that  
21 the new design gives higher heat removal performance compared with the U shape heat  
22 exchanger with identical heat transfer area; it removes more heat out of the process than the  
23 conventional one of about 23%.

24 **Keyword:** W serpentine shape; Hard chromium electroplating; Mathematical modeling;  
25 Simulation; Heat exchanger.

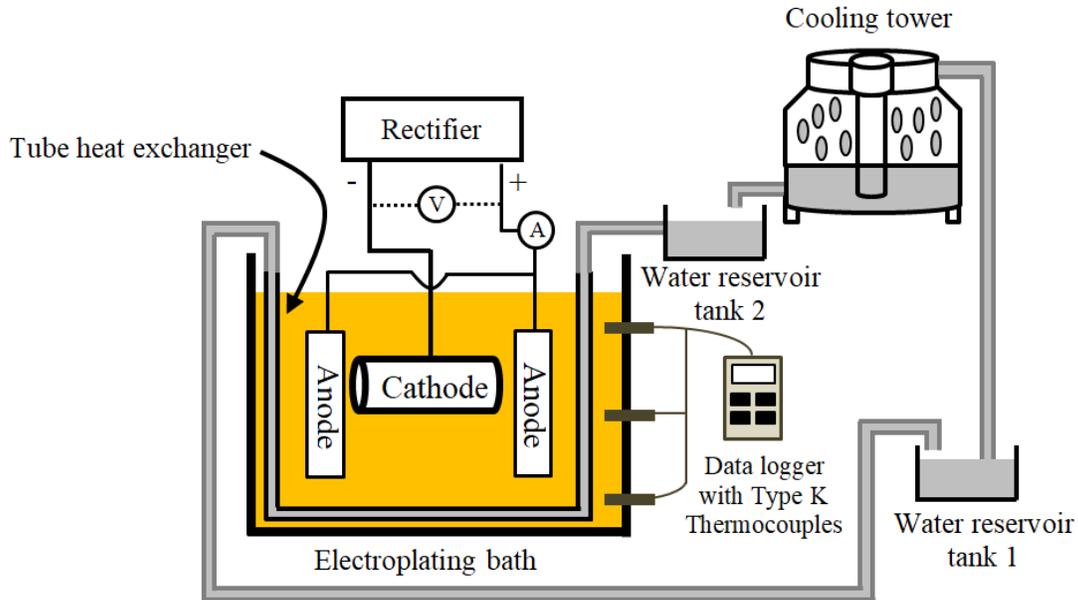
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## 28 **1. Introduction**

29 A hard chromium electroplating process is one kind of chromium electroplating. This  
30 process is usually applied for protecting the surface of base materials against a harmful  
31 environment, extending the maintenance time and increasing the material properties *i.e.*  
32 corrosive resistance, wear resistance and shear stress [1, 2]. In the hard chromium electroplating  
33 process, the workpieces such as pistons, rollers, gaskets, vehicle molds and electrical parts, etc.  
34 are coated with the chromium metal from 2.5 to 500  $\mu\text{m}$  in thickness [3]. Generally, the  
35 performance of this plating and the probability of defect occurrence on coated products are  
36 depended on the operating conditions during the plating period such as the concentration of  
37 plating solution, current density, power voltage and temperature [4, 5]. To provide the best  
38 quality of the coated products, the optimal range for the hard chromium electroplating is in range  
39 of  $(50 \pm 3) ^\circ\text{C}$  [5, 6]. All unit operations in the hard chromium electroplating process are shown  
40 in Fig. 1. This process comprises of an electroplating bath with an immersed tube heat exchanger  
41 that is also connected to a cooling tower. The cooling water is a media to deliver the heat from  
42 the bath and to cool the plating solution through the heat exchanger. When the cooling water  
43 temperature is high after flowing through the electroplating bath, the cooling tower takes away  
44 the heat and supplies the low temperature cooling water to the bath again.



**Fig. 1** Hard chromium electroplating process with the cooling system.

However, the main factor affected on the product quality is the temperature of the plating solution during the operation. Due to the fact that the plating solution temperature is continually raised by the heat produced from the high current load during the plating time, then the accumulated heat of plating solution can cause the defects on the surface of products. When this problem takes place, the defected products are recoating again [7]. Since this high temperature problem is normally found in the hard chromium electroplating plant, an effective heat exchanger is needed to keep the plating solution temperature in the optimal range around 47 to 53 °C along the plating period [8].

In general, a conventional U shape tube heat exchanger is installed at the wall of the electroplating bath. This pipe is made of the titanium to protect against the corrosion from the chromic acid. Normally, the U shape tube heat exchanger in the bath is placed in parallel with the direction of heat flow which directly affects to heat transfer coefficient [9]. Then, it leads to the thermal resistance film that reduces the heat transfer between two fluids, at the outer surface

61 of the tube [10]. In order to improve the heat transfer coefficient of the tube heat exchanger,  
62 piping patterns or shape of heat exchangers reported by recent literatures such as a spiral  
63 corrugated tube [11, 12], a curved tube [13, 14], an inserted triangle coil tube [15, 16] and a  
64 vibrating tube [17, 18] have been studied. To evaluate the performance of the heat exchanger,  
65 mathematical models of the process and heat exchangers are also developed.

66 The objective of this work is to devise a novel heat exchanger for the hard chromium  
67 electroplating process to improve the heat transfer coefficient. In addition, the mathematical  
68 models of the hard chromium electroplating process and the heat exchangers have been  
69 developed and validated with the actual data. The developed models have been used to study the  
70 temperature profile and the heat removal performance of the conventional U shape and the novel  
71 design heat exchangers. Finally, the novel design heat exchanger has been implemented in the  
72 bath and its performance has been evaluated.

## 73 **2. Methods**

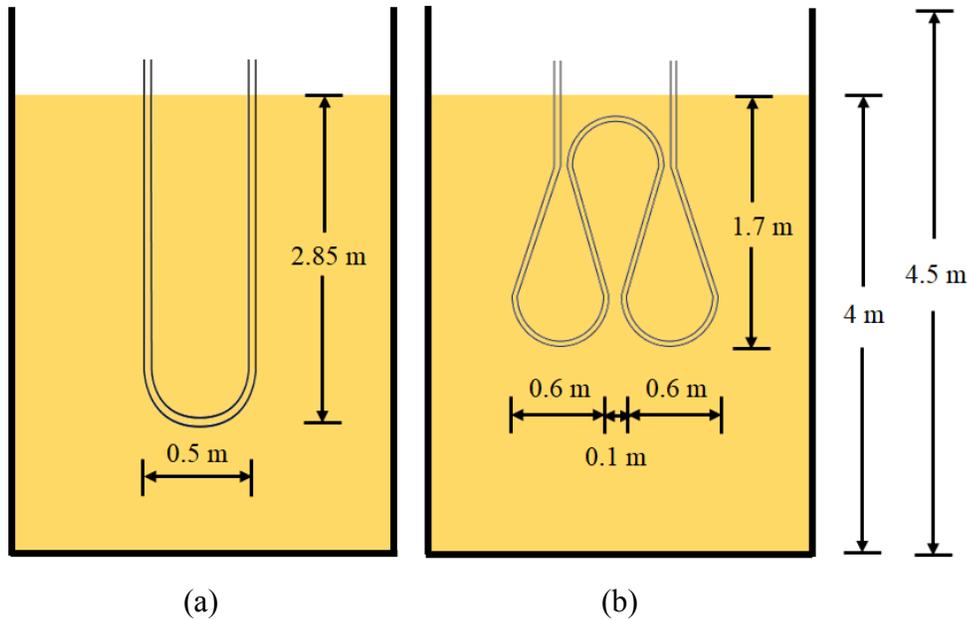
### 74 *2.1 Process overview*

75 A hard chromium electroplating process in this study consists of an electroplating bath  
76 (1.7 m diameter and 4.5 m height), a tube heat exchanger, two reservoir tanks of cooling water  
77 and a cooling tower as shown in Fig.1. In this process, the height of plating solution is 4 m from  
78 the bottom of the bath and the objects to be plated are connected with the rectifier and are  
79 submerged into the plating solution. The conventional U shape tube heat exchanger (2.54 cm  
80 diameter and 30 m in total length) with cooling water as the medium is installed inside the bath  
81 for removing any heat generated from the electrical current. Then, the high temperature cooling  
82 water from all electroplating baths collected at the first water reservoir tank are fed into the  
83 cooling tower in order to cool down its temperature to about 34 °C. After that, the cooling water

84 is recirculated to the electroplating bath again. Some amounts of cooling water are loss from the  
85 drag out, wind and evaporation at the reservoir tanks and the cooling tower. In order to collect  
86 the data from the real plant, a data logger connected with Type K Thermocouples is used for this  
87 purpose. Three thermocouples are placed at 1 m, 2 m and 3.5 m from the plating solution surface  
88 in order to observe the temperatures in the bath during 8 hours of the operation and the plating  
89 bath temperatures can be collected and used to validate the mathematical models of the bath.

## 90 *2.2 Devise of the W serpentine shape tube heat exchanger*

91 The novel heat exchanger of this work is devised with a pattern of W serpentine shape [Fig.  
92 2(b)]. This new design attempts to prevent the thermal resistance film formulation by introducing  
93 inclined and curve shapes that give the unparalleled flow direction of the cooling water and the  
94 plating solution. Thus, the W shape heat exchanger has less the thermal resistance film  
95 formulation at the outer tube surface resulting in more heat transfer rate than the original one. In  
96 addition, the curve design of the W shape induces the secondary flow of the cooling water inside  
97 the tube [19, 20] that enhances the heat transfer rate between the plating solution and the cooling  
98 water [21, 22]. Titanium is chosen as the piping material for this novel heat exchanger. In this  
99 study, the W serpentine shape heat exchangers with 1.27 and 2.54 cm diameter, which have the  
100 identical heat transfer area as to the U shape heat exchanger, are designed to compare the  
101 performance. Furthermore, the heat exchangers are tested with various flow velocities in a cross-  
102 section at 1.6, 2.0 and 2.4 m·s<sup>-1</sup> for evaluating its performance. In order to obtain the same flow  
103 velocity in each heat exchanger, the volumetric water flow rates at  $1.55 \times 10^{-4}$ ,  $1.94 \times 10^{-4}$  and  
104  $2.32 \times 10^{-4}$  m<sup>3</sup>·s<sup>-1</sup> are used for the 1.27 cm diameter heat exchanger and the volumetric water flow  
105 rates at  $7.12 \times 10^{-4}$ ,  $8.9 \times 10^{-4}$  and  $10.68 \times 10^{-4}$  m<sup>3</sup>·s<sup>-1</sup> are used for the 2.54 cm diameter heat  
106 exchanger.



**Fig. 2** Illustration of the heat exchangers inside the hard chromium electroplating bath:  
 (a) U shape heat exchanger and (b) W serpentine shape heat exchanger.

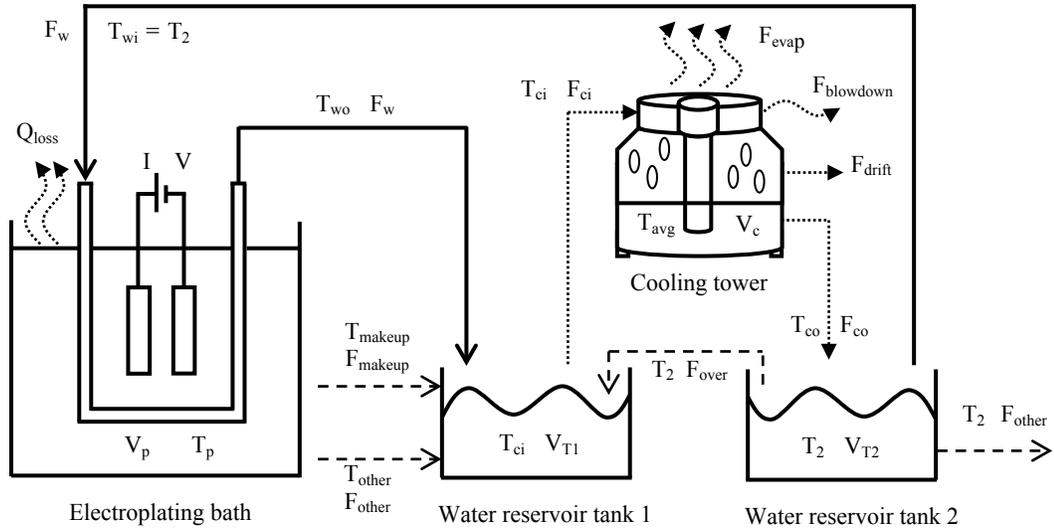
### 2.3 Assumptions

To derive the equations for the hard chromium electroplating process, the following assumptions are made as follows,

- The variation of the plating solution concentration is negligible.
- The physical and chemical properties of the plating solution such as density or heat capacity are constant along the plating period.
- The electroplating bath is well-mixed.
- The heat generated from electroplating current load is remarkably significant compared to heat released from chemical reactions.
- Heat loss of the cooling water in the heat exchanger outside the bath to the surrounding is negligible.

### 2.4 Mathematical modeling of the hard chromium electroplating process

123 Mathematical models of the electroplating bath and cooling water system in this study  
 124 (Fig. 3) are based on the principle of mass and energy conservation [23, 24].



125  
 126 **Fig. 3** Schematic diagram of the hard chromium electroplating process with mass and  
 127 energy balance.

#### 128 2.4.1 The electroplating bath

129 Mass conservation equation

$$130 \frac{d(\rho_p V_p)}{dt} \quad (1)$$

131 Energy conservation equation

$$132 \frac{dT_p}{dt} = \frac{IV - Q_{\text{loss}} - F_t U_0 A_{\text{ht}} \Delta T_{\text{lm}}}{\rho_p C_{pp} V_p} \quad (2)$$

133 The equation of energy conservation in Eq. (2) contains the heat production owing to the  
 134 power current load, the heat loss at the upper surface of the plating solution to the surrounding  
 135 and the term related to heat transfer between the electroplating bath and the heat exchanger. The

136  $Q_{\text{loss}}$  term related on the power current load and plating solution temperature is calculated from  
 137 Eq. (3).

$$138 \quad Q_{\text{loss}} = f(IV) + (0.0196T_p^{2.8806} + 2.1527T_p - 32.655)A_{\text{sur}} \quad (3)$$

139 In Eq. (3), the function of  $f(IV)$  can be obtained by the least squares method with the  
 140 relation of the actual data between the plating solution temperature and the current load.

#### 141 *2.4.2 The tube heat exchanger*

142 The energy conservation equation of the tube heat exchanger that immersed in the  
 143 electroplating bath is applied using a lumped model [25], while a constant volumetric water flow  
 144 rate is considered on the mass balance.

145 Mass conservation equation

$$146 \quad \frac{d(\rho_w V_{\text{tube}})}{dt} = 0 \quad (4)$$

147 Energy conservation equation

$$148 \quad \frac{dT_{\text{wo}}}{dt} = \frac{F_w (T_{\text{wi}} - T_{\text{wo}})}{L_{\text{tube}} A_o} + \frac{F_t U_o A_{\text{ht}} \Delta T_{\text{lm}}}{\rho_w C_{\text{pw}} L_{\text{tube}} A_o} \quad (5)$$

149 Where  $U_o$  refers to the overall heat transfer coefficient,  $\Delta T_{\text{lm}}$  expresses to the logarithmic  
 150 mean temperature and can be computed by Eq. (6). The right term of energy balance in Eq. (5) is  
 151 constituted of the different of heat flow between outlet and inlet tube heat exchanger and the heat  
 152 exchanged with the electroplating bath and heat exchanger.

$$153 \quad \Delta T_{\text{lm}} = \frac{T_{\text{wo}} - T_{\text{wi}}}{\ln \left[ \frac{T_p - T_{\text{wi}}}{T_p - T_{\text{wo}}} \right]} \quad (6)$$

154 *2.4.3 The cooling system*

155 The cooling system composes two water reservoir tanks and a cooling tower. The water  
 156 flowing from the tube heat exchanger to a tank 1 is delivered to the cooling tower in order to  
 157 reduce its temperature. The cooling water flows from the cooling tower to a tank 2 before  
 158 entering to the electroplating bath. Eq. (7) to Eq. (9) provide the mass conservation equations for  
 159 both tanks and the cooling tower, respectively.

160 Mass conservation equations

$$161 \quad F_{co} = F_{ci} - F_{makeup} \quad (7)$$

$$162 \quad F_{over} = F_{co} - F_w - F_{other} \quad (8)$$

$$163 \quad F_{makeup} = F_{blowdown} + F_{evap} + F_{drift} \quad (9)$$

164 The water makeup of the cooling tower in Eq. (9) consists of the summation of blowdown,  
 165 evaporation loss and drift loss [26]. Blowdown discards a portion of the concentrated circulating  
 166 water due to the evaporation process in order to lower the system solid concentration. Drift loss  
 167 is entrained water that carried out from the cooling tower by the wind.

168 Energy conservation equations

$$169 \quad \frac{dT_{ci}}{dt} = \frac{F_w T_{wo} + F_{makeup} T_{makeup} - F_{ci} T_{ci}}{V_{T1}} + \frac{F_{other} T_{other} + F_{over} T_2}{V_{T1}} \quad (10)$$

$$170 \quad \frac{dT_2}{dt} = \frac{F_{co} T_{co} - F_w T_2 - F_{over} T_2 - F_{other} T_2}{V_{T2}} \quad (11)$$

$$171 \quad \frac{dT_{co}}{dt} = \frac{F_{ci} T_{ci} - F_{co} T_{co} - F_{makeup} T_{avg} - \frac{h_A A_s (T_{avg} - T_{air})}{\rho_w c_{pw}} - \frac{F_{evap} \lambda_{evap}}{c_{pw}}}{V_c} \quad (12)$$

172 The three terms in the energy conservation equation of the cooling tower as shown in Eq.  
 173 (12) demonstrate the difference of heat flow between outlet and inlet of the cooling tower with

174 the last two terms showing the heat transferred by convection and evaporation, respectively.  
175 Term of  $h_A A_s$  can be obtained by the least squares method with the water temperature profile at  
176 the cooling tower. The  $T_{\text{avg}}$  in the above equation is calculated by

$$177 \quad T_{\text{avg}} = \frac{T_{\text{ci}} + T_{\text{co}}}{2} \quad (13)$$

178 The overall heat transfer coefficient of tube heat exchanger involves two convective and one  
179 conductive resistance, while the fouling is negligible. In case of both U shape and W shape tube  
180 heat exchangers, the overall heat transfer coefficients are calculated by optimization based on  
181 actual data. The optimization problem can be formulated as follows:

182 Objective function: 
$$\min_{U_o} \sum_{i=0}^{t_f} \{T_{p,actual}(i) - T_{p,simulation}(i)\}^2 \quad (14)$$

183 Subject to process models from Eq. (1) to Eq. (13).

184 The physical properties, geometric characteristics and operating conditions used in this work  
 185 are summarized in Table 1 to Table 3. In the model validation, the simulation results are  
 186 validated with the actual data collected from a real plant and demonstrated in Fig. 4.

187 **Table 1**

188 Physical properties [27, 28].

Physical property	Value
Density of water/kg·m <sup>-3</sup>	992.25
Density of plating solution/kg·m <sup>-3</sup>	1,174.4
Heat capacity of water/kJ·kg <sup>-1</sup> ·°C <sup>-1</sup>	4.181
Heat capacity of plating solution/kJ·kg <sup>-1</sup> ·°C <sup>-1</sup>	4.917
Latent heat of vaporization of water/kJ·kg <sup>-1</sup>	2,260
Thermal conductivity of titanium/kW·m <sup>-1</sup> ·°C <sup>-1</sup>	0.0206

189

190 **Table 2**

191 Simulation system geometric characteristics.

System characteristic	Value
Inner diameter of a 1.27 cm diameter tube heat exchanger/m	0.0111
Outer diameter of a 1.27 cm diameter tube heat exchanger/m	0.0127
Inner diameter of a 2.54 cm diameter tube heat exchanger/m	0.0238
Outer diameter of a 2.54 cm diameter tube heat exchanger/m	0.0254
Volume of an electroplating bath/m <sup>3</sup>	9.3062
Volume of a water tank 1/m <sup>3</sup>	2.1155
Volume of a water tank 2/m <sup>3</sup>	2.5663
Volume of a cooling tower/m <sup>3</sup>	0.3771

192

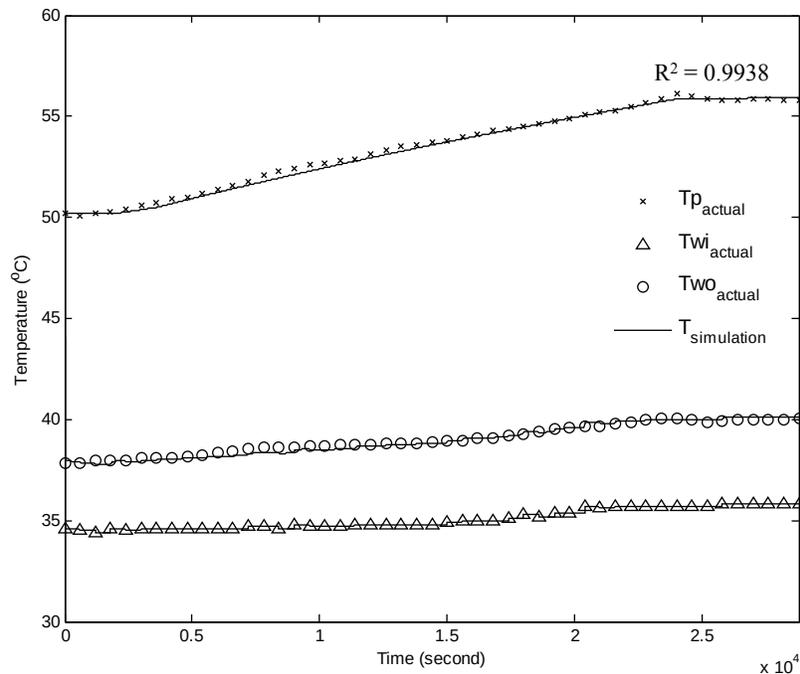
**Table 3**

193 Operating conditions for simulation.

Operating condition	Value
Outlet water temperature to other electroplating baths/°C	44.1

Water make up temperature/°C	34.9
Air temperature/°C	30
Volumetric flow rate of cooling water in other electroplating baths flow to a cooling tower/m <sup>3</sup> ·s <sup>-1</sup>	$4.3364 \times 10^{-4}$
Water make up to a cooling tower/m <sup>3</sup> ·s <sup>-1</sup>	$7.7597 \times 10^{-6}$
Water evaporation rate in a cooling tower/m <sup>3</sup> ·s <sup>-1</sup>	$4.3238 \times 10^{-6}$
Water blow down rate of a cooling tower/m <sup>3</sup> ·s <sup>-1</sup>	$1.0809 \times 10^{-6}$
Water drift loss of a cooling water/m <sup>3</sup> ·s <sup>-1</sup>	$2.3550 \times 10^{-6}$

194



195

196

**Fig. 4** Comparison results between simulation and actual data of plating solution

197

temperature and water temperature at inlet and outlet of the electroplating bath.

198

199

Since the workpieces require a high thickness of hard chromium coating, the current load of electroplating is supplied at a high rate. The high current load can lead to the increase in the

200

plating solution temperature if the heat removed out of the solution by the heat exchanger is

201

lower than that of the heat generated from the current load. Fig. 4 shows a good agreement

202

between simulation results and the actual data with the coefficient of determination ( $R^2$ ) of more

203

than 90% so the mathematical models of this process can be used to predict the temperature

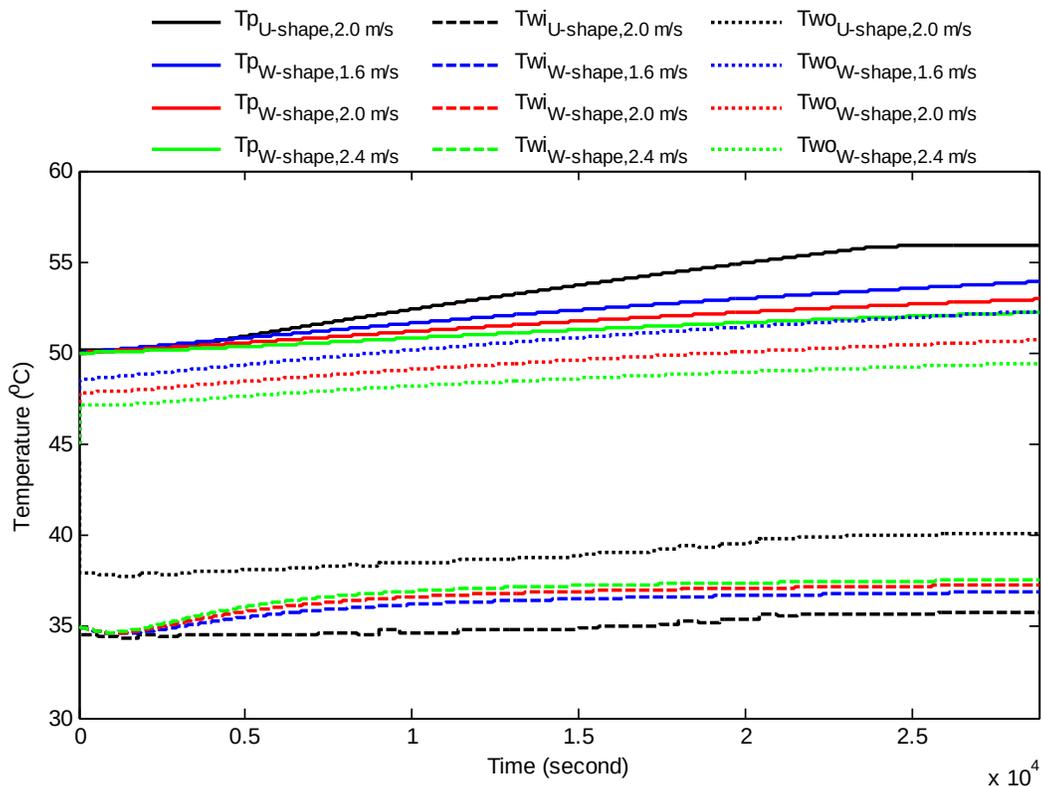
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profile of the process.

### 205 3. Results & Discussion

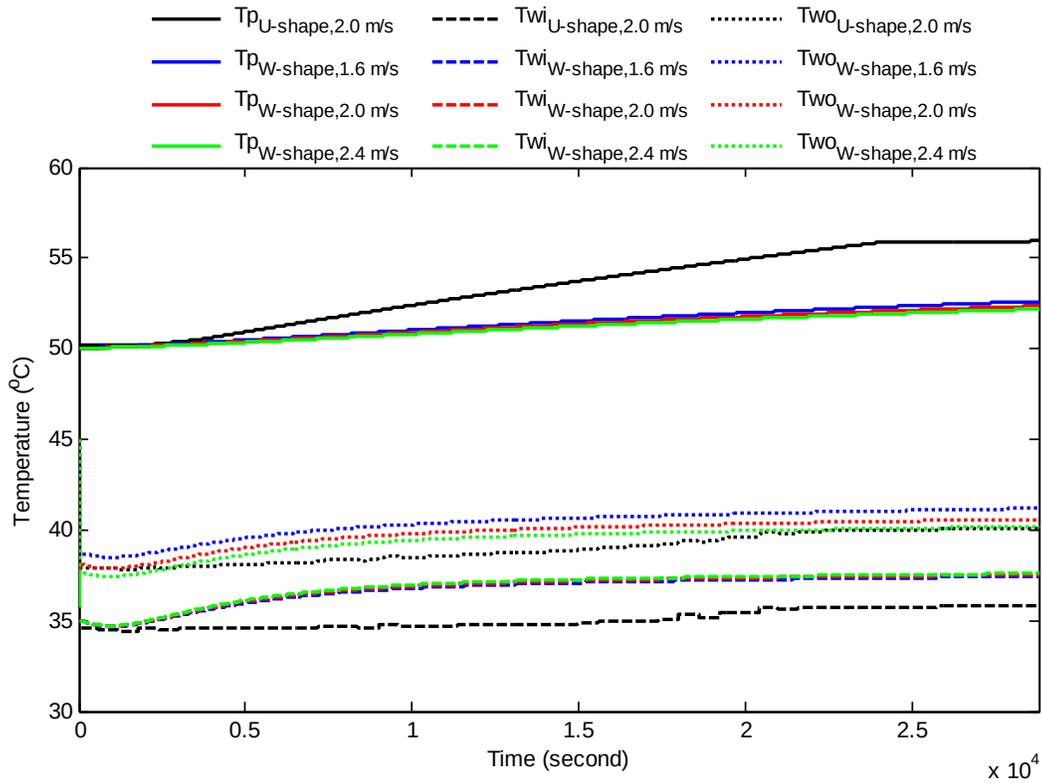
#### 206 3.1 Simulation results

207 Fig. 5 and Fig .6 demonstrate the temperature profile of the plating solution, water inlet and  
 208 outlet at the electroplating bath for the W serpentine shape with diameters of 1.27 and 2.54 cm  
 209 comparing to the conventional U shape tube heat exchanger. To test the heat exchangers, the  
 210 cooling water flow velocities of 1.6, 2.0 and 2.4 m·s<sup>-1</sup> are introduced in this study. These results  
 211 show that the plating solution temperature profiles of both sizes of the W serpentine shape are  
 212 lower than that of the U shape heat exchanger. Since, the new design has the combination of the  
 213 inclined and curved shapes which makes an unparallelled flow direction between the cooling  
 214 water and the plating solution inside the bath. This prevents the formulation of thermal resistance  
 215 film at the outer tube surface that resulting in enhances the heat transfer rate [10].



217 **Fig. 5** The temperature profile of plating solution, water inlet and outlet at the  
 218 electroplating bath for 1.27 cm diameter of W serpentine shape tube heat exchanger  
 219 at various water velocities.

220



221

222 **Fig. 6.** The temperature profile of plating solution, water inlet and outlet at the  
 223 electroplating bath for 2.54 cm diameter of W serpentine shape tube heat exchanger  
 224 at various water velocities.

225 Furthermore, the curve shape of this devised heat exchanger increases the heat transfer rate  
226 between the plating solution and the cooling water from the secondary flow of the cooling water  
227 inside the tube [20, 21, 22]. In Fig. 5, when current load is applied to the electroplating bath  
228 during the 8 hours of operation, the 1.27 cm diameter of the W shape heat exchanger with 2.4  
229  $\text{m}\cdot\text{s}^{-1}$  of flow velocity can adequately remove the heat that generated from the bath and the  
230 temperature of the plating solution can be maintained in the optimal range of  $(50\pm 3)^\circ\text{C}$ .  
231 However, in the case of  $1.6 \text{ m}\cdot\text{s}^{-1}$  of flow velocity, the temperature difference between plating  
232 solution and water at the outlet is small. As a consequence, the heat removal is insufficient to  
233 maintain the plating solution temperature at the optimal range; the temperature of the bath is  
234 more than  $53^\circ\text{C}$ . Nevertheless, the result of the W serpentine shape with 2.54 cm diameter in  
235 Fig. 6 shows that the cooling water at all velocities can remove the generated heat from the  
236 process and the plating solution temperature can be kept at the optimal range along the  
237 electroplating period; the maximum temperature of the plating solution is 52.6, 52.3 and  $52.2^\circ\text{C}$   
238 at 1.6, 2.0 and  $2.4 \text{ m}\cdot\text{s}^{-1}$  of flow velocities, respectively. With these results, thus the W serpentine  
239 shape with 2.54 cm diameter is selected for implementation at the real plant.

### 240 *3.2 Implementation results of the W serpentine shape tube heat exchanger*

241 According to the simulation study, the W serpentine shape tube heat exchanger requires the  
242 2.54 cm diameter and 30 m in total length. However, in practical and due to the limitations of the  
243 free space for installation inside the real electroplating bath, this heat exchanger is divided into  
244 four pieces. Each piece has a diameter of 2.54 cm and a length of 7.5 m (Fig. 7), which is  
245 conveniently implemented in the real bath. Each heat exchanger is immersed in half of plating  
246 solution depth because a large amount of heat from the hard chromium electroplating process

247 releases at this position. The end of both sides is connected with a polyvinylchloride (PVC) tube  
248 to supply and recirculate the cooling water.



249  
250

(a) The W serpentine shape tube heat exchanger.



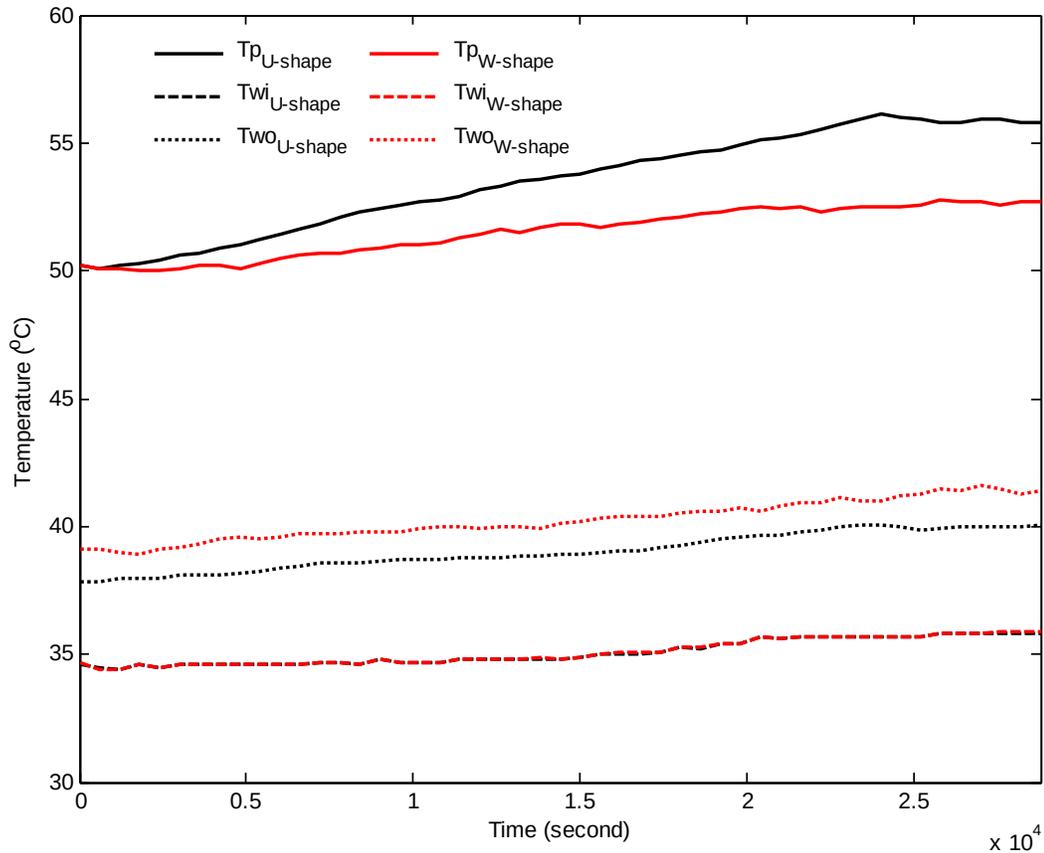
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(b) The installation of the W serpentine shape tube heat exchanger in the electroplating bath.

253 **Fig. 7** The implementation of W serpentine shape tube heat exchanger.

254 Fig.8 demonstrates the actual data after the implementation of the W serpentine shape tube  
255 heat exchanger and the U shape tube heat exchanger. The result indicates that the W serpentine  
256 shape tube heat exchanger can keep the plating solution temperature during the plating period  
257 lower than the original one. The plating solution temperature can be kept in the range of 50 -  
258 53°C during the plating period and the water outlet temperature is about 39 - 42°C. With the

259 collected data, the novel W serpentine shape tube heat exchanger removes more heat out of the  
 260 process than the conventional heat exchanger around 23%.



261  
 262 **Fig. 8** Comparison of temperature profile of plating solution, water inlet and outlet at the  
 263 electroplating bath with the cooling water flow velocity at 2.0 m·s<sup>-1</sup>.

#### 264 4. Conclusions

265 To control the temperature of the hard chromium electroplating bath, an effective heat  
 266 exchanger is needed to remove heat occurred during the electroplating process. In this work, heat  
 267 removals of two tube heat exchangers have been compared. In addition, mathematical models of  
 268 the hard chromium electroplating process have been formulated to predict the dynamics  
 269 temperature of the electroplating bath and evaluate the heat exchanger performance. Unknown  
 270 parameters in the developed models are determined based on the actual plant data. The  
 271 simulation results show that the developed models can give a good accurate prediction of the

272 plating solution temperature with the coefficient of determination ( $R^2$ ) of more than 90%. The  
273 heat removal performances of 1.27 and 2.54 cm diameter of the W serpentine shape tube heat  
274 exchangers with the flow velocity in a cross-section at 1.6, 2.0 and 2.4 m·s<sup>-1</sup> are compared. The  
275 simulation results indicate that the W serpentine shape with 2.54 cm diameter is applicable to  
276 maintain the plating solution temperature at the desired range at any flow velocity. Furthermore,  
277 four W serpentine shape tube heat exchangers with identical heat transfer area to the U shape  
278 tube heat exchanger (2.54 cm diameter and 30 m in total length) are implemented in the real  
279 electroplating bath. The plating solution temperature after the implementation can be kept at the  
280 range. Moreover, the novel design provides higher heat removal than the conventional U shape  
281 tube heat exchanger around 23%.

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 286 for financial support to this study.

## 287 Nomenclature

288	$A_{ht}$	Heat transfer area of a tube heat exchanger, $m^2$
289	$A_o$	Cross section area of a tube heat exchanger, $m^2$
290	$A_{sur}$	Contacted area of the surface of plating solution with surroundings, $m^2$
291	$A_s$	Surface area between water droplet and air, $m^2$
292	$C_{pp}$	Specific heat capacity of plating solution, $kJ \cdot kg^{-1} \cdot ^\circ C^{-1}$
293	$C_{pw}$	Specific heat capacity of water, $kJ \cdot kg^{-1} \cdot ^\circ C^{-1}$
294	$F_{blowdown}$	Water blowdown rate of a cooling tower, $m^3 \cdot s^{-1}$
295	$F_{ci}$	Inlet volumetric water flow rate of a cooling tower, $m^3 \cdot s^{-1}$
296	$F_{co}$	Outlet volumetric water flow rate of a cooling tower, $m^3 \cdot s^{-1}$
297	$F_{drift}$	Water drift loss of a cooling water, $m^3 \cdot s^{-1}$
298	$F_{evap}$	Water evaporation rate in a cooling tower, $m^3 \cdot s^{-1}$
299	$F_{makeup}$	Water makeup to a cooling tower, $m^3 \cdot s^{-1}$
300	$F_{other}$	Volumetric flow rate of cooling water from other electroplating baths to a
301		cooling tower, $m^3 \cdot s^{-1}$
302	$F_{over}$	Volumetric flow rate of cooling water from a water reservoir tank 2 overflows
303		to a water reservoir tank 1, $m^3 \cdot s^{-1}$

304	$F_w$	Volumetric flow rate of cooling water, $\text{m}^3\cdot\text{s}^{-1}$
305	$F_t$	Heat exchanger correction factor
306	$h_A$	Heat transfer coefficient of convection between water and air, $\text{W}\cdot\text{m}^{-2}\cdot\text{C}^{-1}$
307	$I$	Electric current, A
308	$L_{\text{tube}}$	Length of a tube heat exchanger, m
309	$Q_{\text{loss}}$	Heat loss from an upper surface of the plating solution to surroundings, W
310	$T_{\text{air}}$	Air temperature, $^{\circ}\text{C}$
311	$T_{\text{avg}}$	Average different water temperature at a cooling tower, $^{\circ}\text{C}$
312	$T_{\text{ci}}$	Water temperature at a water reservoir tank 1, $^{\circ}\text{C}$
313	$T_{\text{co}}$	Outlet water temperature in a cooling tower, $^{\circ}\text{C}$
314	$t_f$	Total operation time, s
315	$T_{\text{makeup}}$	Water makeup temperature, $^{\circ}\text{C}$
316	$T_{\text{other}}$	Outlet water temperature from other electroplating baths, $^{\circ}\text{C}$
317	$T_p$	Plating solution temperature, $^{\circ}\text{C}$
318	$T_{p,\text{actual}}$	Plating solution temperature which collected from a real plant, $^{\circ}\text{C}$
319	$T_{p,\text{simulation}}$	Plating solution temperature from simulation, $^{\circ}\text{C}$
320	$T_{\text{simulation}}$	Temperature results from the simulation, $^{\circ}\text{C}$
321	$T_{\text{wi}}$	Inlet cooling water temperature, $^{\circ}\text{C}$
322	$T_{\text{wi,actual}}$	Inlet cooling water temperature which collected from a real plant, $^{\circ}\text{C}$
323	$T_{\text{wo}}$	Outlet cooling water temperature, $^{\circ}\text{C}$
324	$T_{\text{wo,actual}}$	Outlet cooling water temperature which collected from a real plant, $^{\circ}\text{C}$
325	$T_2$	Water temperature at a water reservoir tank 2, $^{\circ}\text{C}$

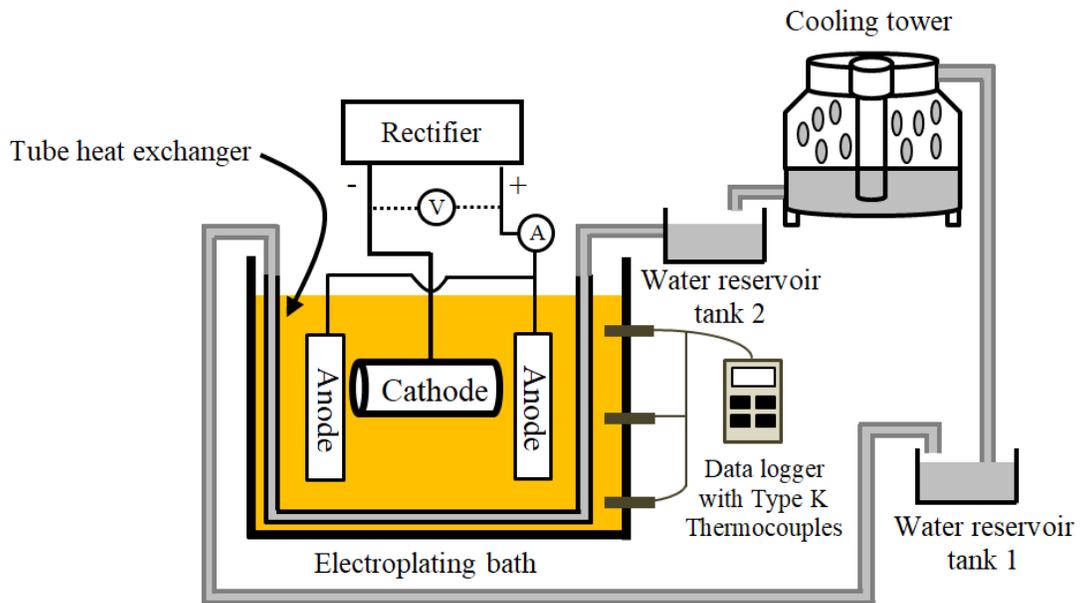
326	$\Delta T_{lm}$	Logarithmic mean temperature at a tube heat exchanger, °C
327	$v$	Flow velocity in a cross-section of a tube heat exchanger, m·s <sup>-1</sup>
328	$V$	Electrical voltage, V
329	$V_c$	Volume of a cooling tower, m <sup>3</sup>
330	$V_p$	Volume of an electroplating bath, m <sup>3</sup>
331	$V_{T1}$	Volume of a water reservoir tank 1, m <sup>3</sup>
332	$V_{T2}$	Volume of a water reservoir tank 2, m <sup>3</sup>
333	$V_{tube}$	Volume of a tube heat exchanger, m <sup>3</sup>
334	$U_o$	Overall heat transfer coefficient, kW·m <sup>-2</sup> ·°C <sup>-1</sup>
335	$\lambda_{evap}$	Latent heat of vaporization of water, kJ·kg <sup>-1</sup>
336	$\rho_p$	Density of plating solution, kg·m <sup>-3</sup>
337	$\rho_w$	Density of water, kg·m <sup>-3</sup>
338	$\mu_w$	Dynamic viscosity of water, kg·m <sup>-1</sup> ·s <sup>-1</sup>

339 **References**

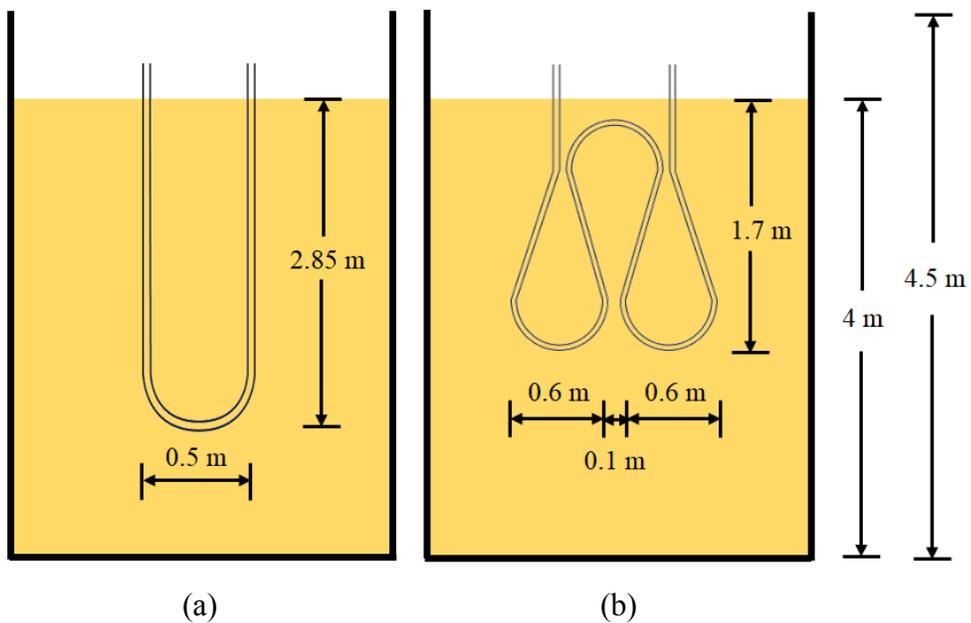
- 340 [1] E. Svenson, DuraChrome hard chromium plating, Plating resources, Inc., Florida, 2006,  
341 pp. 1-40.
- 342 [2] G.A. Lausmann, Electrolytically deposited hard chrome, Surf. and Coat. Technol 86-87  
343 (1996), pp. 814-820.
- 344 [3] N.V. Mandich, D.L. Snyder, Modern electroplating, fifth ed., John Wiley & Sons, New  
345 Jersy, 2010, pp. 205-248.
- 346 [4] A.K. Graham, Electroplating Engineering Handbook, Reinhold, U.S.A., 1955.
- 347 [5] L. Zitko, G. Cushnie, P. Chalmer, R. Taylor, Hard chrome plating training course, The  
348 National Center for Manufacturing Sciences, Michigan, 2010.
- 349 [6] F.A. Lowenheim, Modern Electroplating, 3<sup>rd</sup> Ed., J Wiley & Son, U.S.A., 1974.
- 350 [7] S. Tanthadiloke, P. Kittisupakorn, I. M. Mujtaba, Improvement of production  
351 performance of a hard chromium electroplating via operational optimization. Proc. 5<sup>th</sup>  
352 Reg. Conf. Chem. Eng., Thailand (2013) 221-224.
- 353 [8] S. Tanthadiloke, P. Kittisupakorn, I. M. Mujtaba, Modeling and design a controller for  
354 improving the plating performance of a hard chromium electroplating process, Comput.  
355 Aided Chem. Eng. 33 (2014) 805-810.
- 356 [9] D.G. Prabhanjan, G.S.V. Paghavan, Comparison of heat transfer rates between a straight  
357 tube heat exchanger and a helically coiled heat exchanger, Int. J. Heat Mass Transf. 29  
358 (2005) 185-191.

- 359 [10] Y.A. Çengel, Heat Transfer: A Practical Approach, 2<sup>nd</sup> Ed., McGraw-Hill, U.S.A., 2003.
- 360 [11] S. Niamsuwan, P. Kittisupakorn, I. M. Mujtaba, A newly designed economizer to  
361 improve waste heat recovery: A case study in a pasteurized milk plant, J. Appl. Therm.  
362 Eng. 60 (2013) 188-199.
- 363 [12] A. Zachar, Analysis of coiled-tube heat exchangers to improve heat transfer rate with  
364 spirally corrugated wall, Int. J. Heat Mass Transf. 53 (2010) 3928-3939.
- 365 [13] P. Naphon, S. Wongwises, A review of flow and heat transfer characteristics in curved  
366 tubes, Renew. Sustain. Energy Rev. 10 (2006) 463-490.
- 367 [14] W. Lin, N. Qiao. In-plan vibration analyses of curved pipes conveying fluid using the  
368 generalized differential quadrature rule, Comput. Struct. 86 (2008) 133-139.
- 369 [15] S. Gunes, V. Ozceyhan, B. Orhan, Heat transfer enhancement in tube with equilateral  
370 triangle cross sectioned coiled wire inserts, Exp. Therm. Fluid Sci. 34 (2010) 684-691.
- 371 [16] S. Gunes, V. Ozceyhan, The experimental investigation of heat transfer and pressure drop  
372 in a tube with coiled wire inserts placed separately from the tube wall, Appl. Therm. Eng.  
373 30 (2010) 1719-1725.
- 374 [17] L. Cheng, T. Luan, W.D.M. Xu, Heat transfer enhancement by flow-induced vibration in  
375 heat exchangers, Int. J. Heat Mass Transf. 52 (2009) 1053-1057.
- 376 [18] A. Thaikua, P. Kittisupakorn, S. Tanthadiloke, Temperature control by heat exchanger  
377 incorporating with vibration type coiled-tube, Proc. Int. Multiconf. Eng. Comput. Sci.  
378 2012 Vol II, Hong Kong (2012) 1357-1361.

- 379 [19] V. Kumar, P. Gupta, K. D. P. Nigam, Fluid flow and heat transfer in curved tubes with  
380 temperature-dependent properties, *Ind. Rng. Chem. Res.* 46(2007) 3226-3236.
- 381 [20] M. Yasuo, N. Wataru, Study on forced convective heat transfer in curved pipes, *Int. J.*  
382 *Heat Mass Transf.* 8 (1965) 67-82.
- 383 [21] R. Yang, S. F. Chang, W. Wu, Flow and heat transfer in a curved pipe with periodically  
384 varying curvature, *Int. Commun. Heat Mass Transf.* 27(2000) 133-143.
- 385 [22] C. Camci, D. H. Rizzo, Secondary flow and forced convection heat transfer near endwall  
386 boundary layer fences in a 90° turning duct, *Int. J. Heat Mass Transf.* 45 (2002) 831-843.
- 387 [23] B.W. Bequette, *Process Dynamics Modeling, Analysis, and Simulation*, 1<sup>st</sup> Ed., Prentice  
388 Hall, U.S.A., 1998.
- 389 [24] F.P. Incropera, D. P. DeWitt, *Fundamentals of Heat and Mass Transfer*, 6<sup>th</sup> Ed., J Wiley  
390 & Son, U.S.A., 2007.
- 391 [25] R.B. Bird, W.E. Stewart, E.N. Lightfoot, *Transport Phenomena*, 2<sup>nd</sup> Ed., J Wiley & Son,  
392 U.S.A., 1998.
- 393 [26] P. Naphon, Study on heat transfer characteristics of an evaporative cooling tower, *Int.*  
394 *Commun. Heat Mass Transf.* 32 (2005) 1066-1074.
- 395 [27] R.H. Perry, *Perry's Chemical Engineering Handbook*, 6<sup>th</sup> Ed., McGraw-Hill, U.S.A.,  
396 1984.
- 397 [28] C. Veiga, J. P. Davim, A. J. R. Loureiro, Properties and application of titanium alloys: A  
398 brief review, *Rev. Adv. Mater. Sci.* 32 (2012) 133-148.

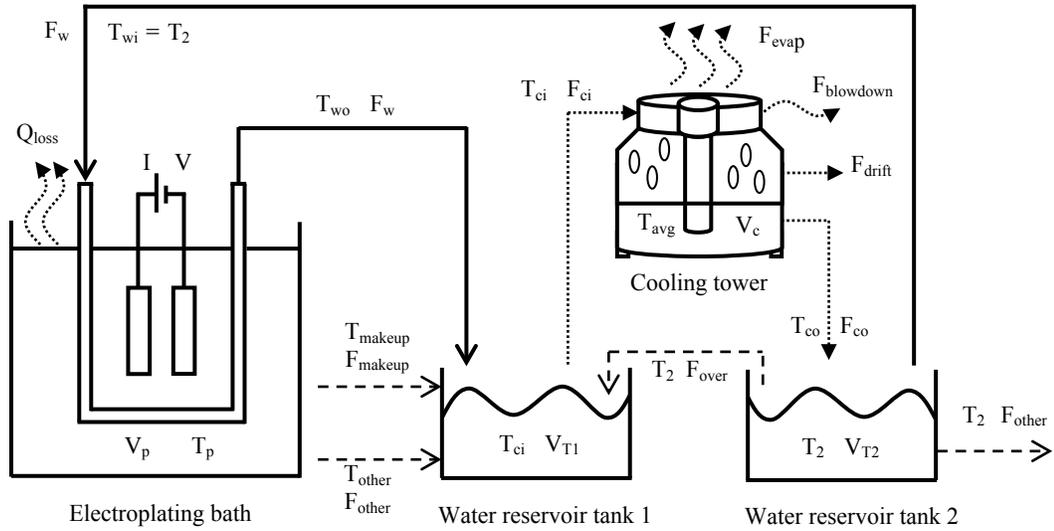


**Fig. 1** Hard chromium electroplating process with the cooling system.

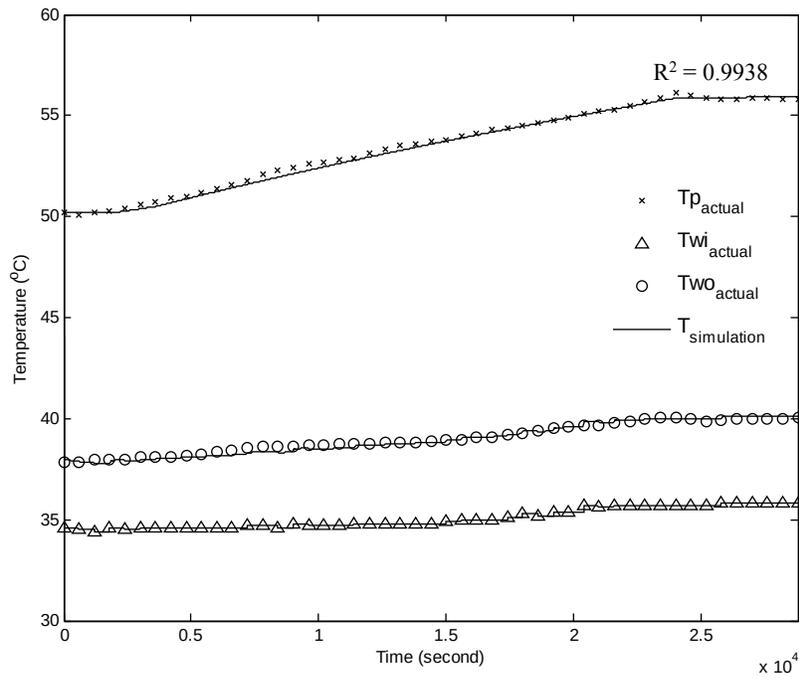


**Fig. 2** Illustration of the heat exchangers inside the hard chromium electroplating bath:

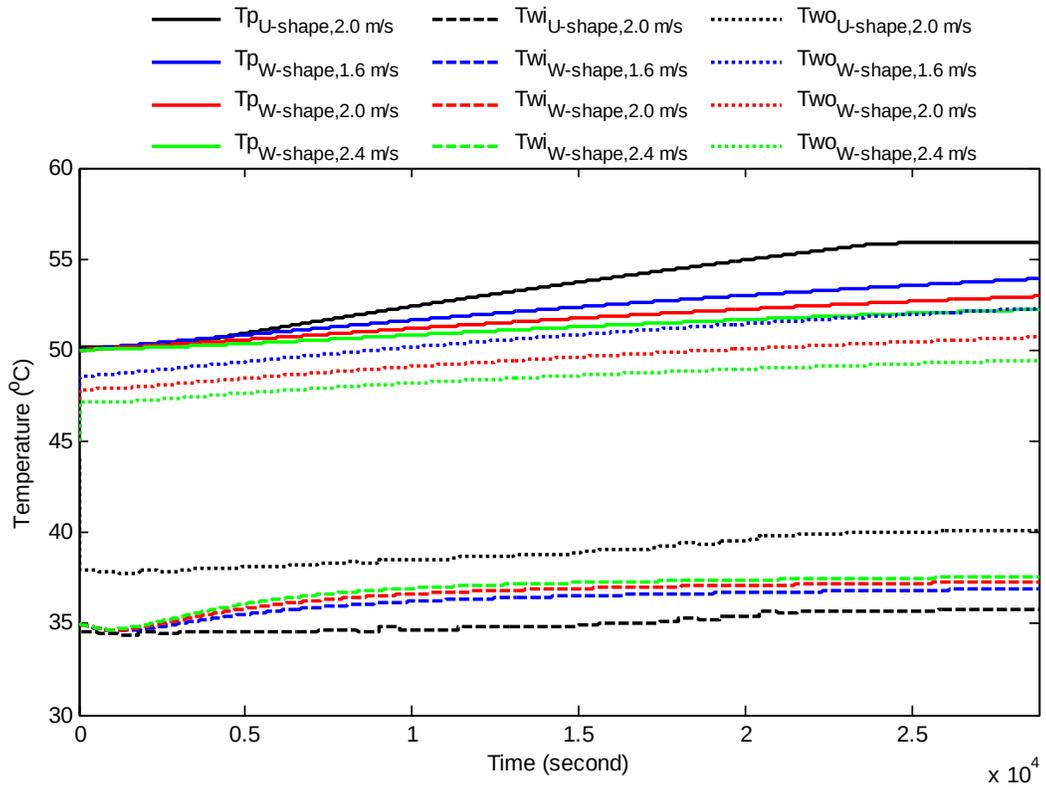
(a) U shape heat exchanger and (b) W serpentine shape heat exchanger.



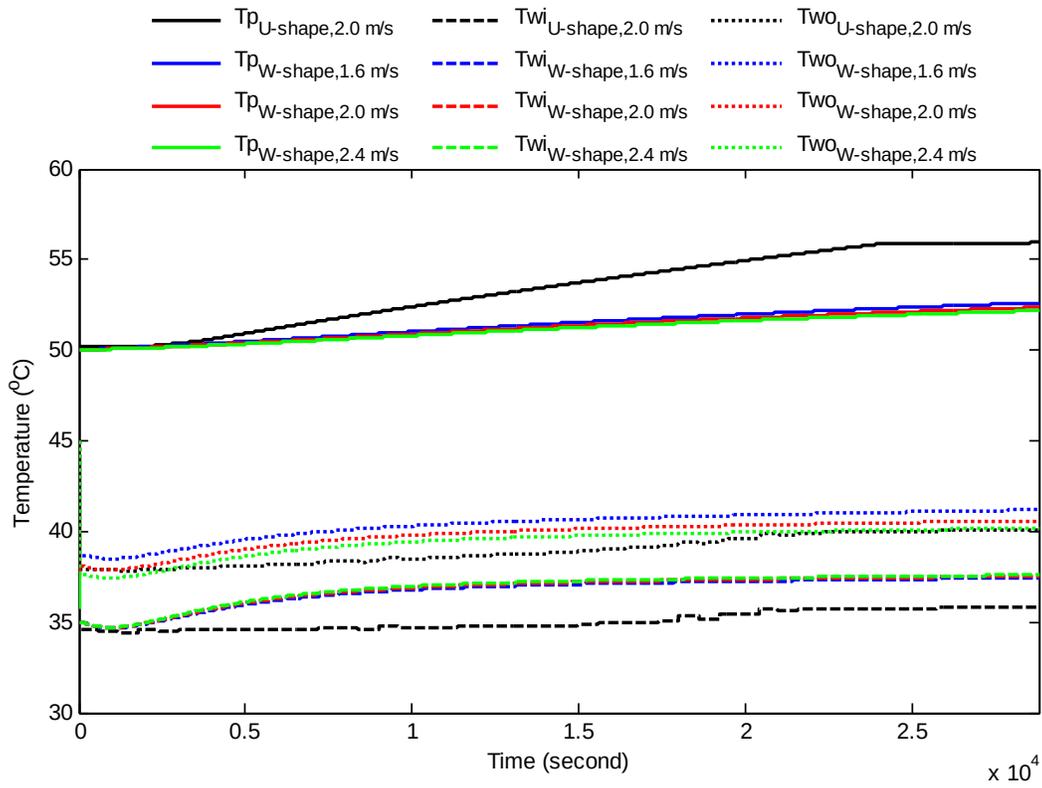
**Fig. 3** Schematic diagram of the hard chromium electroplating process with mass and energy balance.



**Fig. 4** Comparison results between simulation and actual data of plating solution temperature and water temperature at inlet and outlet of the electroplating bath.



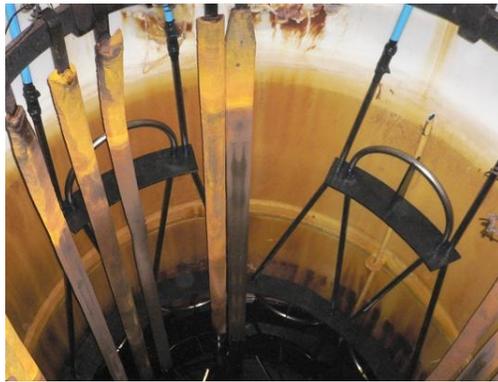
**Fig. 5** The temperature profile of plating solution, water inlet and outlet at the electroplating bath for 1.27 cm diameter of W serpentine shape tube heat exchanger at various water velocities.



**Fig. 6.** The temperature profile of plating solution, water inlet and outlet at the electroplating bath for 2.54 cm diameter of W serpentine shape tube heat exchanger at various water velocities.

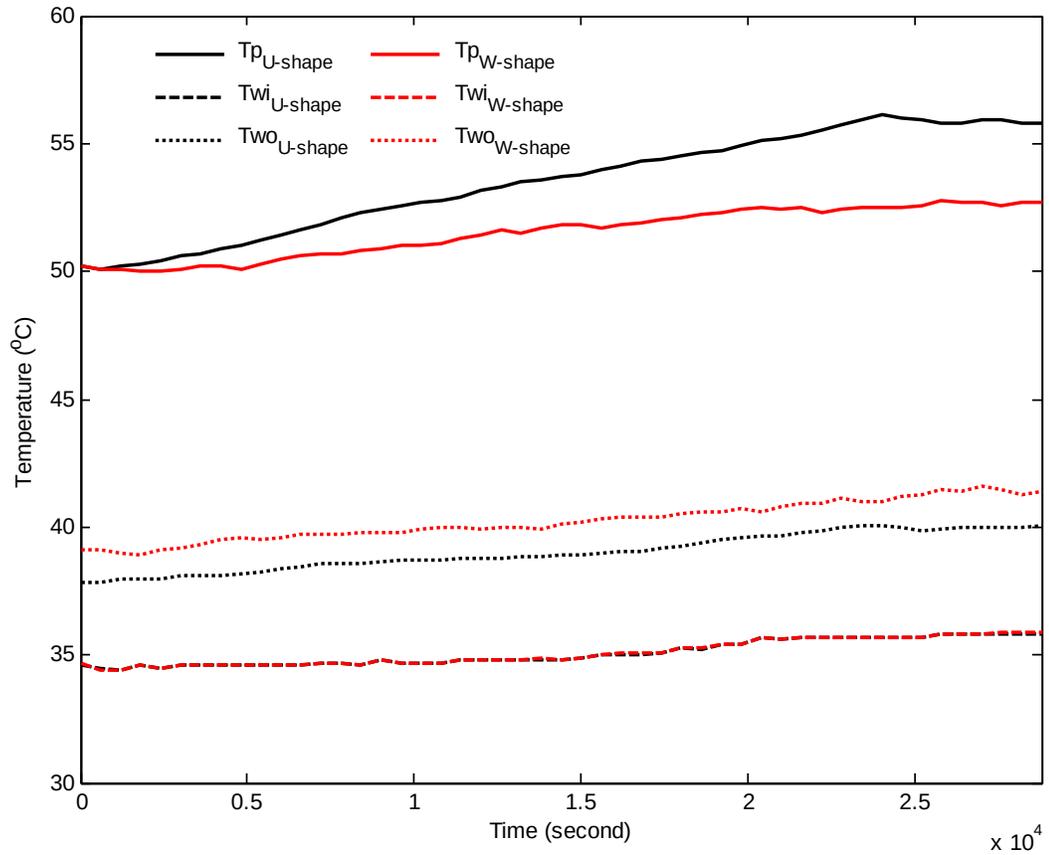


(a) The W serpentine shape tube heat exchanger.



(b) The installation of the W serpentine shape tube heat exchanger in the electroplating bath.

**Fig. 7** The implementation of W serpentine shape tube heat exchanger.



**Fig. 8** Comparison of temperature profile of plating solution, water inlet and outlet at the electroplating bath with the cooling water flow velocity at 2.0 m/s.

**Table 1**

Physical properties [27, 28].

<b>Physical property</b>	<b>Unit</b>	<b>Value</b>
Density of water	kg/m <sup>3</sup>	992.25
Density of plating solution	kg/m <sup>3</sup>	1,174.4
Heat capacity of water	kJ/kg·°C	4.181
Heat capacity of plating solution	kJ/kg·°C	4.917
Latent heat of vaporization of water	kJ/kg	2,260
Thermal conductivity of titanium	kW/m·°C	0.0206

**Table 2**

Simulation system geometric characteristics.

<b>System characteristic</b>	<b>Unit</b>	<b>Value</b>
Inner diameter of a 1.27 cm diameter tube heat exchanger	m	0.0111
Outer diameter of a 1.27 cm diameter tube heat exchanger	m	0.0127
Inner diameter of a 2.54 cm diameter tube heat exchanger	m	0.0238
Outer diameter of a 2.54 cm diameter tube heat exchanger	m	0.0254
Volume of an electroplating bath	m <sup>3</sup>	9.3062
Volume of a water tank 1	m <sup>3</sup>	2.1155
Volume of a water tank 2	m <sup>3</sup>	2.5663
Volume of a cooling tower	m <sup>3</sup>	0.3771

**Table 3**

Operating conditions for simulation.

<b>Operating condition</b>	<b>Unit</b>	<b>Value</b>
Outlet water temperature to other electroplating baths	°C	44.1
Water make up temperature	°C	34.9
Air temperature	°C	30
Volumetric flow rate of cooling water in other electroplating baths flow to a cooling tower	m <sup>3</sup> /s	4.3364 x 10 <sup>-4</sup>
Water make up to a cooling tower	m <sup>3</sup> /s	7.7597 x 10 <sup>-6</sup>
Water evaporation rate in a cooling tower	m <sup>3</sup> /s	4.3238 x 10 <sup>-6</sup>
Water blow down rate of a cooling tower	m <sup>3</sup> /s	1.0809 x 10 <sup>-6</sup>
Water drift loss of a cooling water	m <sup>3</sup> /s	2.3550 x 10 <sup>-6</sup>